

Design and Fabrication of Experiment for Dynamic Analysis of Mechanisms

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for the degree of*

BACHELOR OF TECHNOLOGY

in

MECHANICAL ENGINEERING

by

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December 2019

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We declare that this written submission represents our ideas in our own words and where others' ideas or words have been included, we have adequately cited and referenced the original sources. We also declare that we have adhered to all principles of academic honesty and integrity and have not misrepresented or fabricated or falsified any idea/data/fact/source in our submission. We understand that any violation of the above will be cause for disciplinary action by the Institute and can also evoke penal action from the sources which have thus not been properly cited or from whom proper permission has not been taken when needed.

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This is to certify that the thesis titled **Design and Fabrication of Experiment for Dynamic Analysis of Mechanisms**, submitted by **Aakash** and **A. Akhil**, to the Indian Institute of Technology, Tirupati, for the award of the degree of **Bachelor of Technology**, is a bona fide record of the research work done by them under my supervision. The contents of this thesis, in full or in parts, have not been submitted to any other Institute or University for the award of any degree or diploma.

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ABSTRACT

KEYWORDS: Slider crank mechanism; Four bar mechanism; Six-bar mechanism;
Dynamic analysis; Kinematic analysis; Simulation.

This report explains the detailed process of design and analysis of an experimental setup, which consists of a 3-in-1 mechanism. The setup is designed to perform static, kinematic and dynamic analysis of mechanisms. The design and analysis were performed analytically and numerically by using various commercial software's. The results thus obtained were used to determine the link geometry of the mechanism and in selecting the suitable sensors which in turn will be used for fabrication and instrumentation.

TABLE OF CONTENTS

ACKNOWLEDGEMENTS	i
ABSTRACT	ii
LIST OF FIGURES	v
LIST OF TABLES	vi
ABBREVIATIONS	vii
NOTATION	viii
1 INTRODUCTION	1
1.1 Motivation and objective	1
1.2 Present method(s) and challenges	1
2 ANALYSIS OF MECHANISMS	3
2.1 Kinematic analysis	3
2.1.1 Mathematical formulation	3
2.1.2 GeoGebra modelling	8
2.1.3 Python simulation	8
2.2 Dynamic analysis	10
2.2.1 Mathematical formulation	10
2.2.2 Using commercial software: MathWorks Simscape	13
3 MANUFACTURING	15
3.0.1 Sensor selection	15
3.0.2 Manufacturing plan	15
4 RESULTS	17
5 CONCLUSION AND FUTURE WORK	19

A	CODE LISTING	20
A.1	Six-bar mechanism (Python)	20

LIST OF FIGURES

1.1	CAD model of the mechanism	1
1.2	Three possible configurations of the mechanism: (a) Four bar, (b) Slider crank and (c) Six bar	2
2.1	Slider crank mechanism	4
2.2	Four bar mechanism	5
2.3	Six bar mechanism	6
2.4	Snapshot from GeoGebra showing the mechanism (left) and the velocity profile (right)	8
2.5	Output window from Python for kinematic simulation	9
2.6	Free Body Diagram for Slider Crank Mechanism	10
2.7	Free Body Diagram for four-bar mechanism	12
2.8	Free Body Diagram for six-bar mechanism	13
2.9	CAD model in MATLAB Simscape	13
2.10	Results obtained from Simscape	14
3.1	3D Model of the experiment on (table)	15
3.2	Flowchart showing manufacturing	16
4.1	Slider Velocity	17
4.2	Slider acceleration	18

LIST OF TABLES

2.1	GeoGebra results	9
4.1	Final link lengths	17

ABBREVIATIONS

The following list describes the significance of various abbreviations and acronyms used throughout the report.

KDM	Kinematics and Dynamics of Machinery
PMSM	Permanent Magnet Synchronous Motor
CAD	Computer Aided Design
CSV	Comma Seperated Values
FBD	Free Body Diagram

NOTATION

The following notations are used throughout the report.

$\vec{r}_{A/B}$	Position vector of point A with respect to point B , m
ω_{AB}	Angular velocity of link AB , $\frac{rad}{s}$
$\vec{V}_{A/B}$	Velocity vector of point A with respect to point B , $\frac{m}{s}$
$\vec{a}_{A/B}$	Acceleration vector of point A with respect to point B , $\frac{m}{s^2}$
α_{AB}	Angular acceleration of link AB , $\frac{rad}{s^2}$

CHAPTER 1

INTRODUCTION

1.1 Motivation and objective

The study of the "*Kinematics and Dynamics of Machinery*" (IITT course code: ME2206) lies at the very core of a mechanical engineering background. Although, little has changed in the way the subject is presented, our methodology brings the subject alive and current. We present the design and fabrication of a novel experimental setup for carrying out static, kinematic and dynamic analysis of three different mechanisms in a single setup (Figure 1.1). The mechanism is designed to be configurable to three different types of mechanisms namely - double crank, slider crank and a six bar mechanism depending on the use case as shown in Figure 1.2. The mechanism has retrofitted parts (different link lengths and sliders) to facilitate multiple experiments in the same setup.

The learner gets to "play" with the mechanism parameters and immediately understand their effects. This will enhance one's grasp of the concepts and the development of analytical skills. Hence greatly supplementing and reinforcing the theoretical understanding of the undergraduate students taking the course.

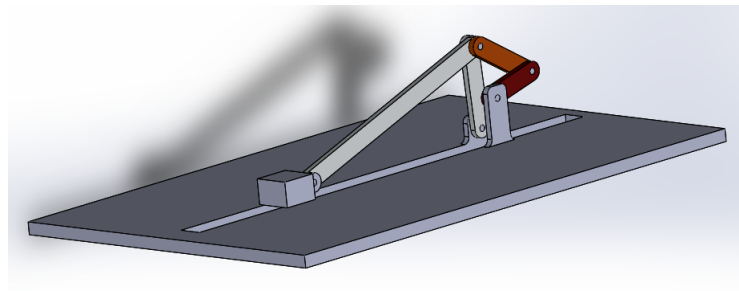


Figure 1.1: CAD model of the mechanism

1.2 Present method(s) and challenges

In the present scenario finding standard mechanisms integrated with different sensor measurement and data acquisition is hard to find. Almost all the mechanisms that are

