

Yunuf Bham

CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
- True
 False
- (b) The constraint `Semigroup a => Monoid a` implies that:
- (i) Every type that has a `Semigroup` instance, also has a `Monoid` instance.
 (ii) Every type that has a `Monoid` instance, also has a `Semigroup` instance.
 (iii) Both of the above.
 (iv) None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler.
- (i) True
 (ii) False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a main function:
- (i) The program will fail to typecheck.
~~and ~> the arbitrary testable~~
 (ii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `Int` and `Char` to generate inputs and test `foo`.
 (iii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `()` as default to generate inputs and test `foo`.
 (iv) Haskell will require user-provided generators for integers and characters in order to run the tests

Part 2 - 12pts

The standard library defines `foldMap` with the following type:

`foldMap :: (Monoid m, Foldable t) => (a -> m) -> t a -> m`

For each of the following `foldMap` calls, select all options that are true:

(a) `foldMap ([]) [1..10]`

- (i) The expression will fail to typecheck.
- (ii) The monoid in this call is `Int`.
- (iii) The monoid in this call is `[Int]`.
- (iv) The monoid in this call is `String`.
- (v) The expression is equivalent to the identity function.
- (vi) The foldable in this call is `[]` - the instance for lists.

(b) `foldMap show "123456"`

- (i) The expression will fail to typecheck.
- (ii) The monoid in this call is `Int`.
- (iii) The monoid in this call is `[Int]`.
- (iv) The monoid in this call is `String`.
- (v) The expression is equivalent to the identity function.
- (vi) The foldable in this call is `[]` - the instance for lists.

$(\text{Int} \rightarrow [\text{Int}]) \rightarrow [\text{Int}] \rightarrow [\text{Int}]$

$\text{show} :: \text{a} \rightarrow \text{String}$

$\text{foldMap} (\text{a} \rightarrow \text{String})$

$\Rightarrow [\text{Char} \rightarrow \text{String}]$

$\Rightarrow \text{String}$

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or “well-typed” if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

(a) $\lambda x \rightarrow x$

Example answer:

$a \rightarrow a$

(b) $\lambda x y \rightarrow (x,y)$

(c) $\lambda x y \rightarrow \text{if } x == y \text{ then show } x \text{ else show } (x,y)$

$\boxed{\text{Eq}} \quad a \Rightarrow a \rightarrow a \rightarrow \text{String}$

(d) $\lambda x l \rightarrow x : (l ++ 1 ++ [x])$

$a \rightarrow [a] \rightarrow [a]$

(e) `getLine >>= putStrLn`

$\boxed{\text{IO ()}}$

(f) `putStrLn 42 >>= putStrLn 43`

~~(g) $\lambda () \rightarrow$~~

~~$\lambda () \rightarrow$~~

(h) `reverse . foldMap return`

$[a] \rightarrow [a]$

(i) $\lambda l \rightarrow [(x,y) \mid x < -1, y < -1, x /= y]$

$\boxed{\text{Eq}} \quad a \Rightarrow [a] \rightarrow [c a, a]$

(j) `let f x = x in (f 'a', f True)`

$(\text{char}, \text{Bool})$

(k) `filterM (const [True, False])`

$[a]$

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix, do syntax, list comprehensions, or any valid Haskell.

(a) `Int -> Int`

Example answers:

`\x -> x + 1`

(+1)

(b) `Bool -> [Bool]`

pure

(c) `a -> Maybe b`

const Nothing

(d) `(Int -> Char -> Bool) -> [Int] -> [Char] -> [Bool]`

~~`\$`~~ `a -> map (uncurry \$ zip a b)`

(e) `(a -> b -> c) -> IO a -> IO b -> IO c`

liftM2

(f) `(a -> b) -> (b -> Bool) -> [a] -> [b]`

~~`\$`~~ `a -> map b`

(g) `Maybe a -> (a -> Gen b) -> Gen (a,b)`

~~`\$`~~ `a -> (fromList a) -> (Gen a)`

(h) `Eq a => a -> [a] -> [a]`

~~`\$`~~ `a -> filter (== a)`

(i) `Show a => [a] -> IO String`

pure . foldMap show

(j) `(a,b) -> (a -> b -> c) -> c`

flip uncurry

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a)

```
foo :: [Int] -> [Int]
foo 1 = [ x * x | x <- 1, x > 0 ]
```

Example answer:

Calculates the squares of all positive numbers in a list.

```
foo [] = []
foo [1,0,2,-1] = [1, 4]
```

(b)

```
foo :: [Int] -> [(Int, Int)]
```

```
foo 1 = [ (x,y) | x <- 1, y <- 1, x /= y ]
```

Answer:

Gives every pair of distinct integers in the list (in both orders)

(c)

```
foo :: a -> [a] -> [a]
```

```
foo x 1 = reverse (x : reverse 1)
```

Answer:

It appends at the end of a list

$\text{foo } 4 \text{ } [1, 2, 3] = [1, 2, 3, 4]$

(d)

```
bar :: (a -> Maybe b) -> [a] -> [b]
```

```
bar [] = []
```

```
bar f (x:xs) =
```

```
let rs = bar f xs in
```

```
case f x of
```

```
Nothing -> rs
```

```
Just x -> x:rs
```

```
foo :: [Maybe a] -> [a]
```

```
foo = bar id
```

Answer:

It gives the first elements of a list

Char is just map Maybe

(e)

```
foo :: [Int] -> Int -> (Int, [Int])
```

```
foo [] m = (m, [])
```

```
foo [x] m = (x, [m])
```

```
foo (x : xs) m = (max m' x, m : xs')
```

```
where (m', xs') = foo xs m
```

Answer:

Gives the maximum of the 1st arg and a list of the same length

as the first arg full of the record arg

the record arg

(f) Bonus!

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM _ [] = return []
dropWhileM p (x:xs) = do
    q <- p x
    if q then dropWhileM p xs else return (x:xs)
```

foo :: ??

