Exercises Set 6

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Abstract

Only the questions with a * are compulsory (but do all of them!).

1 Lagrangian multiplier technique



1.1 Unconstrained optimization

Let $f(x,y) = 2x^2 - 3x + 4y^2 + 4y + 20$. Find $(x^*,y^*) \in \mathbb{R}^2$ such that f reaches its minimum (i.e. $f(x^*,y^*) \leq f(x,y) \quad \forall (x,y) \in \mathbb{R}^2$).

1.2 Constrained optimization

Let $f(x,y)=2x^2-3x+4y^2+4y+20$. Suppose further that we want 3x+5y=2. Find $(x^*,y^*)\in\mathbb{R}^2$ such that $3x^*+5y^*=2$ and f reaches its minimum (i.e. $f(x^*,y^*)\leq f(x,y) \quad \forall (x,y)\in\mathbb{R}^2,\ 3x+5y=2$).

1.3 Lagrange multiplier

Let $f(x,y) = 2x^2 - 3x + 4y^2 + 4y + 20$. Suppose further that we want 3x + 5y = 2. Let $\mathcal{L}(x,y,\lambda) = f(x,y) - \lambda(3x + 5y - 2)$. Find the point where $\nabla f = 0$