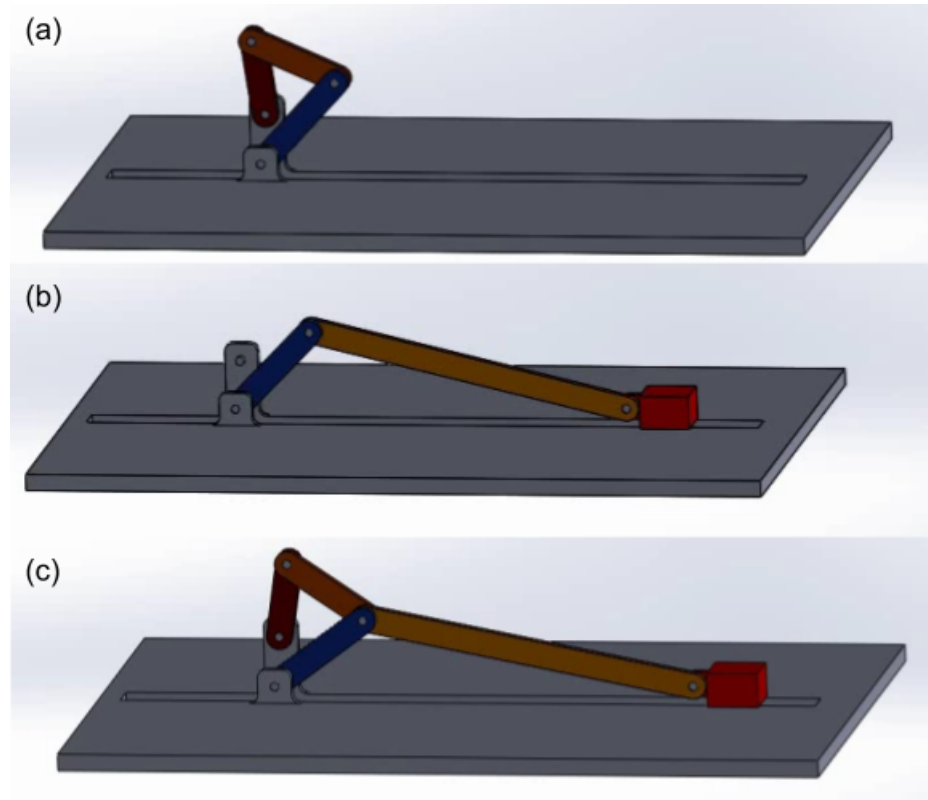


Figure 1.2: Three possible configurations of the mechanism: (a) Four bar, (b) Slider crank and (c) Six bar

available off-the-shelf do not have any data measurement capability and thus can only be used for demonstrations purpose and not as an experimental setup.

In chapter 2 we present thoroughly all the methodologies used in designing and modelling the mechanisms. This includes both the analysis carried out by analytical as well as numerical methods. In the chapter that follows we bring out the various design considerations that has to be taken into account while manufacturing the product. The final two sections present the result(s) and the conclusion(s).

CHAPTER 2

ANALYSIS OF MECHANISMS

2.1 Kinematic analysis

This section presents the methodology employed in order to simulate the kinematics of the various mechanisms. In order to carry out the preliminary analysis of the mechanism, *GeoGebra* an interactive math and geometry software was used. This provided the coarse link lengths required for having the least deviant constant velocity mechanism as shown in Figure 2.4. Once the coarse link lengths were obtained, we developed an in-house Python code that can do iterations on the link lengths so as to minimise any fluctuations in the constant velocity mechanism. The visual output of the Python simulation can be seen in Figure 2.5 while rest of the simulation data is store in a CSV file.

2.1.1 Mathematical formulation

This section brings out the equations of motion associated with the three different mechanisms (Norton, 2011; Uicker *et al.*, 2011). These equations are used to carry out the kinematic and dynamics method theoretically, which then in turn be compared with the numerical solutions obtained by other simulation tools.

Slider crank mechanism

The equations of motion pertaining to the slider crank mechanism (Figure 2.1) are presented in this subsection.

$$\vec{V}_{B/A} = \vec{V}_B - \vec{V}_A \quad (2.1)$$

For link *OA* we have

$$\vec{V}_{A/O} = \vec{\omega}_{AO} \times \vec{r}_{A/O} = \vec{V}_A \quad (2.2)$$

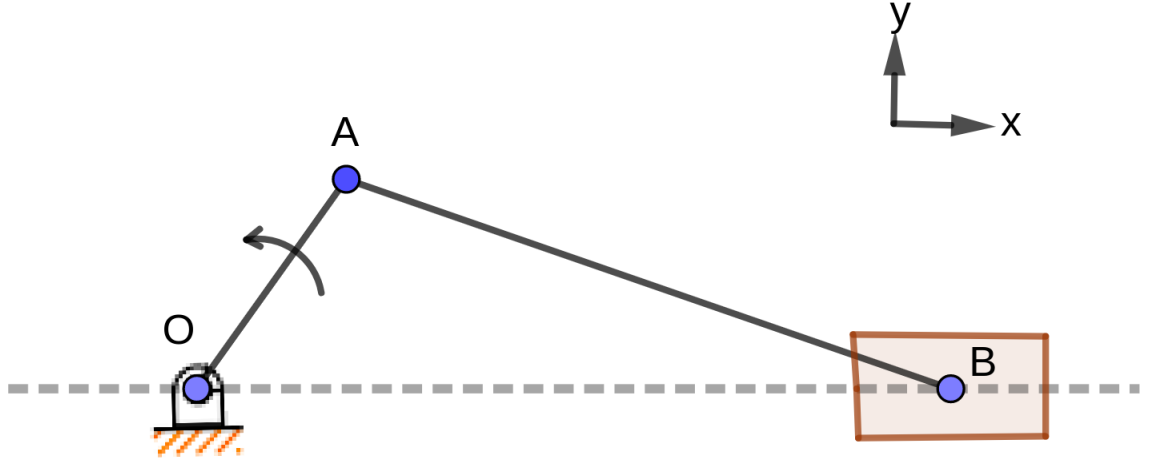


Figure 2.1: Slider crank mechanism

Since 'O' is ground link we have $\vec{V}_O = 0 \implies \vec{V}_{A/O} = \vec{V}_A - \vec{V}_O = \vec{V}_A$. As point B lies on the slider and is moving leftwards it will have velocity along the negative x-direction i.e. $\vec{V}_B = -V_B \hat{i}$; because $\vec{\omega}_{AO} = \omega_{AO} \hat{k}$. For link AB we have

$$\vec{V}_{B/A} = \vec{\omega}_{BA} \times \vec{r}_{B/A} \quad (2.3)$$

Substituting equation 2.3 in equation 2.1 we obtain

$$\vec{\omega}_{BA} \times \vec{r}_{B/A} = \vec{V}_B - \vec{V}_A \quad (2.4)$$

Using equation 2.4 we can find ω_{BA} and V_B . For finding the accelerations we can write

$$\vec{a}_{A/O} = \vec{a}_A = \vec{a}_A^t + \vec{a}_A^n \quad (2.5a)$$

$$\vec{a}_A^t = \alpha_{A/O}^{\rightarrow} \times \vec{r}_{A/O} \quad (2.5b)$$

$$\vec{a}_A^n = \vec{\omega}_{AO} \times \vec{\omega}_{AO} \times \vec{r}_{A/O} \quad (2.5c)$$

where, \vec{a}_A^t and \vec{a}_A^n denote the tangential and normal acceleration of point A. As point B lies on the slider, we have $\vec{a}_B = a_B \hat{i}$.

$$\vec{a}_{B/A} = \vec{a}_{B/A}^t + \vec{a}_{B/A}^n = \vec{a}_B - \vec{a}_A \quad (2.6)$$

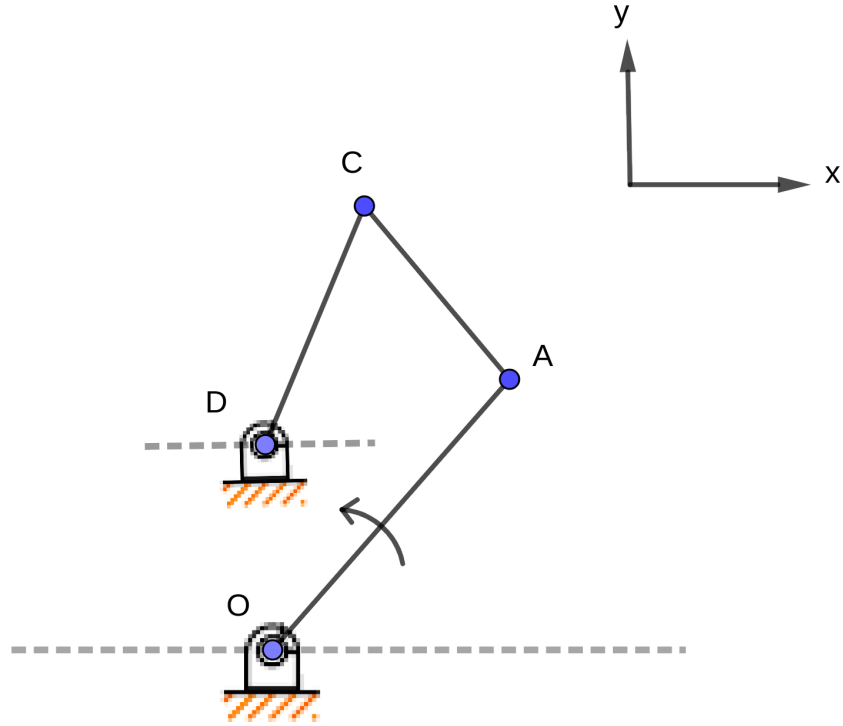


Figure 2.2: Four bar mechanism

Using the above equation we can find α_{BA} and \vec{a}_B .

