

# SEQUENTIAL LOGIC

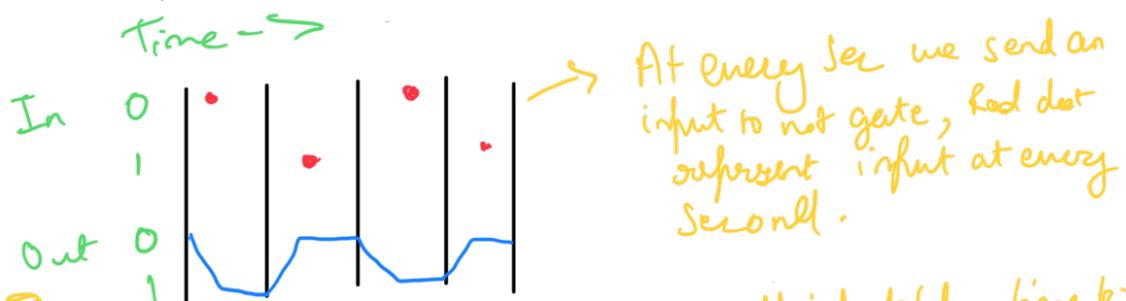
Till now, we have only looked at Combinational Circuits  
→ Combinational Circuits require present input & give present output  
→ Sequential Circ use present inp and past input to give present output.

Lets take the example of ALUs. ALU required a lot of chips but for a particular input all the operations were performed with that input, previous x or y values were not used.

↳ This is an example of Combinational Circuits.

Time is Continuous in real World but in Computer Systems it can be hard to understand what's going on in continuous time bcoz continuous time can have multiple inputs & outputs at varying time.

Real World Ex → Let's say we have a not gate & it takes some time to function. Time is moving forward



In this example  
we take time to be 1 sec but  
it can be anything

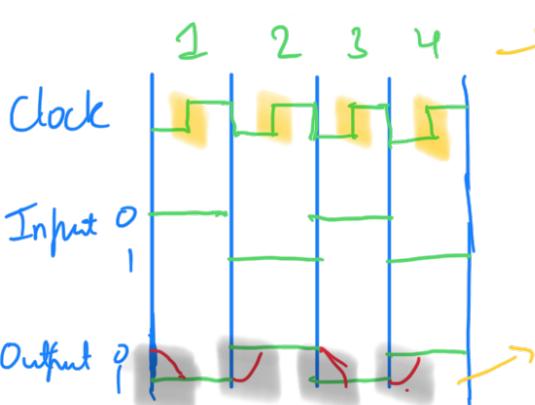
In real world input take time to switch and during that time they spit out weird outputs so we use discrete Time

## Discrete Time

We set up a Clock. This Clock ticks at a predefined time and we only perform actions at that point in time.

Ex: Again we have a not gate & let look at it with a clock

Throughout  
the time input  
stays same



Time is discrete. We don't care about 1.111 or 2.12 etc. we only care about time at 1, 2, 3, ...

Red lines indicate the real world. but we grey that portion out, ignore it & only care about green vals.



## SEQUENTIAL CIRCUIT

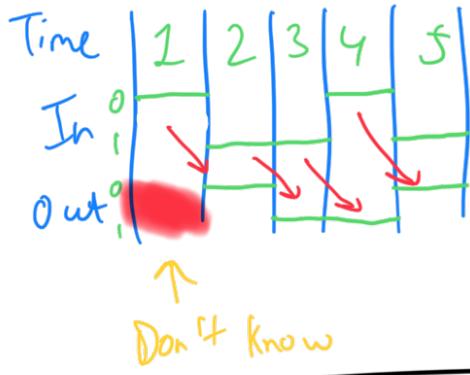
Here we need to take the input from previous time step So unlike our previous function  $out(t) = f(in[t])$ , here it will be  $out[t] = f(in[t-1])$

Time	1	2	3	4
in	a	b	c	d
out	$f(a)$	$f(b)$	$f(c)$	$f(d)$

(basically is  $ff(a)$  & Dis  $f(f(f(f(a))))$ )

