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MODULE *Zarb*

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EXTENDS *Integers, Sequences, FiniteSets, TLC*

CONSTANT

The total number of faulty nodes

*NumFaulty*,

*MaxRound*

$NumValidators \triangleq (3 * NumFaulty) + 1$

$QuorumCnt \triangleq (2 * NumFaulty) + 1$

$OneThird \triangleq NumFaulty + 1$

ASSUME

$\wedge NumFaulty \geq 1$

VARIABLES

*log*,

*states*

$vars \triangleq \langle states, log \rangle$

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Helper functions

Fetch a subset of messages in the network based on the *params* filter.

$SubsetOfMsgs(params) \triangleq$

$\{msg \in log : \forall field \in DOMAIN\ params : msg[field] = params[field]\}$

In *Zarb* *isProposer* is chosen based on the time a validator was joined the network  
here we assume the validators joined sequentially

$IsProposer(index) \triangleq$

$(states[index].round + states[index].proposerIndex) \% NumValidators = index$

$HasPrepareQuorum(index) \triangleq$

$Cardinality(SubsetOfMsgs([$

$type \mapsto "PREPARE",$

$height \mapsto states[index].height,$

$round \mapsto states[index].round])) \geq QuorumCnt$

$HasPrecommitQuorum(index) \triangleq$

$Cardinality(SubsetOfMsgs([$

$type \mapsto "PRECOMMIT",$

$height \mapsto states[index].height,$

$round \mapsto states[index].round])) \geq QuorumCnt$

$HasChangeProposerQuorum(index) \triangleq$

$Cardinality(SubsetOfMsgs([$   
 $type \mapsto \text{"CHANGE-PROPOSER"},$   
 $height \mapsto states[index].height,$   
 $round \mapsto states[index].round])) \geq QuorumCnt$

$HasOneThirdOfChangeProposer(index) \triangleq$   
 $Cardinality(SubsetOfMsgs([$   
 $type \mapsto \text{"CHANGE-PROPOSER"},$   
 $height \mapsto states[index].height,$   
 $round \mapsto states[index].round])) \geq OneThird$

$GetProposal(height, round) \triangleq$   
 $SubsetOfMsgs([type \mapsto \text{"PROPOSAL"}, height \mapsto height, round \mapsto round])$

$HasProposal(height, round) \triangleq$   
 $Cardinality(GetProposal(height, round)) > 0$

$IsCommitted(height) \triangleq$   
 $Cardinality(SubsetOfMsgs([type \mapsto \text{"BLOCK-ANNOUNCE"}, height \mapsto height])) > 0$

$SendProposal$  is used to broadcast proposal into the network

$SendProposal(index) \triangleq$   
 $log' = log \cup \{[$   
 $type \mapsto \text{"PROPOSAL"},$   
 $height \mapsto states[index].height,$   
 $round \mapsto states[index].round,$   
 $index \mapsto index$   
 $]\}$

$SendPrepareVote(index) \triangleq$   
 $log' = log \cup \{[$   
 $type \mapsto \text{"PREPARE"},$   
 $height \mapsto states[index].height,$   
 $round \mapsto states[index].round,$   
 $index \mapsto index$   
 $]\}$

$SendPrecommitVote(index) \triangleq$   
 $log' = log \cup \{[$   
 $type \mapsto \text{"PRECOMMIT"},$   
 $height \mapsto states[index].height,$   
 $round \mapsto states[index].round,$   
 $index \mapsto index$   
 $]\}$

$$\begin{aligned}
\text{SendChangeProposerRequest}(\text{index}) &\triangleq \\
\log' = \log \cup \{[ & \\
\text{type} &\mapsto \text{"CHANGE-PROPOSER"}, \\
\text{height} &\mapsto \text{states}[\text{index}].\text{height}, \\
\text{round} &\mapsto \text{states}[\text{index}].\text{round}, \\
\text{index} &\mapsto \text{index} \\
]&\}
\end{aligned}$$

$$\begin{aligned}
\text{AnnounceBlock}(\text{index}) &\triangleq \\
\log' = \{ \text{msg} \in \log : (\text{msg.type} = \text{"BLOCK-ANNOUNCE"}) \vee \text{msg.height} > \text{states}[\text{index}].\text{height} \} \cup \{[ & \\
\text{type} &\mapsto \text{"BLOCK-ANNOUNCE"}, \\
\text{height} &\mapsto \text{states}[\text{index}].\text{height}, \\
\text{round} &\mapsto \text{states}[\text{index}].\text{round}, \\
\text{index} &\mapsto -1 \\
]&\}
\end{aligned}$$

$$\begin{aligned}
\text{NewHeight}(\text{index}) &\triangleq \\
&\wedge \text{states}[\text{index}].\text{name} = \text{"new-height"} \\
&\wedge \text{states}' = [\text{states} \text{ EXCEPT} \\
&\quad \text{!}[\text{index}].\text{name} = \text{"propose"}, \\
&\quad \text{!}[\text{index}].\text{height} = \text{states}[\text{index}].\text{height} + 1, \\
&\quad \text{!}[\text{index}].\text{round} = 0] \\
&\wedge \text{UNCHANGED } \langle \log \rangle
\end{aligned}$$