Four bar mechanism (with four revolute joints)

This subsection lists the mathematical equations pertaining to the four bar mechanism (Figure 2.2).

$$\vec{V}_{A/O} = \vec{\omega}_{AO} \times \vec{r}_{A/O} = \vec{V}_A \quad (2.7a)$$

$$\vec{V}_{C/D} = \vec{\omega}_{CD} \times \vec{r}_{C/D} = \vec{V}_C \quad (2.7b)$$

$$\vec{V}_{A/C} = \vec{\omega}_{AC} \times \vec{r}_{A/C} = \vec{V}_A - \vec{V}_C = \vec{\omega}_{AO} \times \vec{r}_{A/O} - \vec{\omega}_{CD} \times \vec{r}_{C/D} \quad (2.8)$$

Using the above equation we can find ω_{CD} and ω_{AC} .

$$\vec{a}_{A/O} = \vec{a}_A = \vec{a}_A^t + \vec{a}_A^n \quad (2.9a)$$

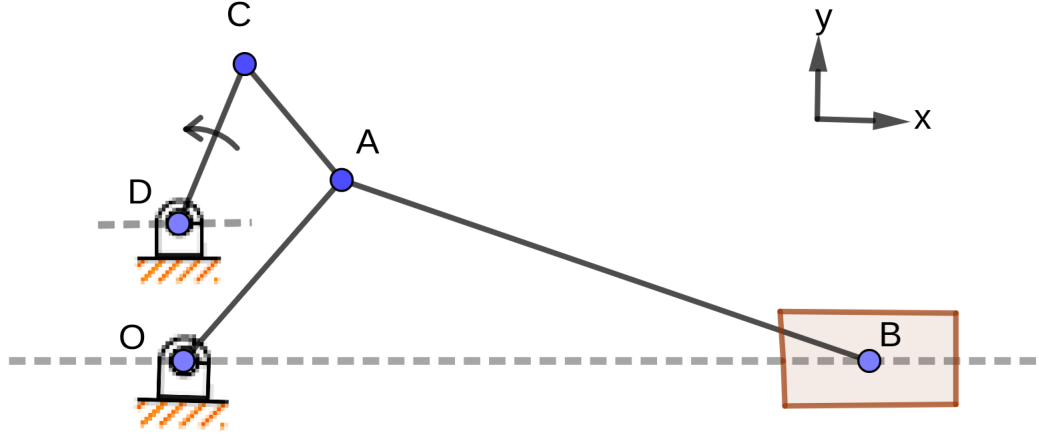


Figure 2.3: Six bar mechanism

$$\vec{a}_{C/D} = \vec{a}_C = \vec{a}_C^t + \vec{a}_C^n \quad (2.9b)$$

$$\vec{a}_{A/C} = \vec{a}_{A/C}^t + \vec{a}_{A/C}^n = \vec{a}_A - \vec{a}_C \quad (2.10)$$

Here $\vec{a}^t = \vec{\alpha} \times \vec{r}$ and $\vec{a}^n = \vec{\omega} \times \vec{\omega} \times \vec{r}$. Using the above equations we can find α_{AC} and α_{CD}

Six bar mechanism

This subsection presents the mathematical equations associated with the six bar mechanism (Figure 2.3).

$$\vec{V}_{C/D} = \vec{\omega}_{CD} \times \vec{r}_{C/D} = \vec{V}_C \quad (2.11)$$

$$\vec{V}_{A/C} = \vec{\omega}_{AC} \times \vec{r}_{A/C} = \vec{V}_A - \vec{V}_C = \vec{\omega}_{AO} \times \vec{r}_{A/O} - \vec{\omega}_{CD} \times \vec{r}_{C/D} \quad (2.12)$$

Using the above equation we can find ω_{OA} and ω_{AC} .

$$\vec{V}_{B/A} = \vec{V}_B - \vec{V}_A \quad (2.13)$$

For link OA we have

$$\vec{V}_{A/O} = \vec{\omega}_{AO} \times \vec{r}_{A/O} = \vec{V}_A \quad (2.14)$$

Since 'O' is ground link we have $\vec{V}_O = 0 \implies \vec{V}_{A/O} = \vec{V}_A - \vec{V}_O = \vec{V}_A$. As point B lies on the slider and is moving leftwards it will have velocity along the negative x-direction i.e. $\vec{V}_B = -V_B \hat{i}$; because $\vec{\omega}_{AO} = \omega_{AO} \hat{k}$. For link AB we have

$$\vec{V}_{B/A} = \vec{\omega}_{BA} \times \vec{r}_{B/A} \quad (2.15)$$

Substituting equation 2.15 in equation 2.13 we obtain

$$\vec{\omega}_{BA} \times \vec{r}_{B/A} = \vec{V}_B - \vec{V}_A \quad (2.16)$$

Using equation 2.16 we can find ω_{BA} and V_B .

For finding the accelerations we can write

$$\vec{a}_{C/D} = \vec{a}_C = \vec{a}_C^t + \vec{a}_C^n \quad (2.17)$$

$$\vec{a}_{A/C} = \vec{a}_{A/C}^t + \vec{a}_{A/C}^n = \vec{a}_A - \vec{a}_C \quad (2.18)$$

Here $\vec{a}^t = \vec{\alpha} \times \vec{r}$ and $\vec{a}^n = \vec{\omega} \times \vec{\omega} \times \vec{r}$. Using the above equations we can find α_{AC} and α_{OA}

$$\vec{a}_{A/O} = \vec{a}_A = \vec{a}_A^t + \vec{a}_A^n \quad (2.19a)$$

$$\vec{a}_A^t = \alpha_{A/O} \vec{r}_{A/O} \quad (2.19b)$$

$$\vec{a}_A^n = \omega_{AO} \vec{\omega}_{AO} \times \vec{r}_{A/O} \quad (2.19c)$$

where, \vec{a}_A^t and \vec{a}_A^n denote the tangential and normal acceleration of point A. As point B lies on the slider, we have $\vec{a}_B = a_B \hat{i}$.

$$\vec{a}_{B/A} = \vec{a}_{B/A}^t + \vec{a}_{B/A}^n = \vec{a}_B - \vec{a}_A \quad (2.20)$$

Using the above equation we can find α_{BA} and \vec{a}_B .

2.1.2 GeoGebra modelling

This subsection provides an insight into the preliminary analysis done by using off-the-shelf software - GeoGebra for determining initial link lengths (Hohenwarter *et al.*, 2013). First the mechanism was created inside GeoGebra geometry with sliders for varying the link lengths manually. Later the slider velocity was plotted by using graphical analysis of the mechanism inside GeoGebra itself (as shown in Figure 2.4). In order to find the required link lengths yielding constant velocity mechanism, each of the link lengths were varied to get the constant velocity mechanism with least variation while keeping the others fixed. The manual iterations are shown in Table 2.1.