```
foo = dropWhileM (const [True, False])
```

Answer:

Gives the tail of list
so $\text{C} = \text{C} \text{C} \text{C}$
~~so $\text{C}^1, \text{C}^2, \text{C}^3$~~
 $= [\text{C}^1, \text{C}^2, \text{C}^3,$
 $\text{C}^2, \text{C}^3,$
 $\text{C}^3]$
 $\sqsubseteq \text{C}^3$

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:
`weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]`

You can assume that the lists have the same length.

`foo :: [a] → [a] → [a]`

`foo a b = concat . map (\(ca, cb) → [ca, cb]) $ zip a b`

- (b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

`toMax [1,4,2,5,3] = [5,5,5,5,5]`

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

`toMax l = map (const m) l`

where `m = maximum l`

Bonus

`toMax (x:xs) = snd $ go x xs`

where

`go e (x:xs) = (cm, m: l)`

`go e [] = (cm, e)`

where `cm = max e`

`go e cs = (e, (e:cs))`

Typeclass Definitions

```
class Semigroup a where
  (++) :: a -> a -> a

class Semigroup m => Monoid m where
  mempty :: m

class Show a where
  show :: a -> String

class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool

class Eq a => Ord a where
  compare :: a -> a -> Ordering
  (<), (=<), (=>), (>) :: a -> a -> Bool
  max, min :: a -> a -> a

class Functor f where
  fmap :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure :: a -> f a
  (*>) :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return :: a -> m a
  (=>) :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary :: Gen a
  shrink :: a -> [a]

class Num a where
  (+), (-), (*) :: a -> a -> a
  negate :: a -> a
  abs :: a -> a
  signum :: a -> a
  fromInteger :: Integer -> a
```

CMS 488B: Midterm Exam (Spring 2022)

Matvey Stepanov
WID: 11668401

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
- (i) True
 (ii) False
- (b) The constraint `Semigroup a => Monoid a` implies that:
- (i) Every type that has a `Semigroup` instance, also has a `Monoid` instance.
 (ii) Every type that has a `Monoid` instance, also has a `Semigroup` instance.
 (iii) Both of the above.
 (iv) None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler.
- (i) True
 (ii) False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a `main` function:
- (i) The program will fail to typecheck.
 (ii) After typeclass resolution, the resulting program will use the Arbitrary instance for `Int` and `Char` to generate inputs and test `foo`.
 (iii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `()` as default to generate inputs and test `foo`.
 (iv) Haskell will require user-provided generators for integers and characters in order to run the tests

Part 2 - 12pts

The standard library defines `foldMap` with the following type:

```
foldMap :: (Monoid m, Foldable t) => (a -> m) -> t a -> m
```

For each of the following `foldMap` calls, select all options that are true:

(a) `foldMap ([]) [1..10] => m: [1,2,3, ..., 10] => foldList`

list.fold (k2) mempty

l3

- (i) The expression will fail to typecheck.
- (ii) The monoid in this call is Int.
- (iii) The monoid in this call is [Int].
- (iv) The monoid in this call is String.
- (v) The expression is equivalent to the identity function.
- (vi) The foldable in this call is [] - the instance for lists.

(b) `foldMap show "12345"`

show :: a -> String

- (i) The expression will fail to typecheck.
- (ii) The monoid in this call is Int.
- (iii) The monoid in this call is [Int].
- (iv) The monoid in this call is String.
- (v) The expression is equivalent to the identity function.
- (vi) The foldable in this call is [] - the instance for lists.

[char]

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or “ill-typed” if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

- (a) $\backslash x \rightarrow x$
Example answer:
 $a \rightarrow a$
- (b) $\backslash x y \rightarrow (x,y)$
 $a \rightarrow b \rightarrow (a,b)$
- (c) $\backslash x y \rightarrow \text{if } x == y \text{ then show } x \text{ else show } (x,y)$
 $\text{Eq } a \Rightarrow a \rightarrow a \rightarrow \text{String}$
- (d) $\backslash x l \rightarrow x : l ++ l ++ [x]$
 $a \rightarrow [a] \rightarrow [a]$
- (e) `getLine >>= putStrLn`
- $\text{IO String} \rightarrow \text{IO ()}$
- (f) `putStrLn "42" >>= putStrLn "43"`
- $\text{IO ()} \rightarrow \text{IO ()}$
-
- $\text{IO -typed} \rightarrow \text{should use} \gg$
- (g) $(.) "42"$
 $a \rightarrow (\text{String}, a)$
- (h) `reverse . foldMap return`
 $\text{Foldable t} \Rightarrow t a \rightarrow [a]$
- (i) $\backslash l \rightarrow [(x,y) \mid x <- l, y <- l, x /= y]$
 $\text{Eq } a \Rightarrow [a] \rightarrow [((a,a))]$
- (j) `let f x = x in (f 'a', f True)`
 Haskell error
- (k) `filterM (const [True, False])`
- $[a] \rightarrow [[a]]$
-
- $\hookrightarrow a \rightarrow [\text{Bool}]$

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix, do syntax, list comprehensions, or any valid Haskell.

- (a) $\text{Int} \rightarrow \text{Int}$

Example answers:

$\lambda x \rightarrow x + 1$

(+1)

- (b) $\text{Bool} \rightarrow [\text{Bool}]$

$\lambda b \rightarrow [b]$

- (c) $a \rightarrow \text{Maybe } c$

$\lambda x \rightarrow \text{Nothing}$

- (d) $(\text{Int} \rightarrow \text{Char} \rightarrow \text{Bool}) \rightarrow [\text{Int}] \rightarrow [\text{Char}] \rightarrow [\text{Bool}]$

$\lambda f l_1 l_2 \rightarrow \text{map}(\lambda c. \text{uncurry})(\pi_0 l_1 l_2)$

- (e) $(a \rightarrow b \rightarrow c) \rightarrow \text{IO } a \rightarrow \text{IO } b \rightarrow \text{IO } c$

$\lambda f a b \rightarrow \text{liftM2 } f a b$

- (f) $(a \rightarrow b) \rightarrow (b \rightarrow \text{Bool}) \rightarrow [a] \rightarrow [b]$

$\lambda f u l \rightarrow [f a | a \leftarrow l, u(f a) = \text{True}]$

- (g) $\text{Maybe } a \rightarrow (a \rightarrow \text{Gen } b) \rightarrow \text{Gen } (a, b)$

$\lambda m f \rightarrow$

- (h) $\text{Eq } a \Rightarrow a \rightarrow [a] \rightarrow [a]$

$\lambda v l \rightarrow \text{filter } (== v) l$

- (i) $\text{Show } a \Rightarrow [a] \rightarrow \text{IO String}$

- (j) $(a, b) \rightarrow (a \rightarrow b \rightarrow c) \rightarrow c$

$\lambda p f \rightarrow \text{uncurry } f p$



$\lambda l \rightarrow \text{foldMap show } l$

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what foo does, and some output examples.

(a) `foo :: [Int] -> [Int]`

`foo l = [x * x | x <- 1, x > 0]`

Example answer:

Calculates the squares of all positive numbers in a list.

`foo [] = []`

`foo [1,0,2,-1] = [1, 4]`

(b) `foo :: [Int] -> [Int]`

`foo l = [(x,y) | x <- 1, y <- 1, x /= y]`

Example answer:

Constructs all combinations (pairs) of distinct elements from given list.

(c) `foo :: a -> [a] -> [a]`

`foo x l = reverse (x : reverse l)`

Example answer:

appends x to end of given list l

Ex: `foo 4 [1,2,3] = [1,2,3,4]`

(d) `bar :: (a -> Maybe b) -> [a] -> [b]`

`bar f [] = []`

`let rs = bar f xs in`

`case f x of`

`Nothing -> rs`

`Just r -> r:rs`

`foo :: [Maybe a] -> [a]`

`foo = bar id`

Answer: Creates new list containing non-nothing values from original list. (Any Nothing values are removed and Maybe values are converted).

(e) `foo :: [Int] -> Int -> (Int, [Int])`

`foo [] m = (m, [])`

`foo [x] m = (x, [m])`

`foo (x : xs) m = (max m' x, m : xs')`

where `(m', xs') = foo xs m`

Answer:

Returns a pair: first element is the max of original list OR the default m passed in if original is empty.

Second element is a list of same size as original containing only the default m repeated - # of times.

→ length of original list

(f) Bonus!

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM = [] = return []
dropWhileM p (x:xs) = do
    q <- p x
    if q then dropWhileM p xs else return (x, xs)

foo :: ???
foo = dropWhileM (const [True, False])
```