DATA FLIP FLOP

$$out = in[t-1]$$



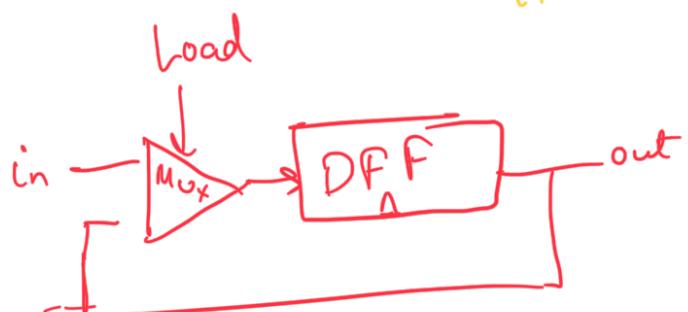
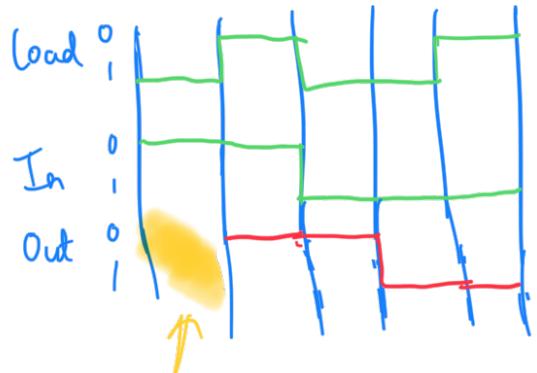
## 1 BIT REGISTER

If remembers a state or bit until we tell it to remember a new Val.



if  $\text{load}(t-1) = 1$  then  $\text{out} = \text{in}(t-1)$   
 else  $\text{out} = \text{out}(t-1)$

↳ previous output  
 thus we remember it.



DFF stands for Data Flip Flop. It is a chip given to us. So, let's make a 1 Bit Register

Remember that a clock ticks & ticks, so in our program  
 in is stored in a tick state & register changes

Output is unchanged in the tick state Ex → We want to store value.

Tick { in = 100 load = 1	Register = 100 Out = 0
Tock { in = 100 load = 1	Register = 100 out = 100

## PROGRAM

```

→ Mux(a = prevout, b = in, sel = load, out = tempout);
DFF(in = tempout, out = out, out = prevout);
  \ / 
  Here we made 2 out pins
  bcz we can't use "out" again
  Remember that everything
  is run in one "swoop"!
  
```

## 16 BIT REGISTER

This is quite straight forward. We just need 16 1-bit registers.

$\text{In} = \text{In}[16], \text{load}$   
 $\text{out} = \text{Out}[16]$

$\text{Bit}(\text{in} = \text{in}[0], \text{load} = \text{load}, \text{out} = \text{out}[0])$

$\text{Bit}(\text{in} = \text{in}[1], \text{load} = \text{load}, \text{out} = \text{out}[1])$

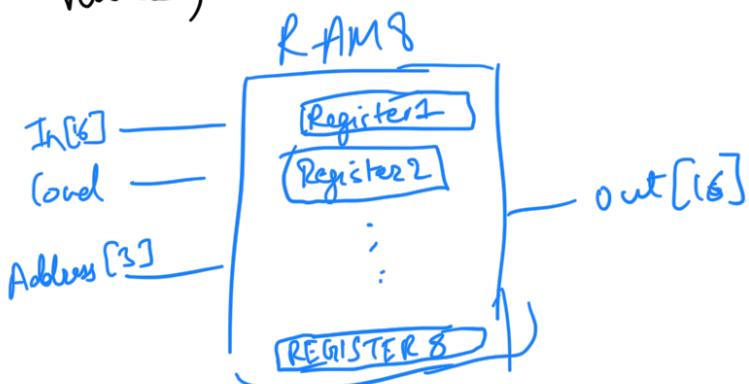
:

... + 16 ]

Bit [in = in[15], load = load, out = out[15]]

# RAM 8

RAM consists of several 16 bit registers & our goal is to read or write any one of these registers. Unless we want to edit these values, the RAM must store them forever.