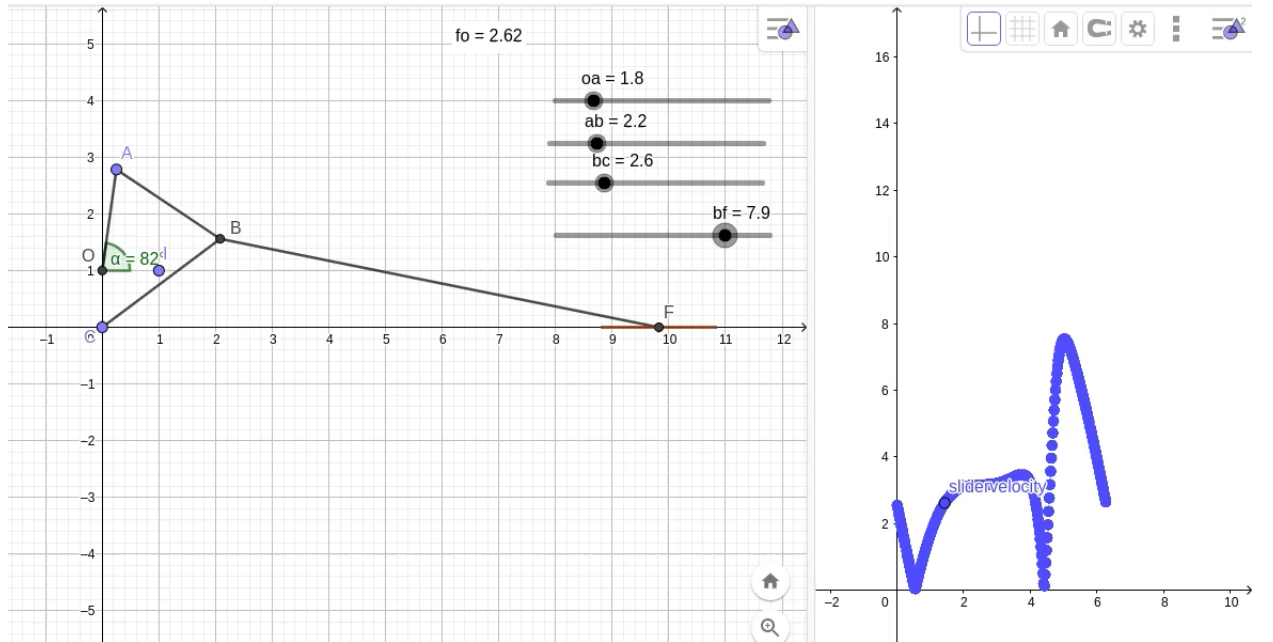


Figure 2.4: Snapshot from GeoGebra showing the mechanism (left) and the velocity profile (right)

2.1.3 Python simulation

This section deals with further refining the preliminary links lengths which were obtained from GeoGebra modelling. The initial lengths are fed to an in-house Python script (see appendix) to get optimum link lengths for nearly constant slider velocity (Python Core Team, 2018). The algorithm performs the iterations by varying each of the link by step size of $0.1 \times \text{unit length}$. It also stores the peak to valley distance for each of the obtained velocity profiles which can be used to select the link lengths giving minimum velocity variation for the constant velocity range. Figure 2.5 shows the mechanism animation as

OC	OA	AB	BC	BF	Mean slider velocity	Peak to valley of slider velocity	ω of crank
1	2	1.6	2	6	2.25	0.5	2
1	2	1.4	2	6	2.28	0.81	2
1	2	1.2	2	6	2.37	1.24	2
1	2	2	2	6	2.385	0.77	2
1	2.2	1.6	2	6	2.31	0.83	2
1	1.8	1.6	2	6	2.375	0.75	2
1	2	1.6	2.2	6	2.545	0.37	2
1	2	1.6	1.8	6	1.92	0.76	2
1	2	1.6	2.4	6	2.87	0.26	2
1	2	1.6	2.6	6	3.2	0.25	2
1	2	1.6	2.8	6	3.52	0.36	2
1	2	1.6	2.6	7	3.135	0.15	2
1	2	1.6	2.6	7.5	3.2	0.12	2
1	2	1.6	2.6	8	3.24	0.09	2

All lengths are in *units*, velocity are in *units/s*, angular velocity ω is in *rad/s*.

Table 2.1: GeoGebra results

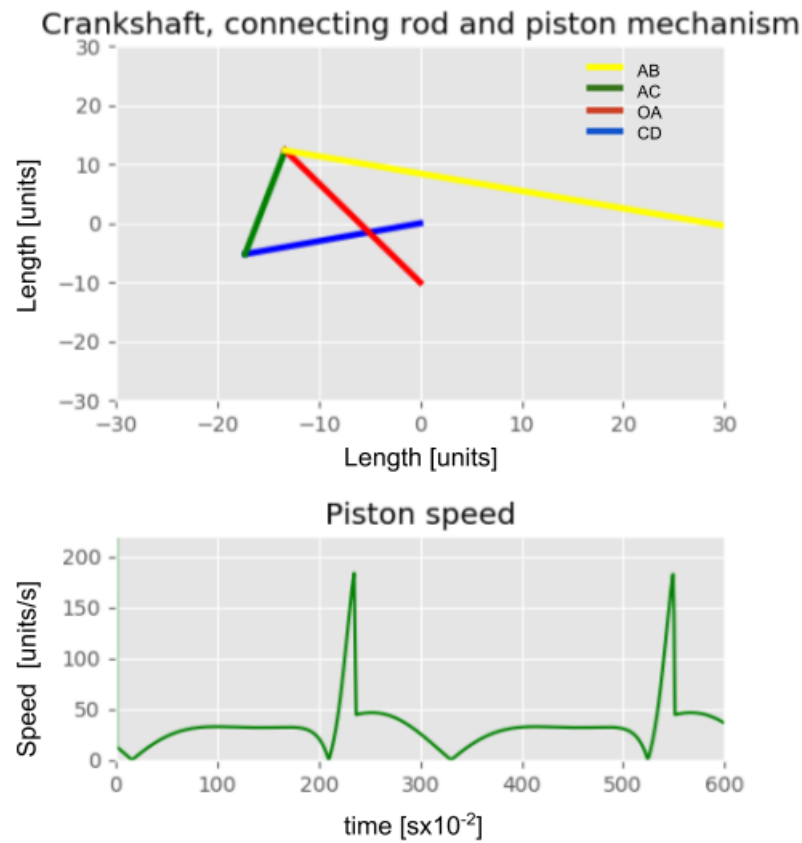


Figure 2.5: Output window from Python for kinematic simulation

well as the velocity plot having a near constant velocity for an interval.