Answer:

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

`weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]`

You can assume that the lists have the same length.

`weave [] [] = []` `weave :: [α] → [α] → [α]`

`weave (x:xs)(y:ys) = x:y:(weave xs ys)`

`weave`

`-- = undefined`

→ should never reach this case if lists are
of equal lengths.

- (b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

`toMax [1,4,2,5,3] = [5,5,5,5,5]`

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

`maxL :: [Int] → (Int, Int)`

`maxL [] = undefined` -- shouldn't happen

`maxL (x:xs) = maxHelp x xs where`

`maxHelpP :: Int → [Int] → (Int, Int)`

`maxHelpP m [] = (m, [])`

`maxHelpP m (x:t) =`

`let (m', l') = maxHelpP (max m x) t in`

`(m', l' ∷ l)`

`toMax :: [Int] → [Int]`

`toMax l = let (max, len) = (maxL l) in`

`replicate len max`

Typeclass Definitions

```
class Semigroup a where
  (++) :: a -> a -> a

class Semigroup m => Nonoid m where
  mempty :: m

class Show a where
  show :: a -> String

class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool

class Eq a => Ord a where
  compare :: a -> a -> Ordering
  (<), (=<), (=>), (>) :: a -> a -> Bool
  max, min :: a -> a -> a

class Functor f where
  fmap :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure :: a -> f a
  (*>) :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return :: a -> m a
  (=>) :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary :: Gen a
  shrink :: a -> [a]

class Num a where
  (+), (-), (*) :: a -> a -> a
  negate :: a -> a
  abs :: a -> a
  signum :: a -> a
  fromInteger :: Integer -> a
```

Hammad Khan
116646077

CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
 (i) True
 (ii) False
- (b) The constraint `Semigroup a => Monoid a` implies that:
 (i) Every type that has a `Semigroup` instance, also has a `Monoid` instance.
 (ii) Every type that has a `Monoid` instance, also has a `Semigroup` instance.
 (iii) Both of the above.
 (iv) None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler.
 (i) True
 (ii) False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a main function:
 (i) The program will fail to typecheck.
 (ii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `Int` and `Char` to generate inputs and test `foo`.
 (iii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `()` as default to generate inputs and test `foo`.
 (iv) Haskell will require user-provided generators for integers and characters in order to run the tests

Part 2 - 12pts

The standard library defines `foldMap` with the following type:

```
foldMap :: (Monoid m, Foldable t) => (a -> m) -> t a -> m
```

For each of the following `foldMap` calls, select all options that are true:

(a) `foldMap (:) [] [1..10]`

(i) The expression will fail to typecheck.

(ii) The monoid in this call is `Int`.

(iii) The monoid in this call is `[Int]`.

(iv) The monoid in this call is `String`.

(v) The expression is equivalent to the identity function.

(vi) The foldable in this call is `[]` - the instance for lists.

(b) `foldMap show "123456"`

(i) The expression will fail to typecheck.

(ii) The monoid in this call is `Int`.

(iii) The monoid in this call is `[Int]`.

(iv) The monoid in this call is `String`.

(v) The expression is equivalent to the identity function.

(vi) The foldable in this call is `[]` - the instance for lists.

Show "123456"
 $\text{Show} : \text{String} \rightarrow \text{String}$
 askell

$\text{Show} "123456" = "\backslash 123456 \backslash."$

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or “ill-typed” if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

(a) $\backslash x \rightarrow x$

Example answer:

$a \rightarrow a$

(b) $\backslash x y \rightarrow (x,y)$

(c) $\backslash x y \rightarrow \text{if } x == y \text{ then show } x \text{ else show } (x,y)$

$\text{Eq } a \Rightarrow a \rightarrow a \rightarrow \text{String}$

(d) $\backslash x_1 \rightarrow x : 1 \quad \quad 1 \quad \quad 1 \quad \quad \backslash x$

$a \rightarrow [a] \rightarrow [a]$

(e) `getLine >>= putStrLn`

`IO ()`

(f) `putStrLn 42 >>= putStrLn 43`

`IO ()`

(g) `(,) "42"`

$a \rightarrow (\text{String}, a)$

(h) `reverse . foldMap return`

$\text{Foldable } t \Rightarrow t a \rightarrow [a]$

(i) $\backslash l \rightarrow [(x,y) \mid x <- 1, y <- 1, x / = y]$

$\text{Eq } a \Rightarrow [a] \rightarrow [(a,a)]$

(j) $\text{let } f x = x \text{ in } (f `a`, f \text{ True})$

$(\text{Char}, \text{Bool})$

(k) `filterM (const [True, False])`

$[a] \rightarrow [[a]]$

`filterM`

`IOIOIO . foldMap`

`[]`

$(a \rightarrow M \text{ Bool}) \rightarrow [a] \rightarrow [M \text{ A}]$

$M = []$

`foldable` $\vdash (a \rightarrow M) \rightarrow t a \rightarrow M$

`void` M

`return`: $a \rightarrow M$ a

$(a \rightarrow [a]) \rightarrow t a \rightarrow [a]$

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix, do syntax list comprehensions, or any valid Haskell.