The address is used to access 1 of 8 registers, load tells us whether to change it or not & Input is our good old input.

address	
0 0 0	→ Register 1
0 0 1	→ Register 2
:	:
1 1 0	→ Register 7
1 1 1	→ Register 8

We need this functionality

We need a way to choose one of these 8 Registers. So we need something like this -



Ring A Bell?

DMUX 8WAY!!!

DMUX 8Way( $in^{load}$ ,  $sel = address$ ,  $a=a$ ,  $b=b \dots h=h$ );

This will make one of the 8 out as 1 and others 0. We will use this as load for our registers.

Register( $in = in$ ,  $load = a$ ,  $out = R1$ );

Register( $in = in$ ,  $load = b$ ,  $out = R2$ );

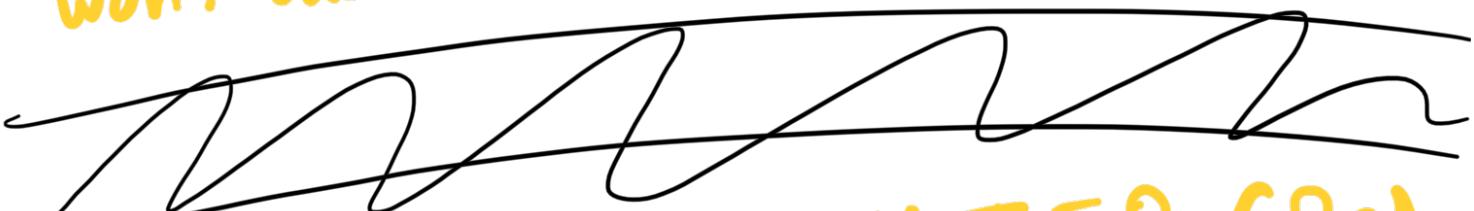
⋮

Register( $in = in$ ,  $load = h$ ,  $out = R8$ );

Now we need to find a way to choose b/w these 8 Registers!

MUX 8Way16( $a=R1$ ,  $b=R2, \dots, h=R8$ ,  $sel = address$ ,  $out = out$ );

You can create RAM 64, RAM 512 etc, in the same way. So we won't discuss RAM further!



## PROGRAM COUNTER (PC)

In  $\rightarrow$   $in[1b]$ , load, inc, reset

Out  $\rightarrow$   $out[1b]$

load	inc	RST	out
			in

Reset overrides  
... at line. if its

0	0	0	0	every in > 0
0	0	1	0	1 out is 0.
0	1	0	1	intl
0	1	1	0	0
1	0	0	new in	new in
1	0	1	0	0
1	1	0	new in	0
1	1	1		

This was the toughest chip for me so far. I tried a lot of times & for some reason increment never worked.

But then eventually I got it!

If we look at our if conditions, reset overrides

all so - - -

The code below is written in a way to aid understanding. the number before the code is the actual line number.

(4) Mux16(a=loadOut, b=false, sel=reset, out=tempOut);

We will get this from our load Output which is the second in our if conditions.

(3) Mux16(a=inout, b=inc, sel=load, out=loadOut);

We will get this from our incrementor

(2) Mux16(a=register value, b=incremented, sel=inc, out=inout);

Value store in the register  
We will get this from inc16

~ ~ ~ register value, out=incremented);

(1)  $\text{Inc}^{16L \text{ in} = \text{reg}} \dots$

At this point, we have our temp Out from the Mux16(... sel=reset). But there is a problem. We haven't specified our register yet & there is no output.

[Also, in the case load is 0 & inc is 1 & reset is 0, we want to change the value in register which currently does not happen]

If you look at the truth table above, you will see that we want to change the value in register when reset or inc is 1 even when load is 0! To do that ↴

Or(a=inc, b=reset, out=newload);  
Mux(a=newload, b=load, sel=load, out=firload);

if load is 0, we want to use new load because we might have used reset or inc but when [load:1], we may want to store the input value, this will also work when reset is 1!

Finally,  
Register(in=tempOut, load=firload, out=out, out=register value);

Y<sub>0(1)</sub>

