Guide to the STACMR Matlab package

21 August 2017

STACMR is a set of Matlab functions that implement the Conjoint Monotonic Regression (CMR) approach to State-Trace Analysis (STA). This is a quick guide to its use.

Contents

1	Starting up			2	2	
2	Partial order				2	
3	Continuous data					
	3.1	Input	data structures	. 3	3	
	3.2	Princi	ipal functions	. 3	3	
		3.2.1	staSTATS.m	. 4	1	
		3.2.2	staPLOT.m	. 5	5	
		3.2.3	staMR.m	. 7	7	
		3.2.4	staCMR.m	. 8	3	
		3.2.5	staMRFIT.m	. 9)	
		3.2.6	staCMRFIT.m 10)	
4	Binary data 1					
	4.1	Input	data structures	. 11	1	
	4.2	Princip	iple functions	. 12	2	
		4.2.1	staSTATSBN.m	. 12	2	
		4.2.2	staPLOTBN.m	. 13	3	
		4.2.3	staMRBN.m	. 14	1	
		4.2.4	staCMRBN.m	. 15	5	
		4.2.5	staMRFITBN.m	. 16	3	
		4.2.6	staCMRFITBN.m	. 17	7	

1 Starting up

- 1. Unzip the file STACMR-matlab.zip.
- 2. Place the folder STACMR-matlab and subfolders on the Matlab path.
- 3. Run staCMRsetup. This locates and links the most recent java runtime library.

You should now be good to go.

2 Partial order

The various STACMR functions often make use of an optional partial order. A partial order on a vector, x, is a set of pairs, (i, j), such that $x_i \leq x_j$. This is represented in STACMR in two (equivalent) ways:

- 1. As a cell array containing the set of (i, j) pairs, such as, $\{[1\ 2], [2\ 3], [1\ 4]\}$. There is a shorthand for a linear order such as, $\{[1\ 2], [2\ 3]\}$, which can be written as, $\{[1\ 2\ 3]\}$ or, even more simply, as $\{1:3\}$.
- 2. As an adjacency matrix in which entry (i, j) = 1 if (i, j) is an element of the partial order, otherwise (i, j) = 0.

The function, cell2adj, converts a partial order in cell array form into its corresponding adjacency matrix form. For example,

```
>> E = \{[1 \ 2] \ [2 \ 3] \ [1 \ 4]\};
>> A = cell2adj (1:4, E)
A =
       0
               1
                       0
                                1
       0
               0
                       1
                                0
       0
               0
                       0
                                0
       0
               0
```

In the above call to cell2adj, the vector, 1:4, specifies the set that the partial order applies to. It is almost invariably the sequence of numbers, 1 to k, where k is the total number of conditions. In the above example, k=4. The function adj2cell converts an adjacency matrix into its corresponding cell array.

3 Continuous data

Continuous data has the form that each observation is a number drawn from a continuous distribution.

3.1 Input data structures

At present, STACMR accepts two kinds of data structure for continuous data:

- 1. Cell array format. In this format, the data are contained in a $b \times n$ cell array where b is the number of between-participant conditions (groups) and n is the number of dependent variables. Each component of this cell array is itself an $N \times w$ matrix of observations where N is the number of subjects (which may vary across groups and dependent variables) and w is the number of within-participant conditions (fixed across groups and dependent variables). The dependent variable may be either within-participant or between-participant it doesnt matter because the correlation between dependent variables is assumed to be zero (although this might change in future implementations).
- 2. **General format**. This is a fixed column format organised as a matrix in which each row corresponds to an observation and each column is defined as follows:
 - column 1: Participant number (for identification only, not used directly)
 - column 2: Between-participant condition or group (if none, then set this value to 1)
 - column 3: Dependent variable (numbered 1, 2, and so on)
 - columns 4 to end: Values for each within-participant condition

While STACMR accepts data in general format it always converts it to cell array format using the function,

```
>> y = gen2cell (data);
```

3.2 Principal functions

The principle functions are located in the folder, .../STACMR-matlab. Their operation is illustrated with respect to the dataset, delay, located in folder, .../STACMR-matlab/Data files.

The delay data set comes from the study by Dunn, J. C., Newell, B. R., & Kalish, M. L. (2012). The effect of feedback delay and feedback type on perceptual category learning. *Journal of Experimental Psychology: Learning, Memory and Cognition*, 38(4), 840-859.