- (a) $\text{Int} \rightarrow \text{Int}$

Example answers:

$$\lambda x \rightarrow x + 1$$

(+1).

(b) $\text{Bool} \rightarrow [\text{Bool}]$

$$\lambda b \rightarrow [b \& b]$$

(c) $a \rightarrow \text{Maybe } b$

$$\lambda x \rightarrow \text{Just } []$$

(d) $(\text{Int} \rightarrow \text{Char} \rightarrow \text{Bool}) \rightarrow [\text{Int}] \rightarrow [\text{Char}] \rightarrow [\text{Bool}]$

$$\lambda f \quad xs \quad ys \rightarrow \text{Not}(f 10 `a')) : (zipWith f xs ys)$$

(e) $(a \rightarrow b \rightarrow c) \rightarrow \text{IO } a \rightarrow \text{IO } b \rightarrow \text{IO } c$

liftM2

(f) $(a \rightarrow b) \rightarrow (b \rightarrow \text{Bool}) \rightarrow [a] \rightarrow [b]$

$$\lambda f \quad p2 \quad (x:xs) = \text{if } (\text{not}(f1 (p1 x))) \text{ then } [f1 x] \text{ else } [p1 x]$$

(g) $\text{Maybe } a \rightarrow (a \rightarrow \text{Gen } b) \rightarrow \text{Gen } (a,b)$

Undefined

(h) $\text{Eq } a \Rightarrow a \rightarrow [a] \rightarrow [a]$

$$\lambda x \quad xs \rightarrow \text{if } x = x \text{ then } (x:xs) \text{ else } xs$$

(i) $\text{Show } a \Rightarrow [a] \rightarrow \text{IO String}$

$$\lambda (x:xs) \rightarrow \text{putStrLn}(\text{show } x) \gg \text{getLine}$$

(j) $(a,b) \rightarrow (a \rightarrow b \rightarrow c) \rightarrow c$

$$\lambda (x,y) \quad f \rightarrow f x y$$

May Show xs

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a)

```
foo :: [Int] -> [Int]
foo l = [x * x | x <- l, x > 0]
```

Example answer:

Calculates the squares of all positive numbers in a list.

```
foo [] = []
foo [1,0,2,-1] = [1, 4]
```

(b)

```
foo :: [Int] -> [Int]
foo l = [ (x,y) | x <- l, y <- l, x /= y ]
```

Answer: All pairs of elements from l that are not equal

foo [] = []
foo [1, 2, 3] = [(1, 2), (1, 3), (2, 1), (2, 3), (3, 1), (3, 2)]

(c)

```
foo :: a -> [a] -> [a]
```

```
foo x l = reverse (x : reverse l)
```

Answer: Appends x to the end of l

foo [] = []
foo 5 [1, 2, 3, 4, 5] = [1, 2, 3, 4, 5]

(d)

```
bar :: (a -> Maybe b) -> [a] -> [b]
```

```
bar f (x:xs) =
  let rs = bar f xs in
```

```
  case f x of
```

```
    Nothing -> rs
```

```
    Just r -> r:rs
```

```
foo :: [Maybe a] -> [a]
```

```
foo = bar id
```

Answer: `foo`s all `Nothing` from list of `Maybe`, unwraps `Just`

foo [] -> []
foo [Nothing, Nothing] -> []
foo [Nothing, Nothing] -> []

(e)

```
foo :: [Int] -> Int -> (Int, [Int])
```

```
foo [] m = (m, [])
foo [x] m = (x, [m])
foo (x : xs) m = (max m' x, m : xs')
```

```
where (m', xs') = foo xs m
```

Answer: Repeats m n times where n is the length of the list, or more

foo [] 1 = ([], [])
foo [1, 2, 4] 5 = ([4, [5, 5, 5]], [5, 5, 5])

foo [] 1 = ([], [])
foo [1, 2, 4] 5 = ([4, [5, 5, 5]], [5, 5, 5])

(f) Bonus!

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM [] = return []
dropWhileM p (x:xs) = do
    q <- p x
    if q then dropWhileM p xs else return (x:xs)
```

```
foo :: ??  
foo = dropWhileM (const [True, False])
```

Answer:

foo : [a] -> [[a]]

foo finds all tails of the given list

foo [1, 2, 3] -> [[1, 2, 3], [2, 3], [3]]
foo [] -> []

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

```
weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]
```

You can assume that the lists have the same length.

`weave :: [a] -> [a] -> [a]`

`weave [] [] => []`

`weave (x:xs) (y:ys) = x:y : (weave xs ys)`

- (b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

```
toMax [1,4,2,5,3] = [5,5,5,5,5]
```

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

`toMax :: [Int] -> [Int]`

`toMax [] = []`

`w/ bonus: toMax xs = replicate (length xs) (maximum xs)`

`lengthAndMax :: [Int] -> (Int, Int)`

`lengthAndMax (x:xs) = (l+1, max x x')` where

`(l, x') = lengthAndMax xs`

`lengthAndMax [] = (0, x)`

`lengthAndMax xs = replicate l m` where $(l, m) = \text{lengthAndMax } xs$

Typeclass Definitions

```
class Semigroup a where
  (<>) :: a -> a -> a

class Semigroup m => Monoid m where
  mempty :: m

class Show a where
  show :: a -> String

class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool

class Eq a => Ord a where
  compare :: a -> a -> Ordering
  ((<)), ((<=)), (=>), (>) :: a -> a -> Bool
  max, min :: a -> a -> a

class Functor f where
  fmap :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure :: a -> f a
  (<>*) :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return :: a -> m a
  (('>>=)) :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary :: Gen a
  shrink :: a -> [a]

class Num a where
  (+), (-), (*) :: a -> a -> a
  negate :: a -> a
  abs :: a -> a
  signum :: a -> a
  fromInteger :: Integer -> a
```

Yishen Zhao

CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
- (i) True
 (ii) False
- (b) The constraint `Semigroup a => Monoid a` implies that:
- (i) Every type that has a `Semigroup` instance, also has a `Monoid` instance.
 (ii) Every type that has a `Monoid` instance, also has a `Semigroup` instance.
 (iii) Both of the above.
 (iv) None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler.
- (i) True
 (ii) False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a main function:
- (i) The program will fail to typecheck.
 (ii) After typeclass resolution, the resulting program will use the Arbitrary instance for `Int` and `Char` to generate inputs and test `foo`.
 (iii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `()` as default to generate inputs and test `foo`.
 (iv) Haskell will require user-provided generators for integers and characters in order to run the tests

Part 2 - 12pts

The standard library defines `foldMap` with the following type:

```
foldMap :: (Monoid m, Foldable t) => (a -> m) -> t a -> m
```

For each of the following `foldMap` calls, select all options that are true:

- (a) `foldMap (:) [] [1..10]`
- (i) The expression will fail to typecheck.
 - (ii) The monoid in this call is `Int`.
 - (iii) The monoid in this call is `[Int]`.
 - (iv) The monoid in this call is `String`.
 - (v) The expression is equivalent to the identity function.
 - (vi) The foldable in this call is `[]` - the instance for lists.
- (b) `foldMap show "123456"`
- (i) The expression will fail to typecheck.
 - (ii) The monoid in this call is `Int`.
 - (iii) The monoid in this call is `[Int]`.
 - (iv) The monoid in this call is `String`.
 - (v) The expression is equivalent to the identity function.
 - (vi) The foldable in this call is `[]` - the instance for lists.

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or “ill-typed” if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

(a) $\lambda x \rightarrow x$

Example answer:

$a \rightarrow a$

(b) $\lambda x y \rightarrow (x,y)$

$a \rightarrow b \rightarrow (a,b)$

(c) $\lambda x y \rightarrow \text{if } x == y \text{ then show } x \text{ else show } (x,y)$

$a \rightarrow b \rightarrow \text{String}$

(d) $\lambda x l \rightarrow x : l ++ l ++ [x]$

ill typed

(e) $\text{getLine} >>= \text{putStrLn}$

IO ()

(f) $\text{putStrLn} 42 >>= \text{putStrLn} 43$

(g) $(,) "42"$

ill typed

(h) $a \rightarrow (a, \text{String})$

$\text{reverse} \cdot \text{foldMap} \cdot \text{return}$

(i) $\lambda l \rightarrow [(x,y) \mid x < -1, y < -1, x \neq y]$

ill typed

$[a] \rightarrow [(a,a)]$

(j) $\text{let } f x = x \text{ in } (f `a', f \text{ True})$

$(\text{Char}, \text{Bool})$

(k) $\text{filterM} (\text{const} [\text{True}, \text{False}])$

$[[a]]$

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix, do syntax, list comprehensions, or any valid Haskell.

(a) $\text{Int} \rightarrow \text{Int}$

Example answers:

$$\lambda x \rightarrow x + 1$$

(+1)

(b) $\text{Bool} \rightarrow [\text{Bool}]$

$$\lambda b \rightarrow [b \& \& \text{True}]$$

(c) $a \rightarrow \text{Maybe } b$

undefined

(d) $(\text{Int} \rightarrow \text{Char} \rightarrow \text{Bool}) \rightarrow [\text{Int}] \rightarrow [\text{Char}] \rightarrow [\text{Bool}]$

liftA2

(e) $(a \rightarrow b \rightarrow c) \rightarrow \text{IO } a \rightarrow \text{IO } b \rightarrow \text{IO } c$

liftM2

(f) $(a \rightarrow b) \rightarrow (b \rightarrow \text{Bool}) \rightarrow [a] \rightarrow [b]$

liftM

(g) $\text{Maybe } a \rightarrow (a \rightarrow \text{Gen } b) \rightarrow \text{Gen } (a, b)$

liftM

(h) $\text{Eq } a \Rightarrow a \rightarrow [a] \rightarrow [a]$

$$\lambda a (x : xs) \rightsquigarrow \begin{cases} a = x \text{ then } (x : xs) \\ \text{else } (x : xs) \end{cases}$$

(i) $\text{Show } a \Rightarrow [a] \rightarrow \text{IO String}$

$$(\text{print}, \text{show}), \text{not } \text{putStrLn}$$

(j) $(a, b) \rightarrow (a \rightarrow b \rightarrow c) \rightarrow c$

$$(a, b) \nmid \rightarrow f a b$$

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a) `foo :: [Int] -> [Int]`

`foo l = [x * x | x <- l, x > 0]`

Example answer:

Calculates the squares of all positive numbers in a list.

`foo [] = []`

`foo [1,0,2,-1] = [1, 4]`

(b) `foo :: [Int] -> [Int]`

`foo l = [(x,y) | x <- l, y <- l, x /= y]`

Answer:

, all possible pairs of elements, given that elements can't pair with themselves

(c) `foo :: a -> [a] -> [a]`

`foo x l = reverse (x : reverse l)`

Answer:

append x to end of the list

(d) `bar :: (a -> Maybe b) -> [a] -> [b]`

`bar f [] = []`

`bar f (x:xs) =`

`let rs = bar f xs in`

`case f x of`

`Nothing -> rs`

`Just x -> x:rs`

`foo :: [Maybe a] -> [a]`

`foo = bar id`

Answer:

filter out the "Nothing"s from the list

(e) `foo :: [Int] -> Int -> (Int, [Int])`

`foo [] m = (m, [])`

`foo [x] m = (x, [m])`

`foo (x : xs) m = (max m' x, m : xs')`

`where (m', xs') = foo xs m`

Answer:

finds a tuple where the first is the

largest element in the list, and the second is a history of the maxima during

iterations

(f) *Bonus!*

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM _ [] = return []
dropWhileM p (x:xs) = do
    q <- p x
    if q then dropWhileM p xs else return (x:xs)
```

```
foo :: ???
foo = dropWhileM (const [True, False])
```

Answer:

power set of $\{1, 2\}$

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

`weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]`

You can assume that the lists have the same length.

```
weave (x:xs) (y:ys) = x:y : (weave xs ys)
weave [] [] = []
```

- (b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

`toMax [1,4,2,5,3] = [5,5,5,5,5]`

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

```
toMax l = replicate (length l) (findMax l)
where
  findMax [] = Int.MinValue
  findMax [x] = x
  findMax (x:y:xs) = if x > y then
    findMax x xs
    else
      findMax y xs
```

