

## Contents

- compute the extended knot vector
- compute coefficient vector for spline that approximates  $u$
- print extended knot vector and coefficient vector
- compute errors
- plot  $s$

```
% Nikhil Jayswal
% MATH 3890
% Machine Problem 5
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clc; clear; close all

% interval limits
a = 0;
b = 1;

% u'' + pu' + qu = f
p = @(x) exp(x);
q = @(x) sin(x.*x);

u = @(x) cos(x) + sin(3*x);
ux = @(x) -sin(x) + 3*cos(3*x);
uxx = @(x) -cos(x) - 9*sin(3*x);

f = @(x) uxx(x) + p(x).*ux(x) + q(x).*u(x);

% get inputs from user
% d = input('Enter the value of d: ');
% k = input('Enter the value of k: ');
% m = input('Enter the value of m: ');
d = 3;
k = 17;
m = 10;

% knot vector
knots = linspace(a, b, k+2);
```

### compute the extended knot vector

dimension of spline space length of knot vector =  $k+2$   $\rightarrow$  spline consists of  $(k+1)$  pieces  $(k)$  interior points

```
dim = (k+1)*(d+1) - k*d;
```

```

% construct extended knot vector
y = zeros(1, dim+d+1);
% first (d+1) points
y(1:d+1) = knots(1);
% last (d+1) points
y(dim+1:dim+d+1) = knots(end);
% points in between
y(d+2:dim) = knots(2:end-1);

```

**compute coefficient vector for spline that approximates u**

```

ua = u(a); ub = u(b);
c = lsc(d, y, m, p, q, f, ua, ub);

```

**print extended knot vector and coefficient vector**

```

fprintf('The extended knot vector is: \n\n')
disp(y')
fprintf('\n\n')
fprintf('The coefficients are: \n\n')
disp(c)

```

The extended knot vector is:

```

0
0
0
0
0.0556
0.1111
0.1667
0.2222
0.2778
0.3333
0.3889
0.4444
0.5000
0.5556
0.6111
0.6667
0.7222
0.7778
0.8333
0.8889

```

```
0.9444
1.0000
1.0000
1.0000
1.0000
```

The coefficients are:

```
1.0000
20.5501
18.4496
15.4803
12.6866
10.0624
7.6014
5.2972
3.1439
1.1357
-0.7326
-2.4658
-4.0681
-5.5435
-6.8953
-8.1265
-9.2402
-10.2391
-11.1263
-11.6454
0.6814
```

### compute errors

```
t = linspace(a, b, 301);
% evaluate
val = sval2(d, y, c, t);
% print maximum norm of (u-s)
e = u(t)-val;
fprintf('\nThe maximum error is: %f\n', norm(e, inf));
% print RMS error
fprintf('\nThe RMS error is: %f\n', erms(e));
```

The maximum error is: 17.809098

The RMS error is: 9.063477

**plot s**

```
plot(t, val, 'LineWidth', 1);  
hold on  
plot(t, u(t), 'LineWidth', 2);  
xlabel('t')  
legend('Spline s', 'Function u', 'Location', 'best')
```