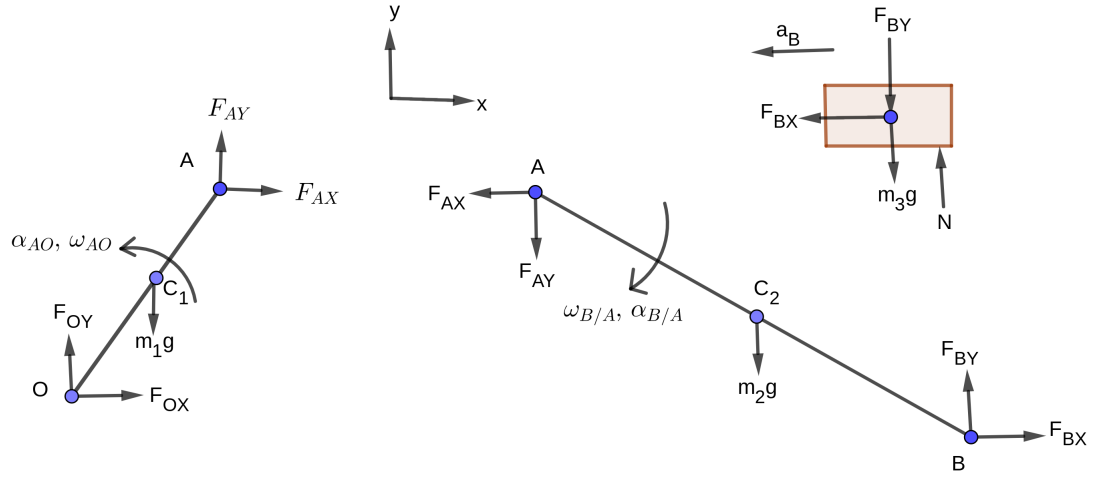


Figure 2.6: Free Body Diagram for Slider Crank Mechanism

2.2 Dynamic analysis

For performing the dynamic analysis of the mechanism we used MathWorks Simscape Mechanical package. A 3D model was created in the package itself and analysed the same for various forces, torques, acceleration and velocities by taking the material as aluminium (Figure 2.9, ??). This analysis is necessary in order to ease the process of selection of actuator, material and the sensor system.

2.2.1 Mathematical formulation

This subsection brings out the mathematical equations for performing dynamic analysis of all the three possible mechanism (Ghosh and Mallik, 2002).

Slider crank mechanism

Force and Torque balance for link OA using Figure 2.6

$$F_{OX} + F_{AX} = 0 \quad (2.21a)$$

$$F_{OY} + F_{AY} = m_1 g \quad (2.21b)$$

$$I_{AO}\vec{\alpha}_{AO} = \vec{r}_{C_1O} \times m_1g(-\hat{j}) + \vec{r}_{A/O} \times \vec{F}_A \quad (2.21c)$$

where, $\vec{F}_A = \vec{F}_{AX}\hat{i} + \vec{F}_{AY}\hat{j}$. Similarly for link AB we have

$$F_{AX} = F_{BX} \quad (2.22a)$$

$$F_{BY} = F_{AY} + m_2g \quad (2.22b)$$

$$I_{BA}\vec{\alpha}_{B/A} = \vec{r}_{C_2/A} \times m_2g(-\hat{j}) + \vec{r}_{B/A} \times \vec{F}_B \quad (2.22c)$$

where, $\vec{F}_B = \vec{F}_{BX}\hat{i} + \vec{F}_{BY}\hat{j}$.

Force balance for the slider

$$F_{BY} + m_3g = N \quad (2.23a)$$

$$m_3a_B = F_{BX} \quad (2.23b)$$

Four bar mechanism (with four revolute joints)

Force and Torque balance for link OA using Figure 2.7

$$\sum \vec{F}_X = 0 \quad (2.24a)$$

$$\sum \vec{F}_Y = 0 \quad (2.24b)$$

$$\sum \vec{T} = I_1 \vec{\alpha}_{AO} \quad (2.24c)$$

Force and Torque balance for link AC using Figure 2.7

$$\sum \vec{F}_X = 0 \quad (2.25a)$$

$$\sum \vec{F}_Y = 0 \quad (2.25b)$$

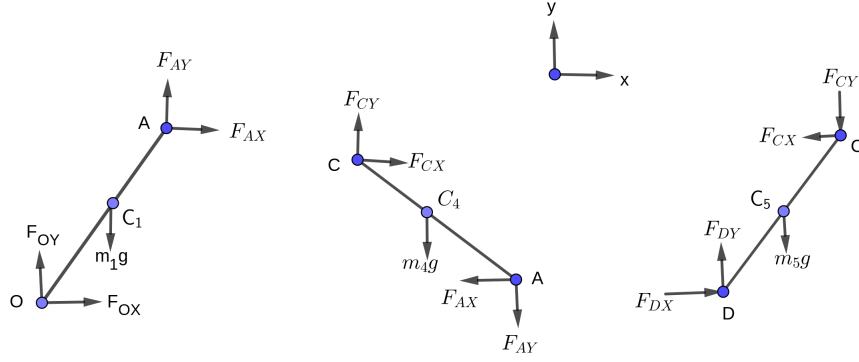


Figure 2.7: Free Body Diagram for four-bar mechanism

$$\sum \vec{T} = I_4 \vec{\alpha}_{AC} \quad (2.25c)$$

Force and Torque balance for link CD using Figure 2.7

$$\sum \vec{F}_X = 0 \quad (2.26a)$$

$$\sum \vec{F}_Y = 0 \quad (2.26b)$$

$$\sum \vec{T} = I_5 \vec{\alpha}_{CD} \quad (2.26c)$$

Six bar mechanism

Force and Torque balance for all links using Figure 2.8

$$\sum \vec{F}_X = 0, \sum \vec{F}_Y = 0, \sum \vec{T} = I \vec{\alpha} \quad (2.27)$$

$$F_{A_1X} + F_{A_2X} + F_{A_4X} = 0 \quad (2.28a)$$

$$F_{A_1Y} + F_{A_2Y} + F_{A_4Y} = 0 \quad (2.28b)$$

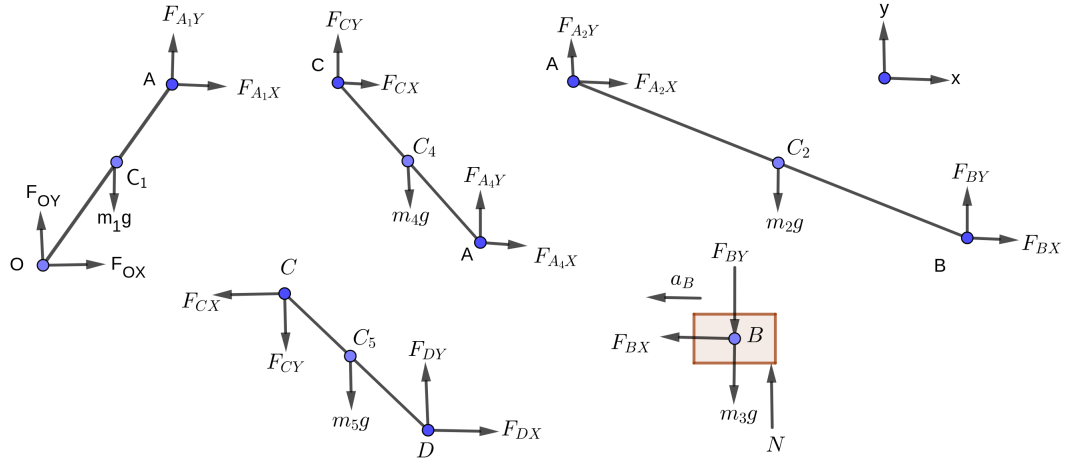


Figure 2.8: Free Body Diagram for six-bar mechanism

Force balance for Slider using Figure 2.8

$$F_{BY} + m_3g = N \quad (2.29a)$$

$$m_3a_B = F_{BX} \quad (2.29b)$$

2.2.2 Using commercial software: MathWorks Simscape

This sections deals with the dynamic analysis of the mechanism using Mathworks Simscape. A MathWorks Simscape model (Figure 2.9) was created based on the link lengths that were obtained from the kinematic analysis. The link width is taken as 3cm and link thickness as 1cm while taking aluminum as material for all links and slider. (MAT, 2017)

