### Planar Monocular SLAM

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#### 1 Introduction

The aim of the project is to develop a full SLAM system capable of determining the trajectory followed by a robot when moving in an environment with a representation of the environment itself (the map consisting of the landmarks). In particular, the program has to work with an initial guess of the trajectory given by the odometry and an image for each of the pose of the robot in the trajectory itself. The image (actually a simplified data structure containing for each seen landmark its image coordinates and its appearance) must be used in order to improve the trajectory and build the map of the environment.

The approach followed is a total least squares method, integrating posepose constraints given by the odometry and pose-landmark constraints given by each image. Before executing the least squares algorithm, the position of each landmark is initialized with a Direct Linear Transformation (DLT) algorithm. Each landmark is associated to a certain landmark depending on its appearance, using a k-d tree, initialized with the appearance of all the landmarks of the map (hence simplifying the problem of updating the k-d tree depending on all the measurements).

The program, entirely written in C++, manages to correctly find the right trajectory, making it correspond exactly with the ground truth. The landmarks are correctly reconstructed as well, with the exception of a small fraction which did not converge to the right position due to a bad initialization.

### 2 Landmark Initialization

As introduced in the previous section, the position of each landmark is initialized with the DLT algorithm, following the analysis discussed in [1]. The

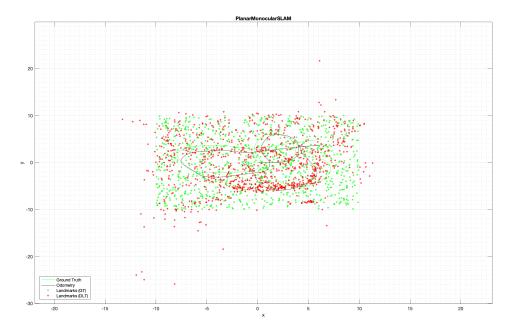


Figure 1: Initial reconstruction of the landmarks using the DLT algorithm.

data available in the dataset allow to use this technique which depends only on the homogeneous camera projection matrix of each pose (initialized with the odometry, the transform between the robot and the camera and the camera calibration matrix of the dataset). A matrix is initialized for each landmark with all the measurements from all the positions in the odometry, then following Algorithm A5.4 in [1], the position of the landmark is initialized. The initial reconstruction can be seen in Fig. 1.

Note that in this step each measurement is associated to a certain landmark depending on the data (appearance of the landmark itself) contained in the k-d tree. If no association can be done the measurement is discarded.

## 3 Least Squares

Once the position of each landmark has been initialized, a least squares algorithm optimized the given constraints. In particular, pose-pose constraints have been used from the odometry, expressing the pose of each robot with respect to the previous pose in the trajectory, and pose-landmark constraints have been used from the camera measurements, where each landmark is

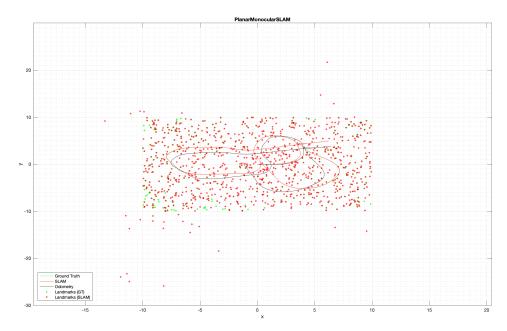


Figure 2: Result obtained after the execution of the least squares algorithm on pose-pose (odometry) and pose-landmark (projective) constraints.

expressed in the image coordinates of the corresponding pose.

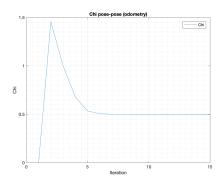
The implementation of the least squares follows a similar implementation of the total least squares shown during the lectures, the Jacobians have been computed analitically and the algorithms has been executed for 15 iterations.

Fig. 2 shows the result of the least squares algorithm at the end of its execution. Notice that the ground truth of the trajectory is completely covered by the solution as well as most of the landmarks. As already introduced before, the landmark which did not converge are those who were initialized with a value too far away from the right one.

Fig. 3 shows how chi changes for both pose-pose (odometry) and pose-landmark (projective) constraints.

### 4 Conclusion

The implemented algorithm obtained great results in both the trajectory and the map reconstruction. Nevertheless, it can be improved a lot by better exploiting the given data. More pose-pose constraints can be added by triangulating the poses (e.g. by using the 8-point algorithm), landmark-landmark



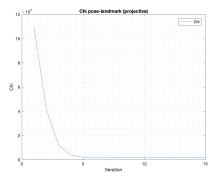


Figure 3: Behaviour of Chi through each iteration of least squares. On the left pose-pose constraints (odometry), on the right pose-landmark constraints (projective).

constraints could be added by considering, again, the given relations between poses and landmarks due to the camera. The k-d tree implementation can be improved by considering that the landmarks should be initialized with the appearance of the landmarks coming from the measurements. In the end, the least squares implementation is not exploiting the sparsity of the matrix H, which should boost the performances and massively decrease the amount of memory used in this step.

# References

[1] R. I. Hartley and A. Zisserman, *Multiple View Geometry in Computer Vision*. Cambridge University Press, ISBN: 0521540518, second ed., 2004.