Participants in this study completed one of two category-learning tasks over 4 blocks of training (a within-participant factor) under one of 2 different conditions (a between-participant factor). The dependent variables are the proportions correct for each of two tasks defined according to the category structure that participants learned. For the rule-based (RB) group, the category structure was defined by a simple rule. For the information-integration (II) group, the category structure was more complex and could not be defined by a simple rule.

The data are in general format and is contained in the file, delay.dat. That is,

```
>> delay = load('delay.dat'); % read the data file
>> y = gen2cell(delay); % convert to cell array format
```

3.2.1 staSTATS.m

This function computes summary statistics of a data structure in cell array format. Example call:

```
>> delaystats = staSTATS (y, shrink);
```

Input:

Here, y is the delay data in cell array format and shrink is an optional parameter denoting how much shrinkage to apply to the estimated covariance matrix. Generally, the covariance matrix needs to be shrunk during the bootstrap cycle to avoid ill-conditioning. If shrink = 0 then no shrinkage is applied. If shrink = 1 then maximum shrinkage is applied. This means that the covariance matrix is diagonalized with all off-diagonal entries set to zero. If shrink < 0 (the default) then an optimal shrinkage value is estimated for each within-participant block and applied according to an algorithm developed by: Ledoit, O. & Wolf, M. (2004). Honey, I shrunk the sample covariance matrix, The Journal of Portfolio Management, 30(4), 110-119.

Output:

staSTATS returns in the variable delaystats a cell array of length equal to the number of dependent variables in y. Each component of delaystats is a structured array. For the dependent variable, ivar:

- delaystats{ivar}.means = vector of means across all conditions
- delaystats{ivar}.cov = the covariance matrix (for information only)
- delaystats{ivar}.regcov = the adjusted covariance matrix following application of shrinkage
- delaystats{ivar}.n = matrix of number of observations (subjects) in each within-participant block
- delaystats{ivar}.lm = matrix of Loftus-Masson within-participant standard errors (used by staPLOT)
- delaystats{ivar}.weights = matrix of weights defined by: delaystats{ivar}.n.*delaystats{ivar}.regcov^-1
- delaystats{ivar}.shrinkage = a vector of length b (where b is the number of levels of the between-participant independent variable) containing the specified or estimated shrinkage values

Thus, delaystats has two components corresponding to the two dependent variables in delay. If you look at the means, they should look like this:

```
>> disp(delaystats{1}.means)
0.3676  0.4676  0.5757  0.6118  0.3445  0.4434  0.5081
0.5169
>> disp(delaystats{2}.means)
0.3308  0.4550  0.5346  0.5492  0.2836  0.3031  0.3180
0.3098
```

3.2.2 staPLOT.m

Generates a state-trace plot for continuous data.

Example call:

```
>> staPLOT(delay, 'groups', {1:4, 5:8}, 'labels', ...
{'No delay', 'Delay'}, 'axislabels', {'RB','II'});
```

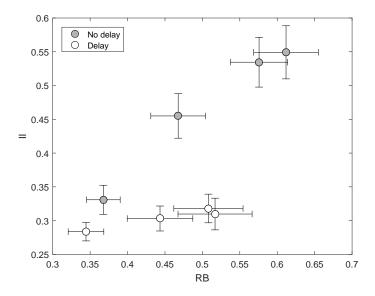


Figure 1: Output from staPLOT based on delay data set.

Input:

- delay is the name of the data set and is the one required argument. It may be in either general or cell-array format, or in summary statistics form (i.e., the output of staSTATS described below). If the input is a data structure then staPLOT invokes staSTATS and accepts an optional covariance shrinkage parameter (also explained above). The plot includes error bars.
- 'groups' identifies the conditions to be distinguished in the plot with different markers. For the delay data, conditions 1 to 4 correspond to the *no delay* group and conditions 5 to 8 correspond to the delay group. This is passed to staPLOT by setting the value of 'groups' to the cell array, {1:4, 5:8}. Up to four groups can be defined in this way.
- 'labels' is a cell array consisting of the labels for the groups defined by 'groups' to appear in the legend. In the present example, this is specified by the cell array, {'No delay','Delay'}.
- 'axislabels' is a cell array that defines the labels on the x-axis and y-axis, respectively (note: the same result can be achieved using the Matlab functions, xlabel and ylabel). In the present example, the labels are defined by the cell array, {'RB','II'}, for rule based and information integration, respectively.