Typeclass Definitions

```
class Semigroup a where
  (++) :: a -> a -> a

class Semigroup m => Monoid m where
  mempty :: m

class Show a where
  show :: a -> String

class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool

class Eq a => Ord a where
  compare :: a -> a -> Ordering
  (<), (=<), (=>), (>) :: a -> a -> Bool
  max, min :: a -> a -> a

class Functor f where
  fmap :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure :: a -> f a
  (<*>) :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return :: a -> m a
  (">>>=) :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary :: Gen a
  shrink :: a -> [a]

class Num a where
  (+), (-), (*) :: a -> a -> a
  negate :: a -> a
  abs :: a -> a
  signum :: a -> a
  fromInteger :: Integer -> a
```

Prin. Wang

CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
- (i) True
 - (ii) False
- (b) The constraint `Semigroup a => Monoid a` implies that:
- (i) Every type that has a `Semigroup` instance, also has a `Monoid` instance.
 - (ii) Every type that has a `Monoid` instance, also has a `Semigroup` instance.
 - (iii) Both of the above.
 - (iv) None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler.
- (i) True
 - (ii) False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a main function:
- (i) The program will fail to typecheck.
 - (ii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `Int` and `Char` to generate inputs and test `foo`.
 - (iii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `()` as default to generate inputs and test `foo`.
 - (iv) Haskell will require user-provided generators for integers and characters in order to run the tests

Part 2 - 12pts

The standard library defines `foldMap` with the following type:

```
foldMap :: (Monoid m, Foldable t) => (a -> m) -> t a -> m
```

For each of the following `foldMap` calls, select all options that are true:

- (a) `foldMap ([]) [1..10]`

 - (i) The expression will fail to typecheck.
 - (ii) The monoid in this call is Int.
 - (iii) The monoid in this call is [Int].
 - (iv) The monoid in this call is String.
 - (v) The expression is equivalent to the identity function.
 - (vi) The foldable in this call is [] - the instance for lists.

(b) `foldMap show "123456"`

 - (i) The expression will fail to typecheck.
 - (ii) The monoid in this call is Int.
 - (iii) The monoid in this call is [Int].
 - (iv) The monoid in this call is String.
 - (v) The expression is equivalent to the identity function.
 - (vi) The foldable in this call is [] - the instance for lists.

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or “ill-typed” if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

(a) $\lambda x \rightarrow x$

Example answer:

$a \rightarrow a$

(b) $\lambda x y \rightarrow (x,y)$

$a \rightarrow b \rightarrow (a,b)$

(c) $\lambda x y \rightarrow \text{if } x == y \text{ then show } x \text{ else show } (x,y)$

$a \rightarrow b \rightarrow \text{String}$

(d) $\lambda x l \rightarrow x : l ++ l ++ [x]$

$a \rightarrow b \rightarrow [a]$

(e) `getLine >>= putStrLn`

$a \rightsquigarrow b \rightsquigarrow \lambda x$

(f) `putStrLn "42" >>= putStrLn "43"`

ill-typed

(g) `() :: "42"`

ill-typed

(h) `reverse . foldMap return`

$[m a]$

(i) $\lambda l \rightarrow [(x,y) \mid x < -1, y < -1, x /= y]$

$([a] \rightarrow ([a, a]))$

(j) `let f x = x in (f a', f True)`

$('a', True)$

(k) `filterM (const [True, False])`

$(\text{Monad } m) \Rightarrow m [a]$

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix, do syntax, list comprehensions, or any valid Haskell.

(a) $\text{Int} \rightarrow \text{Int}$

Example answers:

$\lambda x \rightarrow x + 1$

(+1)

(b) $\text{Bool} \rightarrow [\text{Bool}]$

$\lambda x \rightarrow [x]$

(c) $a \rightarrow \text{Maybe } b$

undefined

(d) $(\text{Int} \rightarrow \text{Char} \rightarrow \text{Bool}) \rightarrow [\text{Int}] \rightarrow [\text{Char}] \rightarrow [\text{Bool}]$

$\lambda i p w i h$

(e) $(a \rightarrow b \rightarrow c) \rightarrow \text{IO } a \rightarrow \text{IO } b \rightarrow \text{IO } c$

$\lambda f \Delta M \Delta$

(f) $(a \rightarrow b) \rightarrow (b \rightarrow \text{Bool}) \rightarrow [a] \rightarrow [b]$

$\lambda f g h \rightarrow$

(g) $\text{Maybe } a \rightarrow (a \rightarrow \text{Gen } b) \rightarrow \text{Gen } (a, b)$

maybe

(h) $\text{Eq } a \Rightarrow a \rightarrow [a] \rightarrow [a] \quad f = [] - []$

$f \sim (\lambda x : x) = \lambda x = x \quad \text{where } x \sim e \backslash x \in \text{EqList}$

(i) $\text{Show } a \Rightarrow [a] \rightarrow \text{IO String}$

$f s = \text{let } x = "\backslash n \backslash t" \text{ in } s \in \text{EqList}$

(j) $(a, b) \rightarrow (a \rightarrow b \rightarrow c) \rightarrow c$

$\lambda (a, b) f \rightarrow f a b$

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a) `foo :: [Int] -> [Int]`

`foo 1 = [x * x | x <- 1, x > 0]`

Example answer:

Calculates the squares of all positive numbers in a list.

`foo [] = []`

`foo [1,0,2,-1] = [1,4]`

(b) `foo :: [Int] -> [Int]`

`foo 1 = [(x,y) | x <- 1, y <- 1, x /= y]`

Answer: `lets all pairs (x,y) such that x != y`

`foo [] ~ []`

(c) `foo :: a -> [a] -> [a]`

`foo x 1 = reverse (x : reverse 1)`

Answer: `invers x to end of 1`

`foo 1 [2,3] = [2,3,1]`

`foo 2 [1,2] = [2,1,2]`

(d) `bar :: (a -> Maybe b) -> [a] -> [b]`

`bar f [] = []`

`let rs = bar f xs in`

`case f x of`

`Nothing -> rs`

`Just r -> r:rs`

`foo :: [Maybe a] -> [a]`

`foo = bar id`

Answer: `bar return a list whose elements are those such that f applied to them is not Nothing.`

`foo is just the identity function.`

(e) `foo :: [Int] -> Int -> (Int, [Int])`

`foo [] m = (m, [])`

`foo [x] m = (x, [m])`

`foo (x : xs) m = (max m' x, m : xs')`

`where (m', xs') = foo xs m`

Answer:

`foo [] 1 = (1, [])`

`foo [2] 3 = (2, [3])`

`first element is the max of the two second elements given list and the second element`

(f) *Bonus!*

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM _ [] = return []
dropWhileM p (x:xs) = do
    q <- p x
    if q then dropWhileM p xs else return (x:xs)
```

```
foo :: ??  
foo = dropWhileM (const [True, False])
```

Answer:

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

`weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]`

You can assume that the lists have the same length.

`weave [] [] = []`

`weave (x:xs) (y:ys) = [x,y] ++ weave xs ys`

- (b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

`toMax [1,4,2,5,3] = [5,5,5,5,5]`

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

* Not sure if max is defined
in Prelude but if not
max :: (Ord x, Eq x) -> [x] -> x
max [] = undefined
max (x:xs) = foldr (\x y -> if x > y then
x else y) x
xs

Bonus: not sure if this counts but could do something like

Typeclass Definitions

```
class Semigroup a where
  (++) :: a -> a -> a
class Semigroup m => Monoid m where
  mempty :: m
class Show a where
  show :: a -> String
class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool
class Eq a => Ord a where
  compare :: a -> a -> Ordering
  (〈), (≤), (≥), (〉) :: a -> a -> Bool
  max, min :: a -> a -> a
class Functor f where
  fmap :: (a -> b) -> f a -> f b
class Functor f => Applicative f where
  pure :: f a -> f a
  (⊛) :: f (a -> b) -> f a -> f b
class Applicative m => Monad m where
  return :: a -> m a
  (⊛)=) :: m a -> (a -> m b) -> m b
class Foldable t where
  foldMap :: Monoid m => (a -> m) -> t a -> m
class Arbitrary a where
  arbitrary :: Gen a
  shrink :: a -> [a]
class Num a where
  (+), (-), (*) :: a -> a -> a
  negate :: a -> a
  abs :: a -> a
  signum :: a -> a
  fromInteger :: Integer -> a
```

Zachary
Gurwitz

(P6)

CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
 (i) True
 (ii) False
- (b) The constraint `Semigroup a => Monoid a` implies that:
 (i) Every type that has a `Semigroup` instance, also has a `Monoid` instance.
 (ii) Every type that has a `Monoid` instance, also has a `Semigroup` instance.
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- (c) Typeclass laws are enforced by the Haskell compiler.
 (i) True
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- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a `main` function:
 (i) The program will fail to typecheck.
 (ii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `Int` and `Char` to generate inputs and test `foo`.
 (iii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `()` as default to generate inputs and test `foo`.
 (iv) Haskell will require user-provided generators for integers and characters in order to run the tests

Part 2 - 12pts

The standard library defines `foldMap` with the following type:

```
foldMap :: (Monoid m, Foldable t) => (a -> m) -> t a -> m
```

For each of the following `foldMap` calls, select all options that are true:

(a) `foldMap (:) [] [1..10]`

- (i) The expression will fail to typecheck.
- (ii) The monoid in this call is `Int`.
- (iii) The monoid in this call is `[Int]`.
- (iv) The monoid in this call is `String`.
- (v) The expression is equivalent to the identity function.
- (vi) The `foldable` in this call is `[]` - the instance for lists.

(b) `foldMap show "123456"`

- (i) The expression will fail to typecheck.
- (ii) The monoid in this call is `Int`.
- (iii) The monoid in this call is `[Int]`.
- (iv) The monoid in this call is `String`.
- (v) The expression is equivalent to the identity function.
- (vi) The `foldable` in this call is `[]` - the instance for lists.

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or “ill-typed” if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

(a) $\lambda x \rightarrow x$
Example answer:

$a \rightarrow a$

(b) $\lambda x y \rightarrow (x,y)$
 ~~$a \Rightarrow b \Rightarrow (a,b)$~~

$m a \rightarrow (a \Rightarrow mb) \rightarrow mb$

(c) $\lambda x y \rightarrow \text{if } x == y \text{ then show } x \text{ else show } (x,y)$
 ~~$\text{if } - \text{typed}$~~

(d) $\lambda x l \rightarrow x : l \xrightarrow{} l + + 1 + + [x]$
 ~~$a \rightarrow [a] \rightarrow [a]$~~

(e) $\text{getLine} >>= \text{putStrLn}$

~~$S \xrightarrow{} \text{ring} \rightarrow \text{IO ()}$~~

(f) $\text{putStrLn "42"} >>= \text{putStrLn "43"}$

~~$\text{if } - \text{typed}$~~

(g) $\lambda () \xrightarrow{} "42"$
 $\Gamma \vdash a \rightarrow (a, [a])$

(h) $\text{reverse} \cdot \text{foldMap} \text{return}$

~~$[a] \rightarrow [a]$~~

(i) $\lambda l \rightarrow [(x,y) \mid x < -1, y < -1, x / = y]$
 $[a] \rightarrow [[a,a]]$

(j) $\text{let } f x = x \text{ in } (f `a`, f \text{ True})$
 ~~$\text{if } - \text{typed}$~~

(k) $\text{filterM} (\text{const} [\text{True}, \text{False}])$

$[a] \rightarrow [[a]]$

$$\left(\begin{array}{l} \text{filterM} :: (a \rightarrow m \text{ Bool}) \rightarrow [a] \rightarrow m [a] \\ \text{const} [\text{True}, \text{False}] :: a \rightarrow [m \text{ Bool}] \end{array} \right)$$

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix, do syntax, list comprehensions, or any valid Haskell.

(a) $\text{Int} \rightarrow \text{Int}$

Example answer:

$\lambda x \rightarrow x + 1$

(b) $\text{Bool} \rightarrow [\text{Bool}]$

$\lambda b \rightarrow [b]$

(c) $\text{a} \rightarrow \text{Maybe b}$

$\lambda x \rightarrow \text{Nothing}$

(d) $(\text{Int} \rightarrow \text{Char} \rightarrow \text{Bool}) \rightarrow [\text{Int}] \rightarrow [\text{Char}] \rightarrow [\text{Bool}]$

$Z; \rho; i; t;$

(e) $(\text{a} \rightarrow \text{b} \rightarrow \text{c}) \rightarrow \text{IO a} \rightarrow \text{IO b} \rightarrow \text{IO c}$

liftM2

(f) $(\text{a} \rightarrow \text{b}) \rightarrow (\text{b} \rightarrow \text{Bool}) \rightarrow [\text{a}] \rightarrow [\text{b}]$

$\lambda x y z \rightarrow \text{filter } y \text{ } \text{map } x \text{ } z$

(g) $\text{Maybe a} \rightarrow (\text{a} \rightarrow \text{Gen b}) \rightarrow \text{Gen (a,b)}$

$\lambda x y \rightarrow \text{filter } c \text{ } y \rightarrow \text{arbitrary } | \text{Nothing } y \rightarrow \text{undefined}$

(h) $\text{Eq a} \Rightarrow \text{a} \rightarrow [\text{a}] \rightarrow [\text{a}]$

$\lambda x y \rightarrow \text{filter } (= x) \text{ } y$

(i) $\text{Show a} \Rightarrow [\text{a}] \rightarrow \text{IO String}$

$\lambda x \rightarrow \text{return } (\text{concatMap } \text{show } x)$

(j) $(\text{a}, \text{b}) \rightarrow (\text{a} \rightarrow \text{b} \rightarrow \text{c}) \rightarrow \text{c}$

$\lambda (x,y) z \rightarrow z \times y$

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a) `foo :: [Int] -> [Int]`

`foo 1 = [x * x | x <- 1, x > 0]`

Example answer:

Calculates the squares of all positive numbers in a list.

`foo [] = []`

`foo [1,0,2,-1] = [1, 4]`

(b) `foo :: [Int] -> [Int]`

`foo 1 = [(x,y) | x <- 1, y <- 1, x /= y]`

Answer:

returns all ordered pairs with unequal terms in a list

`foo [] = []`

`foo [(1,2), (2,1)] = [(1,2), (2,1)]`

(c) `foo :: a -> [a]`

`foo x 1 = reverse (x : reverse 1)`

Answer:

put element at the end of a list

`foo "a" "def" = "defa"`

`foo 1 [3,4] = [3,1,4,1]`

(d) `bar :: (a -> Maybe b) -> [a] -> [b]`

`bar [] = []`

`bar f (x:xs) =`

`let rs = bar f xs in`

`case f x of`

`Nothing -> rs`

`Just r -> r:rs`

`foo :: [Maybe a] -> [a]`

`foo = bar id`

Answer:

make a list of values inside maybes in a list. (Cat maybes)

`foo [Just 2, Nothing] = [2]`

`foo [Nothing, Nothing] = []`

(e) `foo :: [Int] -> Int -> (Int, [Int])`

`foo [] m = (m, [])`

`foo [x] m = (x, [m])`

`foo (x : xs) m = (max m' x, m : xs')`

where (m' , xs') = foo xs m

Answer:

returns a tuple of the max of a list and a number repeated the length of the list times. If the list is empty, returns the number as the "max," and the repeat is zero times

`foo [1,2] 3 = (max 2 1, 3:[3]) = (2, [3,3])`

`foo [2] 3 = (2, [3])`

`foo [] 20 = (20,[])`

`foo [2,4,1] 3 = (max 2 3:[3,3]) = (4, [3,3,3])`

`foo [4,1] 3 = (max 4 1, 3:[3]) = (4, [3,3])`

`foo [] 3 = (1, [3])`

(f) Bonus!

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM [] = return []
dropWhileM p (x:xs) = do
    q <- _ x
    if q then dropWhileM p xs else return (x:xs)
```

```
foo :: ?? String -> [a] -> [[a]]
foo = dropWhileM (const [True, False])
```

