

Day 4 & 5

Term Weighting & Filtering

The initial m doc set has turned into k terms

- Each term memorizes the frequency with which it appeared in each document
- $k*m$ matrix where row = doc, col = term

Document-Term Matrix (DTM)

	T1	T2	T3
D1	5 (term T1 appeared in D1 5 times)	0	2
D2	0	3	1
D3	2	0	0
D4	0	2	1

Inverted (index) File

Transposing the DTM results in a Term-Document Matrix (TDM) which functions as an index

- TDM is usually called the "inverted file" in principle

In practice simple TDM decreases utility

- The matrix is very sparse (most elements = 0)
- It takes a long time to find the query term in the index

(Transpose of DTM above)	D1	D2	D3	D4
T1	5 (frequency of the term in the doc)	0	2	0
T2	0	3	0	2
T3	2	1	0	1

T1 -> D1 -> D3

T2 -> D2 -> D4

T3 -> D1 -> D2 -> D4

Xxx???? list solves the sparsity problem

- Google index based on everything - ngram, word, phrase
- Ngram variation - skip-gram
- We have billions of terms & docs, in practice to use a matrix

Searching Algorithm & Data Structures: Preliminary

$L[n] = L[0], L[1], \dots, L[n-1]$: a list of integers

- In our case, L is a list of index terms
- Any data can be asked if the order of any possible pairs of instances is defined

Task: Given w as a query, return such x that satisfies $L[x]$ (index) = w (term)
(finding position of w in list L)

- We want to minimize of comparison for 2 values
- Time complexity $f(n) = O(g(n)); n \rightarrow \infty$

Linear Search:

- w is compared to $L[x]$ 1 by 1 while scanning $L \rightarrow r$
- 9 11 19 6 13 15 17 12 9

Binary Search:

- w is compared to the middle of remaining list and moves to the left ($w < L[x]$) or right ($w > L[x]$), otherwise found $w = L[x]$
- Requires a sorted list, so we preprocess the list by sorting it.
- 1(left) 3 4 6 **9(w = 4, start)** 11 12 15 17 19(right)
- $w(=4) < 9$, move to the left
- $w(=4) < 6$, move to the left
- $w(=4) = 4$, found
- $L[2] = w$

Linear search only excludes 1 element in each iteration

Binary search can halve halves the search space in each iteration

- Disadvantage of binary search: you have to re-sort the list every time the data is updated
- How to overcome this weakness?
 - Use a BST

Logical Operation

- Logical operator ($n = \# \text{operands}$)
 - Unary ($n=1$) NOT
 - Binary ($n=2$) OR, AND
- Order of precedence: NOT > AND > OR
- Truth table

A		NOT A
0		1
1		0
A	B	$A \cup B$
0	0	0
0	1	1
1	0	1
1	1	1
A	B	$A \cap B$
0	0	0
0	1	0

1	0	0
1	1	1

Fundamental Retrieval Models

- Exact match: Boolean
- Best match (or Ranking)
 - Vector space
 - Probabilistic
 - Language
 - Learning to rank (L2R)
 - (Neural network)

Boolean retrieval model

- In principle: term = bit string (seq of 0/1)
 - Term T_k = line of TDM (term document matrix) for T_k
 - Query Q = a logical formula of $Q_1 \dots Q_i \dots$
 - Retrieved docs R = solution for Q
 - D_i is retrieved if $D_i > 0$
- $Q = (\text{dog OR mouse}) \text{ AND NOT cat}$
 $R = \{D_2, D_4\}$
- But, in practice it is prohibitive to compute long bit strings

	D1	D2	D3	D4
Cat	1	0	1	0
Dog	0	1	1	1
Mouse	1	1	0	0

Boolean retrieval model

- In principle: term = bit string (seq of 0/1)
 - term T_k = line of TDM for T_k
 - cat = 1010, dog = 0111, mouse = 1100
 - $Q = (\text{dog OR mouse}) \text{ AND NOT cat}$
 $= (0111 \text{ OR } 1100) \text{ AND NOT } 1010$
 $= 1111 \text{ AND } 0101 = 0101 \rightarrow \{D_2, D_4\}$
- In practice, this is not feasible

	D1	D2	D3	D4
cat	1	0	1	0
dog	0	1	1	1
mouse	1	1	0	0

Improving Boolean IR

List of docID containing the head term in ascending order

Dictionary		Postings
Bison	->	1 -> 22 -> 53 -> 145 -> #
Cat	->	1 -> 53 -> 80 -> 172 -> -> 256 -> 404 -> #
Dog	->	9 -> 44 -> 53 -> # sentinel (the end of list)

Efficiently identify and obtain documents whose bit element is 1

Example: Q = bison OR cat (resembles MERGE)

Any D(A) or D(B) can be added to the end of R: D(x) is docID where cursor x is pointing to

docID cannot be duplicated in R

If A or B meets sentinel (#), residue is added to R

if D(A) = # then D(C) <- L(B) (the rest of list B after A #)

if D(A) < D(B) then D(C) <- D(A), A++, C++ (if docID from two cursors different, pick the smaller one because the larger ID might appear in D(A) later but docID cannot be duplicated in R)

if D(A) = D(B) then D(C) <- D(A), A++, B++, C++

Bison	->	1 -> 22 (cursor A) -> 53 -> 145 -> #
Cat	->	1 -> 53 (cursor B) -> 80 -> 172 -> 256 -> 404 -> #
R	->	1 -> 22 (cursor C) -> ... #

***目的：比较A&B两个list的每一个docID，按照上面的规则copy到R