• 'predicted' is a cell array consisting of predicted values for each condition. Typically, this is the best-fitting values returned by staMR or staCMR (see below).

Output:

Output is shown in Figure 1.

3.2.3 staMR.m

This function conducts monotonic regression on a data structure according to a given partial order. We say it fits the partial order model to the data (i.e., the set of dependent variables).

Example call:

```
>> [x, f, shrinkage] = staMR (data, E, shrink);
```

Input:

Here, data is either a data structure (in cell array or general format) or structured output from staSTATS; E is a partial order (required) in either cell array or adjacency matrix format; shrink is an optional shrinkage parameter (defined previously). If data is a cell array of structured output from staSTATS, then the shrinkage specified by this output is used whether the argument shrink is specified or not.

Output:

- x is a *n*-element cell array of that contains the best-fitting values for each dependent variable
- f is the value of the least squares fit
- shrinkage is a $b \times n$ matrix of shrinkage values (where b is the number of levels of the between-participant independent variable)

Try staMR with delay. To do so, we have to specify a partial order. Use the following:

```
0.4676
               0.4550
    0.5757
               0.5346
    0.6118
               0.5492
    0.3445
               0.2830
    0.4434
               0.3034
    0.5081
               0.3149
    0.5169
               0.3149
>> disp(f2);
    0.1721
>> disp(shrinkage2);
    0.0520
               0.0491
               0.2650
    0.0314
```

3.2.4 staCMR.m

This is the main function that conducts the CMR (state-trace) analysis. It takes a data structure or a cell array of structured output from staSTATS and an optional partial order and returns the best fitting values (to the data means) and the least squares fit. It fits the monotonic model to the data.

Example call:

```
>> [x, f, s] = staCMR (data, E, shrink);
```

On the input side, data is a data structure, E is an optional partial order, and shrink is an optional shrinkage parameter (defined previously).

On the output side, x is a cell array of the best-fitting values, f is the value of the least squares fit, and s is a structured array of fit statistics. The component, s.shrinkage, is a $b \times n$ matrix of shrinkage values.

Now try staCMR with delay:

```
0.4806 0.3227
0.4850 0.3227
>> disp(f1);
1.7493
>> disp(s1.shrinkage);
0.0520 0.0491
0.0314 0.2650
```

3.2.5 staMRFIT.m

This function tests the fit of the partial order model.

Example call:

```
>> [p,datafit,fits]=staMRFIT(data, name-value pairs);
```

Input:

The stamperit function takes the following arguments:

- data is the name of a data structure (either in general format, cell array format), or structured output from staSTATS. If a data structure is specified then the bootstrap re-sampling is non-parametric. If only the summary statistics are provided (e.g., delaystats) then the bootstrap is parametric and assumes that observations are distributed normally for each dependent variable in each condition.
- 'partial', 'part', 'p' is a required partial order. This may be in either cell array or adjacency matrix form.
- 'nsamples', 'ns', 'n' is the number of Monte-Carlo samples to be drawn in computing the empirical sampling distribution of the fit value.
- 'shrink' is the optional shrink parameter, defined previously.

Output:

• p is the estimated p-value for the hypothesis that the fit of the model is zero. It is the proportion of bootstrap fit values that are greater than or equal to the observed fit value. Note that it will be different from run to run, as it is a Monte Carlo estimate.

- datafit is the observed fit value. It is the same as f1 returned by staMR above.
- fits is a vector of length nsample of computed bootstrap fit values. Thus, p is the proportion of values of fits that are greater than or equal to datafit.

Applying stamper as follows produced the following outputs:

3.2.6 staCMRFIT.m

This function estimates the empirical distribution (and hence p-value) of the difference in the fit of the conjoint monotonic and the fit of the partial order model. The function call is analogous to staMRFIT:

```
>> [p,datafit,fits]=staCMRFIT(data, name-value pairs);
```

Input:

- data is the name of the data structure (in either general or cell array format) or the name of structured output from staSTATS). If specified as a data structure then the bootstrap re-sampling is non-parametric, otherwise the bootstrap is parametric and assumes that observations are distributed normally for each dependent variable in each condition.
- 'partial' is an optional partial order in either cell array or adjacency matrix form.
- 'nsamples' is the number of Monte-Carlo samples to be drawn in computing the empirical sampling distribution of the fit value. We recommend using about 10,000 for estimating p to the nearest 100th.
- shrink is the optional shrink parameter, defined previously.