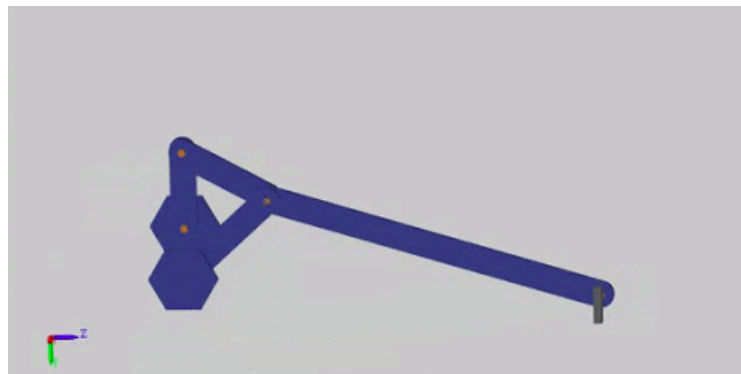
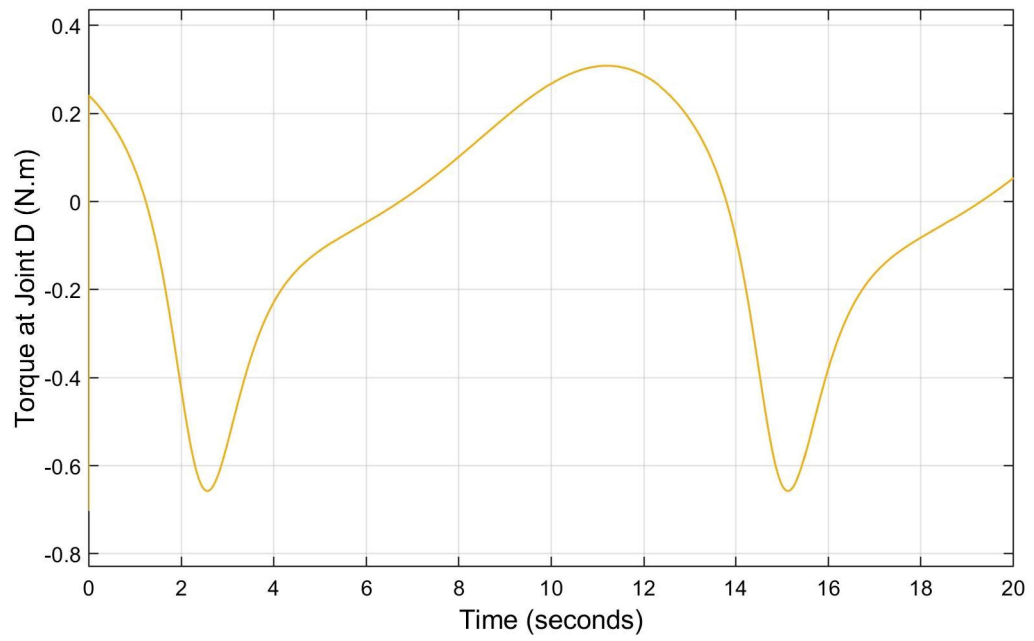
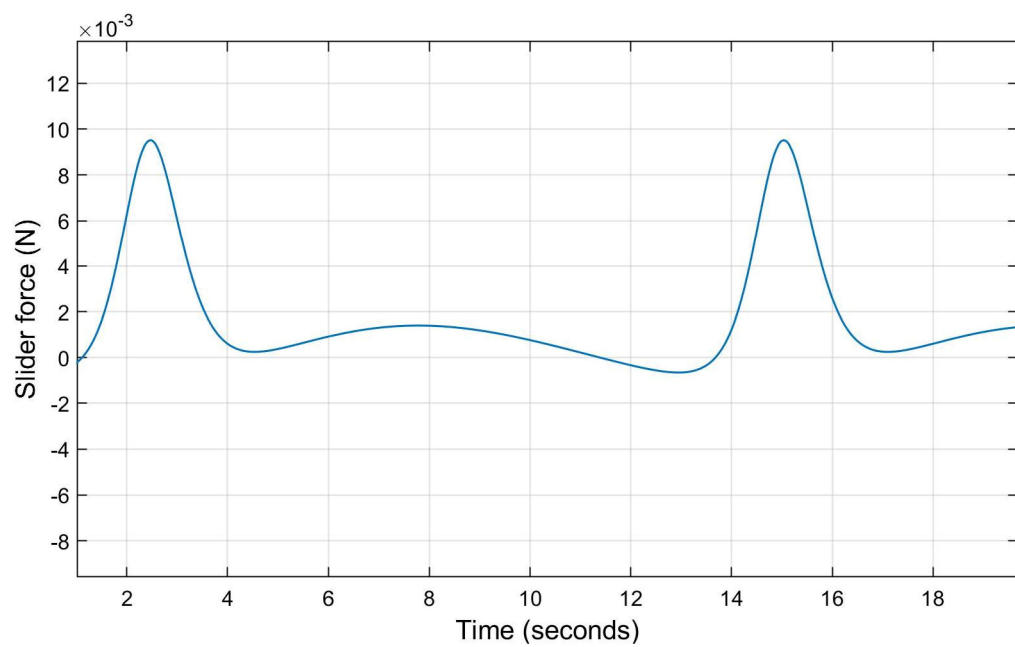


Figure 2.9: CAD model in MATLAB Simscape



(a) Input torque



(b) Slider force

Figure 2.10: Results obtained from Simscape

CHAPTER 3

MANUFACTURING

3.0.1 Sensor selection

Based on the results of Kinematic, Dynamic analysis using MathWorks Simscape, We selected 2-Phase Incremental Optical Rotary Encoder to detect angular velocity and angular acceleration of links, 3-Axis Accelerometer is to detect linear acceleration and linear velocity of slider.

2-Phase Incremental Optical Rotary Encoder has 600 Pulse Per Revolution (PPR).

3-Axis Accelerometer has range of $-16g$ to $16g$, with a sampling rate of 8kHz.

3.0.2 Manufacturing plan

This section focuses on the materials and fabrication processes that will be used for carrying out the manufacturing in the second phase of the project. Figure 3.2 gives complete insight on the various stages involved in manufacturing the experiment design.

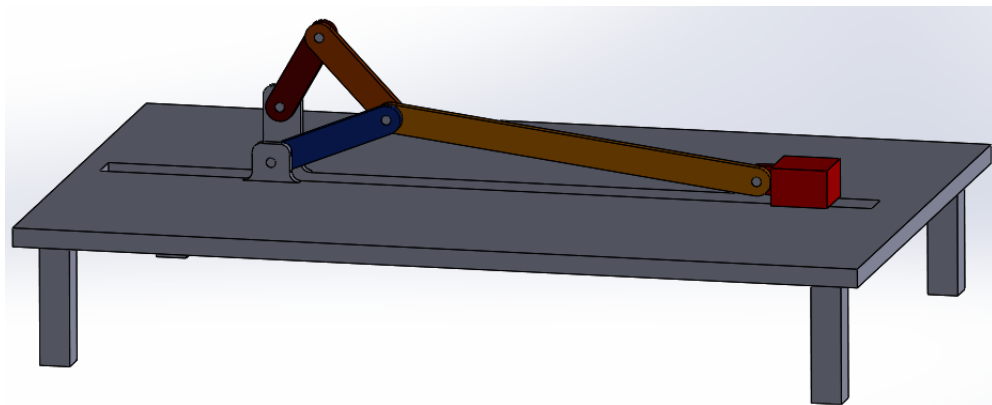


Figure 3.1: 3D Model of the experiment on (table)

