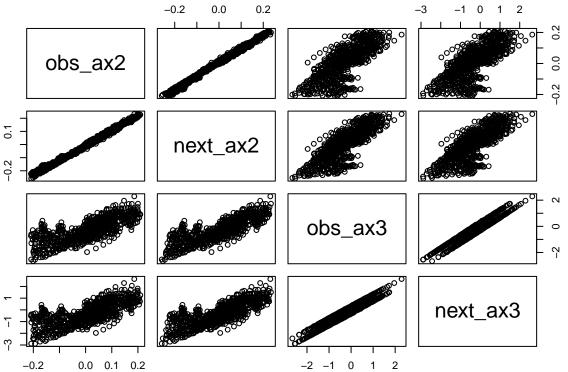
# Data Exploration

## Nathan Shepherd

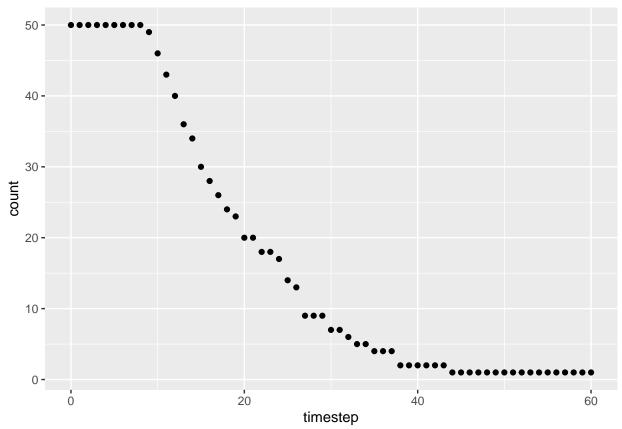
#### 2022-04-03

```
library(readr)
library(dplyr)
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
##
       intersect, setdiff, setequal, union
library(ggplot2)
rand_dat <- read_csv(".../utils/rand_state_acts.csv", show_col_types = FALSE)</pre>
names(rand_dat)
    [1] "timestep" "episode"
                               "reward"
                                           "act"
                                                      "obs_ax0"
                                                                  "next_ax0"
    [7] "obs_ax1"
                    "next_ax1" "obs_ax2"
                                           "next_ax2" "obs_ax3"
                                                                  "next_ax3"
summary(rand_dat)
##
       timestep
                        episode
                                         reward
                                                           act
##
          : 0.00
                            : 0.00
                                            : 9.00
                                                              :0.0000
    Min.
                    Min.
                                     Min.
                                                      Min.
##
    1st Qu.: 5.00
                    1st Qu.:14.00
                                     1st Qu.:16.00
                                                      1st Qu.:0.0000
##
    Median :10.00
                    Median :26.00
                                     Median :25.00
                                                      Median :1.0000
##
    Mean
           :12.46
                    Mean
                            :25.53
                                     Mean
                                             :25.92
                                                      Mean
                                                              :0.5568
##
    3rd Qu.:18.00
                    3rd Qu.:36.00
                                     3rd Qu.:32.00
                                                      3rd Qu.:1.0000
##
    Max.
           :60.00
                    Max.
                            :49.00
                                     Max.
                                             :61.00
                                                      Max.
                                                             :1.0000
##
       obs ax0
                             next ax0
                                                 obs ax1
                                                                     next ax1
##
           :-0.1096541
                                 :-0.12996
   Min.
                         Min.
                                              Min.
                                                     :-1.40519
                                                                         :-1.6015
                                                                 \mathtt{Min}.
##
    1st Qu.:-0.0156297
                          1st Qu.:-0.01832
                                              1st Qu.:-0.06116
                                                                 1st Qu.:-0.2266
##
    Median :-0.0000219
                         Median : 0.00432
                                              Median : 0.16127
                                                                  Median: 0.1625
           : 0.0242654
                          Mean
                                 : 0.02875
                                              Mean
                                                     : 0.22419
                                                                  Mean
                                                                         : 0.2461
    3rd Qu.: 0.0597766
                          3rd Qu.: 0.07109
##
                                              3rd Qu.: 0.55266
                                                                  3rd Qu.: 0.5563
                                 : 0.55580
                                                     : 1.88238
##
           : 0.5181503
                                                                         : 2.0789
                          Max.
                                              Max.
                                                                  Max.
##
       obs_ax2
                           next_ax2
                                               obs_ax3
                                                                  next_ax3
           :-0.20863
                               :-0.25873
                        Min.
                                            Min.
                                                   :-2.6632
                                                               Min.
                                                                      :-2.8973
    1st Qu.:-0.03345
                        1st Qu.:-0.05214
                                            1st Qu.:-0.7747
##
                                                               1st Qu.:-0.8118
##
   Median : 0.03682
                        Median : 0.03486
                                            Median :-0.1940
                                                               Median :-0.2275
##
           : 0.01503
                               : 0.01036
   Mean
                        Mean
                                            Mean
                                                   :-0.2336
                                                               Mean
                                                                      :-0.2620
    3rd Qu.: 0.06781
                        3rd Qu.: 0.07017
                                            3rd Qu.: 0.3324
                                                               3rd Qu.: 0.3572
##
    Max.
           : 0.20913
                        Max.
                               : 0.23477
                                            Max.
                                                   : 2.2920
                                                               Max.
                                                                      : 2.6358
```