Output:

• p is the estimated p-value for the hypothesis that the difference in fit between the monotonic model and the partial order model is zero. It is the proportion of differences of bootstrap fits values that are greater than or equal to the observed difference in fit value.

- datafit is the observed difference in fit value between the monotonic model and the partial order model.
- fits is a vector of length nsample of computed differences in bootstrap fit values. Thus, p is the proportion of components of fits that are greater than or equal to datafit.

Applying staCMRFIT to the delay data produces the following output:

4 Binary data

Binary data has the form that each observation is either a 'success' or a 'failure'. STACMR assumes that these observations have been aggregated into counts of the total number of successes and failures for each participant and each condition.

4.1 Input data structures

At present, STACMR accepts two kinds of data structure for binary data:

- 1. Cell array format. In this format, the data are contained in a $N \times n$ cell array where N is the number of observation units (typically, participants) and n is the number of dependent variables. Each component of this cell array is itself an $k \times 2$ matrix of counts of successes and failures, respectively, where k is the number of conditions.
- 2. **General format**. This is a fixed column format organised as a matrix in which each row corresponds to a particular observation unit (participant) and condition. Each column is defined as follows:

```
column 1: Participant number column 2: Condition number (if none, then set this value to 1) column 3: Dependent variable (numbered 1, 2, and so on) column 4: Count of number of successes column 5: Count of number of failures
```

Data in general format are converted to cell array format using the function,

```
>> y = BNgen2cell (data);
```

4.2 Principle functions

The principle functions are located in the folder, .../STACMR-matlab. Their operation is illustrated with respect to the dataset, dfie, located in folder, .../STACMR-matlab/Data files.

We illustrate the binary STACMR functions using The dfie data set reported by Prince, M., Hawkins, G., Love, J., & Heathcote, A. (2012). An R package for state-trace analysis. *Behavior Research Methods*, 44(3), 644-655.

In this study, the dependent variables were accuracy of memory for pictures of faces and accuracy of memory for pictures of houses. There were k=6 conditions defined by the combination of two factors; stimulus orientation (upright, inverted), and study duration (short, medium, and long). There were N=18 participants each of whom were tested under all six conditions on both dependent variables. The data from each participant therefore can be analyzed individually.

The data (counts of hits and misses) for each participant are contained in the text file, dfie.dat:

```
>> dfie = load('dfie.dat'); % read general format
>> y = BNgen2cell(dfie); % convert to cell array
```

4.2.1 staSTATSBN.m

This function returns summary statistics for binary data.

Example call:

```
>> dfiestats = staSTATSBN (y);
```

The output, dfiestats, consists of a $N \times n$ cell array each component of which is a participant (indexed by isub) and a dependent variable (indexed by dvar). Each such component consists of the following:

- dfiestats{isub, dvar}.count = matrix of counts of successes and failures for each condition.
- dfiestats{isub, dvar}.means = vector of 'means' corresponding to the proportion of successes for each condition.
- dfiestats{isub, dvar}.weights = vector of weights corresponding to the number of trials (i.e., number of successes + number of failures) for each condition.
- dfiestats{isub, dvar}.n = vector of counts corresponding to the number of trials for each condition. Identical to weights.

4.2.2 staPLOTBN.m

Generates a state-trace plot for binary data.

Example call:

```
>> staPLOTBN(dfie, 'subj', 1, 'groups', {1:3, 4:6}, ...
'labels', {'Upright', 'Inverted'}, 'axislabels', ...
{'Faces','Houses'});
```

This command produces the plot shown in Figure 2.

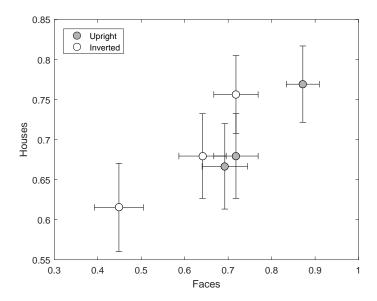


Figure 2: Output from staPLOTBN for Participant 1 from the dfie data set.