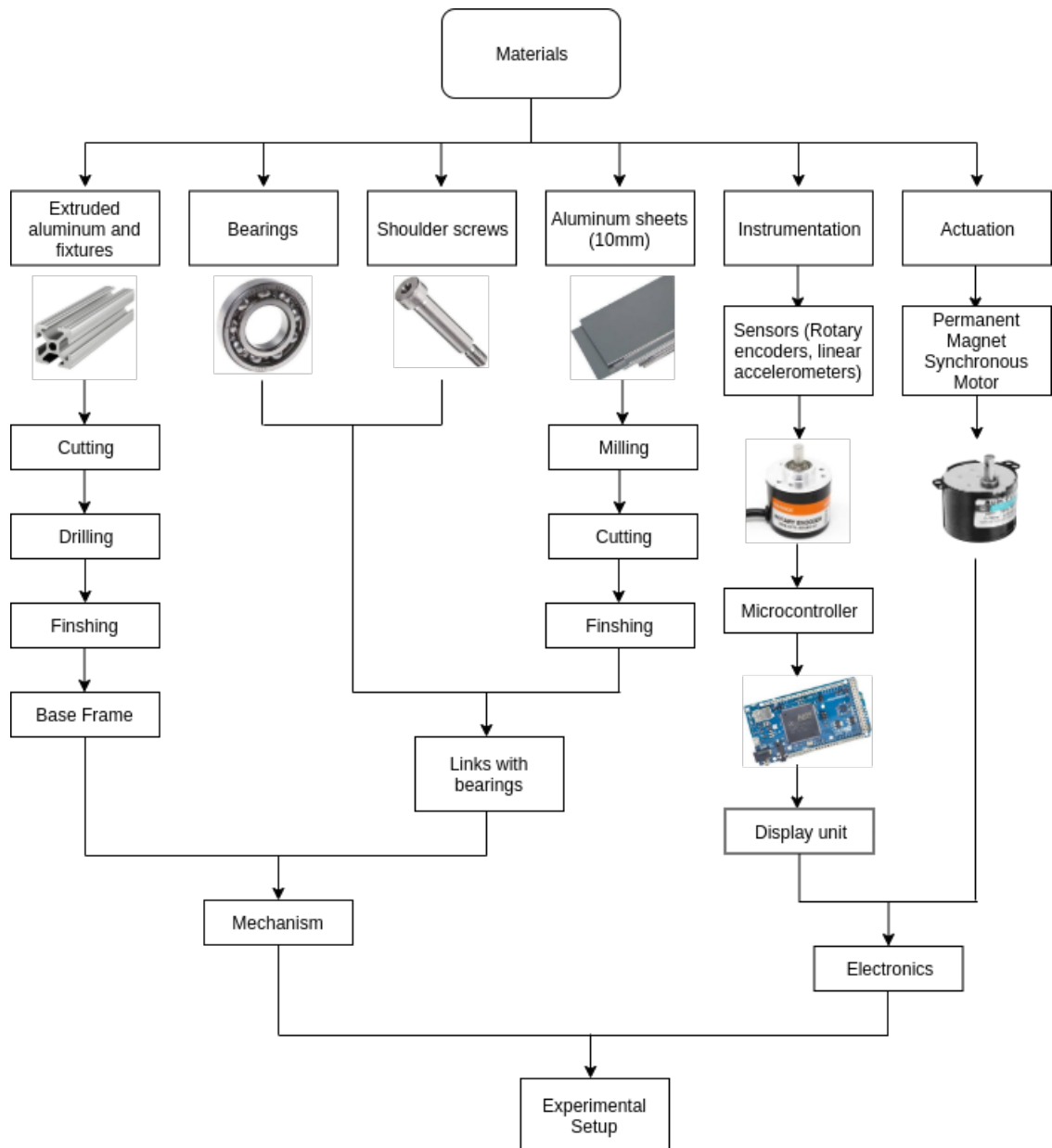


Figure 3.2: Flowchart showing manufacturing

CHAPTER 4

RESULTS

This final section presents obtained results. By utilizing the kinematic analysis we obtained the link lengths resulting in constant velocity mechanism as:

Link	Link length (cm)
OA	13
CD	9
AC	11
AB	39.5
DO	5

Table 4.1: Final link lengths

Furthermore plots for slider velocity and acceleration were obtained using Simscape.

