

The results are:

	$T_1 \cdot T_2$	A_H	$\delta a_2 2\pi^2(\pi^2 - 12)$
$N\bar{N} \rightarrow 1$	$-\frac{N^2-1}{2N}$	$\frac{1}{8}(N-1)N(N+1)$	0
$N\bar{N} \rightarrow \text{adj}$	$\frac{1}{2N}$	$\frac{1}{8}N$	$N^2\pi^2(\pi^2 - 12)$
$NN \rightarrow a$	$-\frac{N+1}{2N}$	$\frac{1}{4}(N+1)$	$\frac{1}{2}N(N-2)\pi^2(\pi^2 - 12)$
$NN \rightarrow s$	$\frac{N-1}{2N}$	$\frac{1}{4}(N-1)$	$\frac{1}{2}N(N+2)\pi^2(\pi^2 - 12)$
$\text{adj} \otimes \text{adj} \rightarrow 1$	$-N$	$\frac{1}{4}N^3$	0
$\text{adj} \otimes \text{adj} \rightarrow \text{adj}_S$	$-\frac{N}{2}$	$\frac{1}{8}N^3$	0
$\text{adj} \otimes \text{adj} \rightarrow \text{adj}_A$	$-\frac{N}{2}$	$\frac{1}{8}N(N^2 + 12)$	$-6\pi^2(\pi^2 - 12)$
$\text{adj} \otimes \text{adj} \rightarrow \bar{a}s + \bar{s}a$	0	$\frac{1}{4}N$	$V_H = -\frac{3}{2}N\pi^2(\pi^2 - 12)$
$\text{adj} \otimes \text{adj} \rightarrow \bar{a}a$	-1	$\frac{3}{4}N - \frac{1}{2}$	$\frac{1}{2}(N-1)(N-2)\pi^2(\pi^2 - 12)$
$\text{adj} \otimes \text{adj} \rightarrow \bar{s}s$	1	$\frac{3}{4}N + \frac{1}{2}$	$\frac{1}{2}(N+1)(N+2)\pi^2(\pi^2 - 12)$
$N \otimes \text{adj} \rightarrow N$	$-\frac{N}{2}$	$\frac{1}{8}N(N^2 + 2)$	$-\pi^2(\pi^2 - 12)$
$N \otimes \text{adj} \rightarrow a\bar{i}$	$-\frac{1}{2}$	$\frac{3}{8}N$	$\frac{1}{2}N(N-3)\pi^2(\pi^2 - 12)$
$N \otimes \text{adj} \rightarrow s\bar{i}$	$\frac{1}{2}$	$\frac{3}{8}N$	$\frac{1}{2}N(N+3)\pi^2(\pi^2 - 12)$

(8.8)

9 H Graph

The H-graph in Coulomb gauge was computed in Ref. [7]. Their Eq. (2.8) is

$$V = -\frac{81}{128}\pi(12 - \pi^2)\frac{\alpha^3}{q^2} \quad (9.1)$$

with $\alpha = (4/3)\alpha_s$.

$$V = \pi^2(\pi^2 - 12) \left[\frac{81}{128\pi} \left(\frac{4}{3} \right)^3 4\pi \right] \frac{4\pi\alpha_s}{q^2} \left(\frac{\alpha_s}{4\pi} \right)^2 = \pi^2(\pi^2 - 12) [6] \frac{4\pi\alpha_s}{q^2} \left(\frac{\alpha_s}{4\pi} \right)^2 \quad (9.2)$$

The QCD group theory factor for $N\bar{N} \rightarrow 1$ is 3, from the table, so the Coulomb H-graph is $2\pi^2(\pi^2 - 12)$ as expected in Eq. (8.7).

Summary: the graph

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$N \otimes \text{adj} \rightarrow N$	$-\frac{N}{2}$	$\frac{1}{8}N(N^2 + 2)$	$-\pi^2(\pi^2 - 12)$
$N \otimes \text{adj} \rightarrow a\bar{i}$	$-\frac{1}{2}$	$\frac{3}{8}N$	$\frac{1}{2}N(N-3)\pi^2(\pi^2 - 12)$
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{sec:coulomb}

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