Input:

- dfie is the name of the data set and is the one required argument. It may be in either general or cell-array format, or in summary statistics form (i.e., the output of staSTATSBN).
- 'subj' identifies the participant number to be plotted.
- 'groups' identifies the conditions to be distinguished in the plot with different markers. For the dfie data, conditions 1 to 2 correspond to the upright orientation and conditions 4 to 6 correspond to the inverted orientation.

- 'labels' is a cell array consisting of the labels for the groups defined by 'groups' to appear in the legend.
- 'axislabels' is a cell array that defines the labels on the x-axis and y-axis, respectively.
- 'predicted' is a cell array consisting of predicted values for each condition (not shown here).

4.2.3 staMRBN.m

The function staMRBN fits a partial order model to a binary data structure.

Example call:

```
>> [x, f, g] = staMRBN (data, E);
```

Input

- data is the name of the binary data structure.
- E is a partial order (required) in either cell array or adjacency matrix format.

Output:

- x is an $N \times n$ -element cell array, where N is the number of observation units (participants) and n is the number of dependent variables. Each component of x is a k-element vector containing the best-fitting values for the corresponding participant and dependent variable.
- f is a N-vector containing the values of the least squares fit for each participant.
- q is a N-vector containing the G^2 fit for each participant.

Execute the following commands:

```
>> E = \{1:3,4:6\};
>> [x1, f1, q1] = staMRBN (dfiestats, E);
```

For participant 1, the observed means are:

The fitted means are:

```
>> [x1{1,:}]

ans =

0.7051     0.6731

0.7051     0.6731

0.8718     0.7692

0.4487     0.6154

0.6410     0.6795

0.7179     0.7564
```

The least-squares fit and G^2 values for this participant are:

```
>> [f1(1), g1(1)]
ans =
0.0321 0.1525
```

4.2.4 staCMRBN.m

This function fits the monotonic model to a binary data structure. Example call:

```
>> [x, f, g] = staCMRBN (data, E);
```

Input:

- data is the name of a binary data structure.
- E is an optional partial order in either cell array or adjacency matrix format.

Output:

• x is an $N \times n$ -element cell array, where N is the number of observation units (participants) and n is the number of dependent variables. Each component of x is a k-element vector containing the best-fitting values for the corresponding participant and dependent variable.

- f is a N-vector containing the values of the least squares fit for each participant.
- g is a N-vector containing the G^2 fit for each participant.

Execute the following commands:

```
\Rightarrow [x2, f2, g2] = staCMRBN (dfie, E);
```

For participant 1, the fitted means are:

```
>> [x2{1,:}]
ans =

0.7051     0.6752
0.7051     0.6752
0.8718     0.7692
0.4487     0.6154
0.6410     0.6752
0.7179     0.7564
```

The least-squares fit and G^2 values for this participant are:

```
>> [f2(1), g2(1)]
ans =
0.0342 0.1622
```

4.2.5 staMRFITBN.m

This function tests the fit of the partial order model to binary data. Example call:

```
>> [p, datafit, fits] = staMRFITBN (data, name-value pairs
);
```

Input:

- data is the name of the binary data structure.
- 'partial', 'p' is the partial order in cell array or adjacency matrix form.
- 'nsamples', 'n' is the number of Monte-Carlo samples.

Output:

- p is an N-vector containing the estimated p-values for each observation unit (participant).
- datafit is an N-vector containing the observed G^2 value for each each observation unit (participant).
- fits is a matrix of computed bootstrap G^2 values. Each row corresponds to each of N observation units (participants) and each row consists of a vector of length nsamples.

Example output (note that p and fits will be differ from run-to-run as they are Monte Carlo estimates):

4.2.6 staCMRFITBN.m

This function tests the difference between the fit of the partial order model and the fit of the monotonic model to binary data.

Example call:

```
>> [p, datafit, fits] = staCMRFITBN (data, name-value pairs
);
```

Input:

- data is the name of the binary data structure.
- 'partial', 'p' is an optional partial order in cell array or adjacency matrix form.
- 'nsamples', 'n' is the number of Monte-Carlo samples.

Output:

- p is an N-vector containing the estimated p-values for each observation unit (participant).
- datafit is an N-vector containing the observed G^2 value for each each observation unit (participant).

• fits is a matrix of computed bootstrap G^2 values. Each row corresponds to each of N observation units (participants) and each row consists of a vector of length nsamples.

Example output (note that p and fits will be differ from run-to-run as they are Monte Carlo estimates):