# pairs(rand\_dat[9:12])



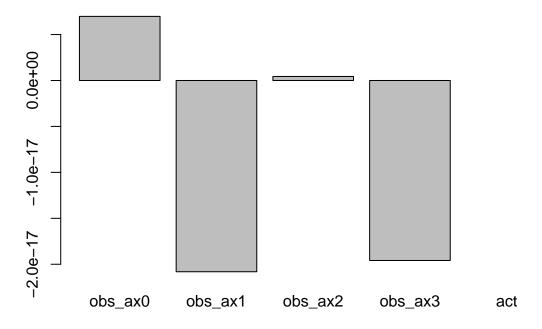
by\_timestep = rand\_dat %>% group\_by(timestep)
timestep\_summ = summarize(by\_timestep, count=n(), avg.reward=mean(reward))
ggplot(timestep\_summ, aes(x=timestep, y=count)) + geom\_point()



```
# Determine obs_axis with greatest difference for observation given the action
states = rand_dat %>% select(obs_ax0,obs_ax1,obs_ax2,obs_ax3,act)
sact0 = states %>% filter(act==0) %>% scale() %>% colMeans(na.rm = TRUE)
sact1 = states %>% filter(act==1) %>% scale() %>% colMeans(na.rm = TRUE)

sact0 - sact1

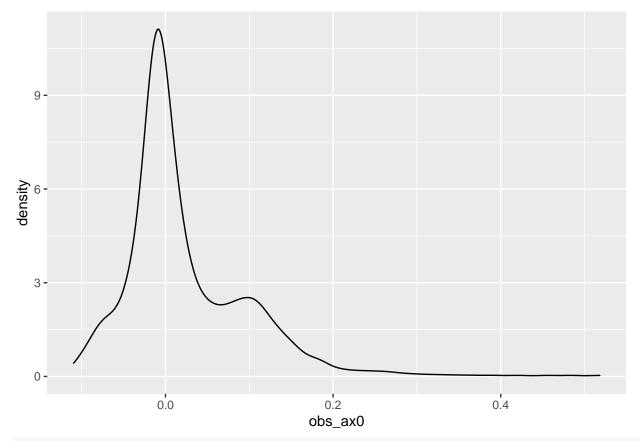
## obs_ax0 obs_ax1 obs_ax2 obs_ax3 act
## 6.976043e-18 -2.081486e-17 4.376055e-19 -1.958966e-17 NaN
barplot(sact0 - sact1)
```



