## Longest Increasing Subsequence

Dada una lista, encuentra la subsecuencia creciente más larga. Puede configurarse qué significa "creciente". Ver ejemplos.

• Tiempo de procesamiento:  $O(n \log(n))$ 

```
#include <algorithm>
#include <cassert>
#include <cmath>
#include <iostream>
#include <numeric>
#include <vector>
template <class T, class Compare = std::less<T>>
auto longest increasing subsequence(const std::vector<T>& X,
                                    Compare comp = std::less<T>())
{
    long n = X.size();
    using PII = std::pair<int, T>;
    // M[k] = index i of smallest X[i] for which
    // there is a subsequence of length k ending
    // at X[i]. Note that M will be increasing.
    std::vector<PII> M(2);
    M.reserve((n + 2) / 2);
    // P[i] = parent \ of \ i.
    std::vector<int> P(n);
    int L = 1;
    M[1].first = 0;
    M[1].second = X[0];
    for (long i = 1; i < n; ++i)
    {
        auto first = M.begin() + 1;
        auto last = M.begin() + L + 1;
        const auto& xi = X[i];
        auto newLIter =
          std::partition_point(first, last, [xi, &comp](const PII& p) {
              return comp(p.second, xi);
          });
        auto newL = newLIter - first + 1;
```

```
P[i] = M[newL - 1].first;
       if (newL < M.size())</pre>
       {
           M[newL].first = i;
           M[newL].second = xi;
       }
       else
       {
           M.push_back({i, xi});
       }
       if (newL > L)
           L = newL;
    }
    std::vector<T> S(L);
    long k = M[L].first;
    for (auto it = S.rbegin(); it != S.rend(); ++it, k = P[k])
    {
       *it = X[k];
    }
   return S;
}
using namespace std;
template <class T>
std::ostream& operator<<(std::ostream& os, const std::vector<T>& A)
    for (const auto& x : A)
       os << x << ' ';
    return os;
}
int main()
{
    4, 5, 6, 4, 5, 3, 1, 5, 2, 6, 9};
    cout << "A = " << A << endl;
    cout << "Longest increasing subsequence: "</pre>
         << longest_increasing_subsequence(A) << endl;</pre>
    cout << "Longest non-decreasing subsequence: "</pre>
        << longest_increasing_subsequence(A, std::less_equal<int>()) << endl;</pre>
    cout << "Longest decreasing subsequence: "</pre>
```