

DAY 6 FP

Gamma: typing environment in Gamma typing envr

above: "under" type type of x is tau1

assumptions under: conclusion

$$\frac{\Gamma \vdash e_1 : \tau_1 \quad \Gamma, x : \tau_1 \vdash e_2 : \tau_2}{\Gamma \vdash \text{let } x = e_1 \text{ in } e_2 : \tau_2} \quad \frac{\Gamma(x) = \tau}{\Gamma \vdash x : \tau}$$

first confirm expression (e) type then conclude the type of whole expression

arg type

x is a function type

only allowed to use in e1

$$\frac{\Gamma, x : \tau_1 \rightarrow \dots \rightarrow \tau_n \rightarrow \tau, y_1 : \tau_1, \dots, y_n : \tau_n \vdash e_1 : \tau \quad \Gamma, x : \tau_1 \rightarrow \dots \rightarrow \tau_n \rightarrow \tau \vdash e_2 : \tau'}{\Gamma \vdash \text{let rec } x = y_1 \dots y_n = e_1 \text{ in } e_2 : \tau'} \quad \frac{\Gamma \vdash e : \tau_1 \rightarrow \dots \rightarrow \tau_n \rightarrow \tau \quad \Gamma \vdash e_1 : \tau_1 \quad \dots \quad \Gamma \vdash e_n : \tau_n}{\Gamma \vdash e \ e_1 \dots e_n : \tau}$$

check x type first then check e2 type if matches

$$\frac{\Gamma \vdash e_1 : \tau_1 \quad \Gamma, x : \tau_1 \vdash e_2 : \tau_2}{\Gamma \vdash \text{let } x = e_1 \text{ in } e_2 : \tau_2}$$

get the conclusion