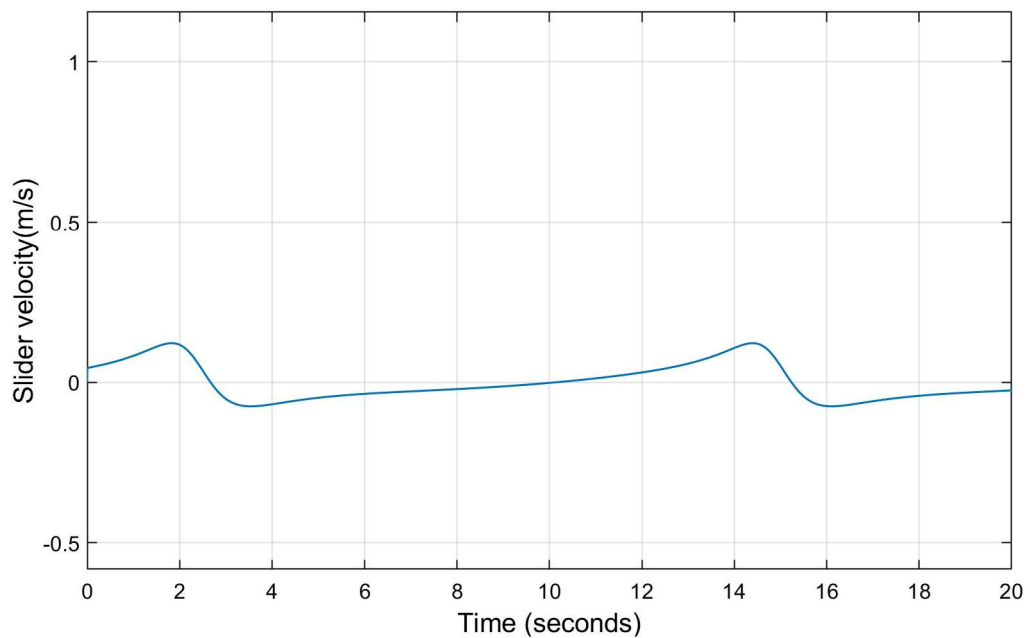


Figure 4.1: Slider Velocity

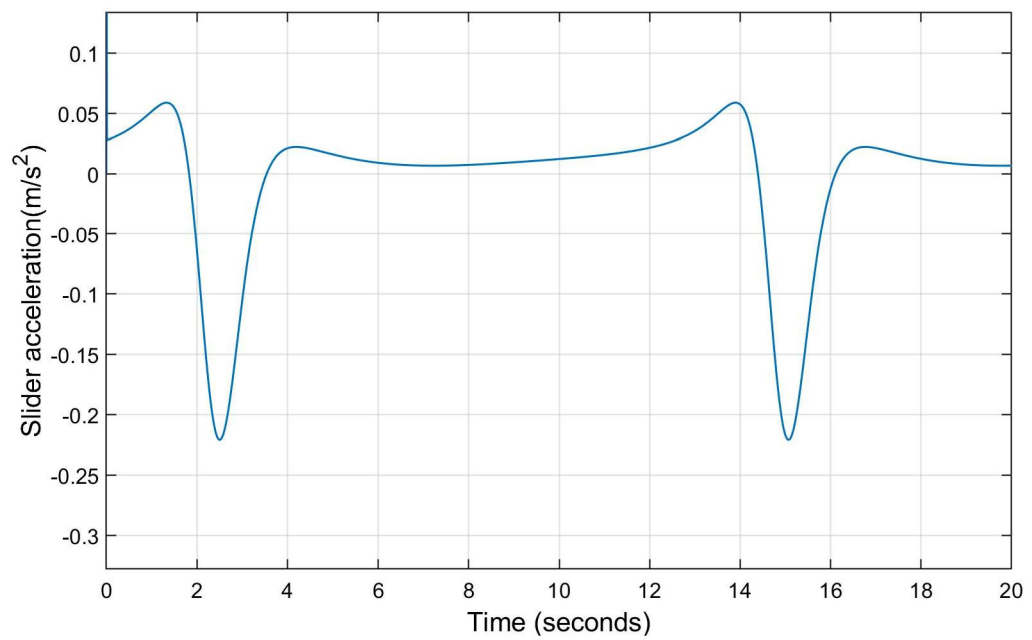


Figure 4.2: Slider acceleration

CHAPTER 5

CONCLUSION AND FUTURE WORK

The complete analysis of the mechanism(s) was performed using applicable method and software. 3D CAD model of the mechanism was created to facilitate better visualisation. Various design considerations were addressed and manufacturing workflow and plan were accomplished as a prerequisite to manufacturing. Also, the BoM was prepared and materials acquisition from the vendor is in process.

In the near future we shall start the manufacturing process based on the work that has been already accomplished by now. After completing the manufacturing rigorous testing will be done on the mechanism and corrections be made accordingly. In the end we will work on preparing the documentation for the product.

APPENDIX A

CODE LISTING

The code used for carrying out this work is presented here. Due due to the high volume of the code involved in this project, it is also hosted on GitHub for clarity at <https://github.com/AakashSYadav/BTP> with complete documentation.

A.1 Six-bar mechanism (Python)

```
1 # http://firsttimeprogrammer.blogspot.com/2015/02/crankshaft-
   connecting-rod-and-piston.html
2
3 # import matplotlib.animation as animation
4 # import matplotlib.pyplot as plt
5 # from sympy import symbols, Eq, solve
6 import numpy as np
7 import time
8 import math
9 import csv
10
11 # plt.style.use('ggplot')
12 link_a_pivot = (0,-10)
13 link_p_pivot = (0,0)
14 # x, y, h = symbols('x y h')
15
16 class My_mechanism(object):
17
18     # The init function
19     def __init__(self,a,b,p,q,omega):
20         self.a = a                # Rod a
21         self.b = b                # Rod b
22         self.p = p                # Rod p
23         self.q = q                # Rod q
24         self.omega = omega        # Angular speed of rod a in rad
                                   /s
```

```

25         self.theta0 = 0                # Initial angular position of
rod a theta()
26         self.set0 = (0,-100)           # for selecting one of the two
solutions
27         self.k = 0.00001                # Initial time for animation
28         self.c_position = []             # Piston position for animation
29         self.c_speed = []                # storing piston speed
30         self.c_time = []                 # storing the time intervals
31         self.pos_old = 0 # old position of the piston for c_dot
calculation
32
33     # Angular position of rod a as a function of time
34     def theta(self,t):
35         # if not all(t):
36         #     raise ValueError('Each time t must be greater than 0')
37         theta = self.theta0 + self.omega*t
38         return theta
39
40     def rod_p_position(self,t):
41         p_y = self.p*np.sin(self.theta(t))
42         p_x = self.p*np.cos(self.theta(t))
43         return p_x,p_y
44
45     def rod_q_position(self,t):
46         px,py = self.rod_p_position(t)
47         ax,ay = link_a_pivot
48         c = ((self.p**2-px**2-py**2) - (self.a**2-ax**2-ay**2)) /
(2*(ax-px))
49         d = (py-ay)/(ax-px)
50         D = (d*(px-c)+py)**2 - (1+d**2)*(py**2 + (px-c)**2 - self.p
**2)
51         if D<0:
52             print("complex")
53             raise Exception('complex')
54         D2 = D**0.5
55         y0 = (d*(px-c)+py+D2)/(1+d**2)
56         y1 = (d*(px-c)+py-D2)/(1+d**2)
57         x0 = c+d*y0
58         x1 = c+d*y1
59         set1=(x0,y0)

```



```

60         set2=(x1,y1)
61         # print(set1,set2)
62
63         dist1 = math.hypot(set1[0] - self.set0[0], set1[1] - self.
set0[1])
64         dist2 = math.hypot(set2[0] - self.set0[0], set2[1] - self.
set0[1])
65         if dist1<dist2:
66             self.set0=set1
67             return set1[0],set1[1]
68         else:
69             self.set0=set2
70             return set2[0],set2[1]
71
72     def piston_position(self,t):
73         q_x,q_y = self.rod_q_position(t)
74         h0 = q_x+(self.b**2 - (q_y-link_a_pivot[1])**2)**0.5
75         return h0
76
77     # Piston speed
78     def c_dot(self,t):
79         c_x = self.piston_position(t)
80         # c_dot = (c_x-self.pos_old)/0.05
81         c_dot = abs(c_x-self.pos_old)/0.01 # dt = 0.01
82         self.pos_old = c_x
83         return c_dot
84
85     def velocity_params(self):
86         while self.k<3.5: # to get one complete cycle
87             speed = self.c_dot(self.k)
88             self.k+=0.01
89
90         """
91         Uncomment the below 3 lines and comment the rest
92         to collect data for a single set of params using "c_out_2.
py"
93
94         """
95         # with open('oneP_best2.csv', mode='a') as label_file:
96         #     label_writer = csv.writer(label_file, delimiter=',',
quotechar='"', quoting=csv.QUOTE_MINIMAL)

```

```

96         # label_writer.writerow([self.k,speed])
97
98         if self.k>0.4 and self.k<2.1:# store the ROI
99             self.c_speed.append(speed)
100             self.c_time.append(self.k)
101
102         # print(self.c_speed)
103         maxi = []
104         mini = []
105         for i in range(1,len(self.c_speed)-1):
106             # local maxima
107             if self.c_speed[i]>self.c_speed[i+1] and self.c_speed[i]>
self.c_speed[i-1]:
108                 maxi.append(self.c_speed[i])
109                 # print("max",self.c_speed[i])
110             # local minima
111             if self.c_speed[i]<self.c_speed[i+1] and self.c_speed[i]<
self.c_speed[i-1]:
112                 mini.append(self.c_speed[i])
113                 # print("min",self.c_speed[i])
114             # print(self.a,self.b,self.p,self.q,max(maxi),min(mini))
115             with open('data_best.csv', mode='a') as label_file:
116                 label_writer = csv.writer(label_file, delimiter=',',
quotechar='"', quoting=csv.QUOTE_MINIMAL)
117                 label_writer.writerow([self.a,self.b,self.p,self.q,max(
maxi),min(mini)])
118             mini.clear()
119             maxi.clear()
120             self.c_speed.clear()
121             self.time.clear()

```

```

1 from crankshaft import *
2 import time
3
4 initial_time = time.time()
5 # #a,b,p,q,omega
6 # best
7 for a in range(20,35):
8     for b in range(70,80):
9         for p in range(15,25):

```

```
10         for q in range(15,30):
11             m = My_mechanism(a,b,p,q,2)
12             try:
13                 m.velocity_params()
14             except Exception:
15                 continue
16
17 print("Processing time : ",time.time()-initial_time,"s")
```

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