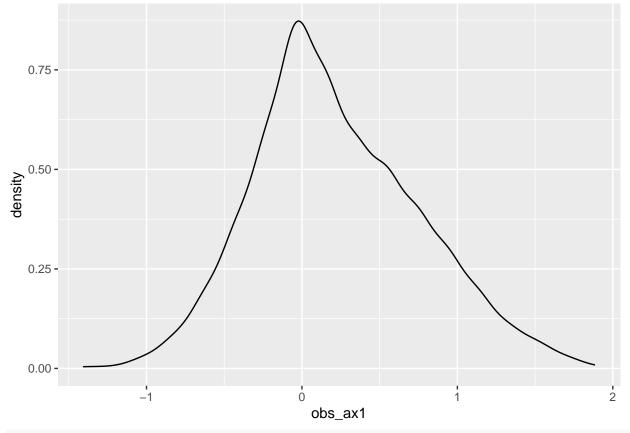
### **Exploratory Factor Analysis**

```
# Maximum Likelihood Factor Analysis
# entering raw data and extracting 3 factors,
# with varimax rotation
mydata = states[1:4] # drop act
fit <- factanal(mydata, 1, rotation="varimax")</pre>
print(fit, digits=2, cutoff=.3, sort=TRUE)
##
## Call:
## factanal(x = mydata, factors = 1, rotation = "varimax")
## Uniquenesses:
## obs_ax0 obs_ax1 obs_ax2 obs_ax3
      0.52
              0.07
                      0.45
                               0.00
##
## Loadings:
## [1] -0.70 -0.96 0.74 1.00
##
##
                  Factor1
## SS loadings
                     2.96
## Proportion Var
                     0.74
## Test of the hypothesis that 1 factor is sufficient.
## The chi square statistic is 2763.4 on 2 degrees of freedom.
## The p-value is 0
# plot factor 1 by factor 2
#load <- fit$loadings[,1:2]</pre>
#plot(load, type="n") # set up plot
\#text(load, labels=names(mydata), cex=.7) \# add variable names
# fraction of the variable's total variance explained by the factor
apply(fit$loadings^2, 1, sum)
```

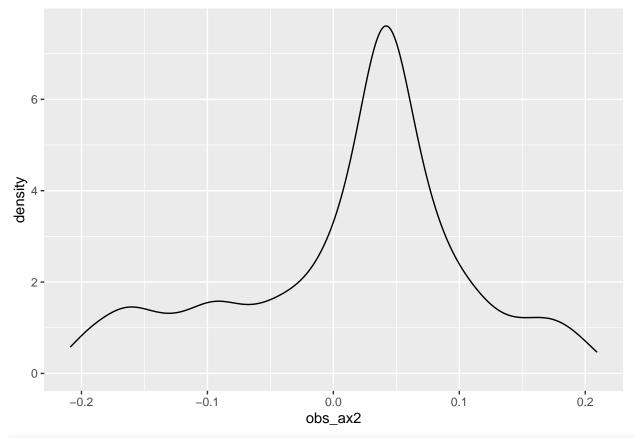
```
obs_ax0
             obs_ax1
                       obs_ax2 obs_ax3
## 0.4842480 0.9286341 0.5504226 0.9950522
Lambda <- fit$loadings</pre>
Psi <- diag(fit$uniquenesses)</pre>
S <- fit$correlation
Sigma <- Lambda %*% t(Lambda) + Psi
# residual matrix. Numbers close to 0 indicate that our factor model is a good representation of the un
round(S - Sigma, 6)
             obs ax0
                     obs_ax1
                                obs_ax2
                                          obs ax3
## obs_ax0 0.000000 0.035391 -0.295516 0.004840
## obs_ax1 0.035391 0.000000 0.105078 -0.000630
## obs_ax2 -0.295516  0.105078  0.000000  0.005113
## obs_ax3 0.004840 -0.000630 0.005113 -0.000052
reg_fit <- factanal(mydata, factors = 1, scores = "regression")</pre>
mean(reg_fit$scores)
## [1] -9.26356e-18
sd(reg_fit$scores)
## [1] 0.9976737
reg_fit$loadings
##
## Loadings:
           Factor1
## obs_ax0 -0.696
## obs_ax1 -0.964
## obs_ax2 0.742
## obs_ax3 0.998
##
##
                  Factor1
## SS loadings
                    2.958
## Proportion Var
                    0.740
ggplot(states, aes(obs_ax0)) + geom_density()
```