$$\begin{aligned}
\text{Propose}(\text{index}) &\triangleq \\
&\wedge \text{states}[\text{index}].\text{name} = \text{"propose"} \\
&\wedge \text{IF } \text{IsProposer}(\text{index}) \\
&\quad \text{THEN } \text{SendProposal}(\text{index}) \\
&\quad \text{ELSE } \log' = \log \\
&\wedge \text{states}' = [\text{states} \text{ EXCEPT } \text{!}[\text{index}].\text{name} = \text{"prepare"}]
\end{aligned}$$

$$\begin{aligned}
\text{Prepare}(\text{index}) &\triangleq \\
&\wedge \text{states}[\text{index}].\text{name} = \text{"prepare"} \\
&\wedge \text{IF } \wedge \text{HasProposal}(\text{states}[\text{index}].\text{height}, \text{states}[\text{index}].\text{round}) \\
&\quad \wedge \neg \text{HasOneThirdOfChangeProposer}(\text{index}) \\
&\quad \vee \text{states}[\text{index}].\text{round} \geq \text{MaxRound} \\
&\text{THEN } \wedge \text{SendPrepareVote}(\text{index}) \\
&\quad \wedge \text{IF } \text{HasPrepareQuorum}(\text{index}) \\
&\quad \quad \text{THEN } \text{states}' = [\text{states} \text{ EXCEPT } \text{!}[\text{index}].\text{name} = \text{"precommit"}] \\
&\quad \quad \text{ELSE } \text{states}' = \text{states} \\
&\text{ELSE } \wedge \text{SendChangeProposerRequest}(\text{index})
\end{aligned}$$

$$\wedge \text{states}' = [\text{states} \text{ EXCEPT } ![index].name = \text{"change-proposer"}]$$

$$\begin{aligned} \text{Precommit}(index) &\triangleq \\ &\wedge \text{states}[index].name = \text{"precommit"} \\ &\wedge \text{SendPrecommitVote}(index) \\ &\wedge \text{IF } \text{HasPrecommitQuorum}(index) \wedge \neg \text{HasOneThirdOfChangeProposer}(index) \\ &\quad \text{THEN } \text{states}' = [\text{states} \text{ EXCEPT } ![index].name = \text{"commit"}] \\ &\quad \text{ELSE } \text{states}' = \text{states} \end{aligned}$$

$$\begin{aligned} \text{Commit}(index) &\triangleq \\ &\wedge \text{states}[index].name = \text{"commit"} \\ &\wedge \text{AnnounceBlock}(index) \\ &\wedge \text{states}' = [\text{states} \text{ EXCEPT } \\ &\quad ![index].name = \text{"new-height"}, \\ &\quad ![index].proposerIndex = (\text{states}[index].round + 1) \% \text{NumValidators}] \end{aligned}$$

$$\begin{aligned} \text{ChangeProposer}(index) &\triangleq \\ &\wedge \text{states}[index].name = \text{"change-proposer"} \\ &\wedge \text{IF } \text{HasChangeProposerQuorum}(index) \\ &\quad \text{THEN } \text{states}' = [\text{states} \text{ EXCEPT } \\ &\quad \quad ![index].name = \text{"propose"}, \\ &\quad \quad ![index].round = \text{states}[index].round + 1] \\ &\quad \text{ELSE } \text{states}' = \text{states} \\ &\wedge \text{UNCHANGED } \langle \log \rangle \end{aligned}$$

$$\begin{aligned} \text{Sync}(index) &\triangleq \\ &\text{LET} \\ &\quad \text{blocks} \triangleq \text{SubsetOfMsgs}([type \mapsto \text{"BLOCK-ANNOUNCE"}, height \mapsto \text{states}[index].height]) \\ &\text{IN} \\ &\quad \wedge \text{Cardinality}(\text{blocks}) > 0 \\ &\quad \wedge \text{states}' = [\text{states} \text{ EXCEPT } \\ &\quad \quad ![index].name = \text{"propose"}, \\ &\quad \quad ![index].height = \text{states}[index].height + 1, \\ &\quad \quad ![index].round = 0, \\ &\quad \quad ![index].proposerIndex = ((\text{CHOOSE } b \in \text{blocks} : \text{TRUE}).round + 1) \% \text{NumValidators}] \\ &\quad \wedge \log' = \log \end{aligned}$$

$$\begin{aligned} \text{Init} &\triangleq \\ &\wedge \log = \{\} \\ &\wedge \text{states} = [index \in 0 \dots \text{NumValidators} - 1 \mapsto [ \\ &\quad \text{name} \mapsto \text{"new-height"}, \\ &\quad \text{height} \mapsto 0, \\ &\quad \text{round} \mapsto 0, \\ &\quad \text{proposerIndex} \mapsto 0 \end{aligned}$$

$$\begin{aligned} \text{Next} &\triangleq \\ &\exists \text{index} \in 0 \dots \text{NumValidators} - 1 : \\ &\quad \vee \text{Sync}(\text{index}) \\ &\quad \vee \text{NewHeight}(\text{index}) \\ &\quad \vee \text{Propose}(\text{index}) \\ &\quad \vee \text{Prepare}(\text{index}) \\ &\quad \vee \text{Precommit}(\text{index}) \\ &\quad \vee \text{Commit}(\text{index}) \\ &\quad \vee \text{ChangeProposer}(\text{index}) \end{aligned}$$
$$Spec \triangleq Init \wedge \Box[Next]_{vars}$$

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