# DAA432C Assignment-05

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#### PROBLEM STATEMENT

Given an NxN chessboard and a Knight at position (x,y). The Knight has to take exactly K steps, where at each step it chooses any of the 8 directions uniformly at random. What is the probability that the Knight remains in the chessboard after taking K steps, with the condition that it can't enter the board again once it leaves it? Solve using Dynamic programming.

#### **ALGORITHM**

1. Define direction vectors for the knight.

```
Ex:- dx[] = \{1, 2, 2, 1, -1, -2, -2, -1\}

dy[] = \{2, 1, -1, -1, -2, -1, 1, 2\}
```

- 2. Take an array dp[N, N, steps + 1] which will store the probability of reaching (x,y) after (steps) number of moves,
- 3. Base case: if the number of steps is 0, then the probability that the Knight will remain inside the board is 1
- 4. Take the position (x, y) after s number of steps.
- 5. Take prob = 0.0 then check for each positions reachable from (x, y) using the direction vectors and store it in new position (nx, ny).
- 6. Check if this new position (nx, ny) is inside of the chessboard, if yes then add dp1[nx][ny][s 1] / 8.0 to prob.
- 7. Store the prob in dp[x][y][s].
- 8. Keep repeating for the given number of steps.
- 9. The required probability will be stored in dp[start\_x][start\_y][k], where (start\_x, start\_y) are the given initial position of the knight and k is the number of steps.

#### PSEUDO CODE

```
int dx[] = {1, 2, 2, 1, -1, -2, -2, -1};
int dy[] = {2, 1, -1, -2, -2, -1, 1, 2};

bool inside(int x, int y)
{
    return (x >= 0 and x < N and y >= 0
and y < N);
}</pre>
```

```
double dp[N][N][steps + 1];
            double prob = 0.0;
               int nx = x + dx[i];
return dp[start_x][start_y][steps];
```

## Time and Space Complexity

Time Complexity: O(NxNxK), where N is the size of the board and K is the number of steps.

As, there are 3 nested loops 2 of them runs for N number of times and one For K number of times.

Space Complexity: O(NxNxK), where N is the size of the board and K is the number of steps. As, we are using dp[N][N][K] array of size NxNxK.

### Result

Enter the size of chessboard 8
Enter the number of steps 3
Enter the space-separated position of knight 0 0 0.125