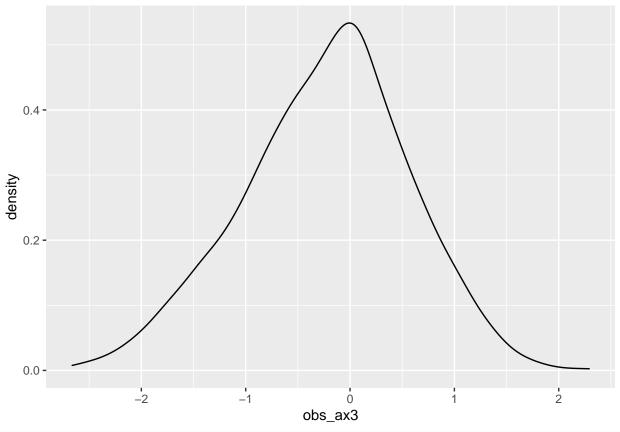
ggplot(states, aes(obs\_ax1)) + geom\_density()



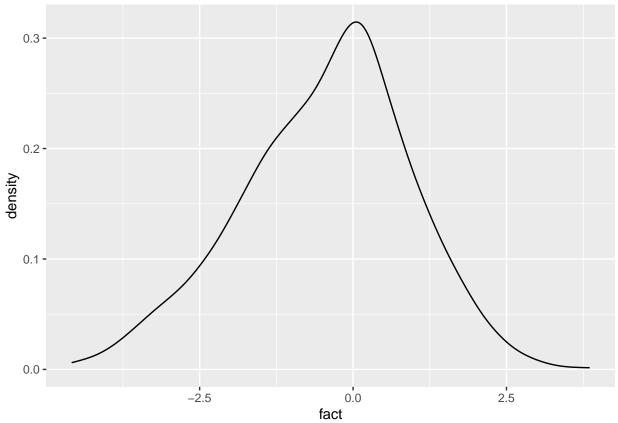
ggplot(states, aes(obs\_ax2)) + geom\_density()



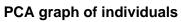
ggplot(states, aes(obs\_ax3)) + geom\_density()

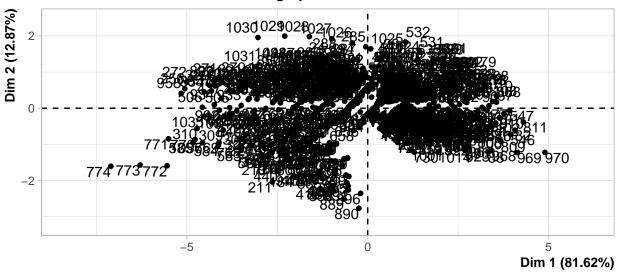


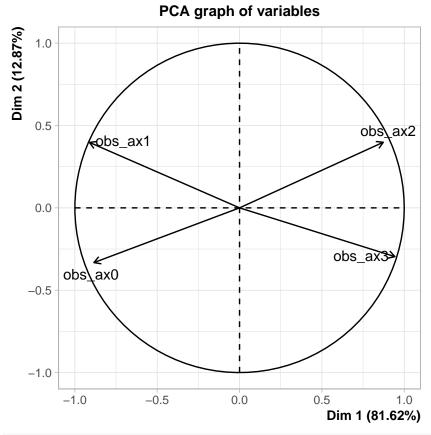
```
data_factor = data.frame(as.matrix(mydata) %*% matrix(fit$loadings))
names(data_factor) = c("fact")
ggplot(data_factor, aes(fact)) + geom_density()
```



# PCA Variable Factor Map
# NOTE: scaling has no effect on fit
library(FactoMineR)
result <- PCA(mydata) # graphs generated automatically</pre>







result <- PCA(states) # graphs generated automatically</pre>