Answer:

give a list of lists which are suffixes of the original list.

$$f_0 \circ [1, 2, 3] = [[1, 2, 3], [2, 3], [3], []]$$

$$f_0 \circ [] = []$$

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

`weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]`

You can assume that the lists have the same length.

`weave [] [] = []`
`weave (x:xs) (y:ys) = x:y:weave xs ys`
`weave _ _ = undefined`

- (b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

`toMax [1,4,2,5,3] = [5,5,5,5,5]`

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

~~`toMax [] = []`~~
~~`toMax xs = rep m n where`~~
~~`rep m n =`~~
~~`f :: a -> [a] -> Int -> (a, Int)`~~
~~`f m n = f (max m n) ls (n+1)`~~
~~`rep :: a -> Int -> [a]`~~
~~`rep v 0 = []`~~
~~`v c = v:repeat v (c-1)`~~

Typeclass Definitions

```
class Semigroup a where
  (++) :: a -> a -> a

class Semigroup m => Monoid m where
  mempty :: m

class Show a where
  show :: a -> String

class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool

class Eq a => Ord a where
  compare :: a -> a -> Ordering
  (<), (=), (>=), (>) :: a -> a -> Bool
  max, min :: a -> a -> a

class Functor f where
  fmap :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure :: a -> f a
  (<>*>) :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return :: a -> m a
  (">>=) :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary :: Gen a
  shrink :: a -> [a]

class Num a where
  (+), (-), (*) :: a -> a -> a
  negate :: a -> a
  abs :: a -> a
  signum :: a -> a
  fromInteger :: Integer -> a
```

Jacob Grünburg

CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
- (i) True
 (ii) False
- (b) The constraint `Semigroup a => Monoid a` implies that:
- (i) Every type that has a `Semigroup` instance, also has a `Monoid` instance.
 (ii) Every type that has a `Monoid` instance, also has a `Semigroup` instance.
 (iii) Both of the above.
 (iv) None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler.
- (i) True
 (ii) False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a `main` function:
- (i) The program will fail to typecheck.
 (ii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `Int` and `Char` to generate inputs and test `foo`.
 (iii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `()` as default to generate inputs and test `foo`.
 (iv) Haskell will require user-provided generators for integers and characters in order to run the tests

Part 2 - 12pts

The standard library defines foldMap with the following type:

```
foldMap :: (Monoid m, Foldable t) => (a -> m) -> t a -> m
```

For each of the following foldMap calls, select all options that are true:

- (a) `foldMap (:) [] [1..10]`
- (i) The expression will fail to typecheck.
 - (ii) The monoid in this call is Int.
 - (iii) The monoid in this call is [Int].
 - (iv) The monoid in this call is String.
 - (v) The expression is equivalent to the identity function.
 - (vi) The foldable in this call is [] - the instance for lists.
- (b) `foldMap show "12345"`
- (i) The expression will fail to typecheck.
 - (ii) The monoid in this call is Int.
 - (iii) The monoid in this call is [Int].
 - (iv) The monoid in this call is String.
 - (v) The expression is equivalent to the identity function.
 - (vi) The foldable in this call is [] - the instance for lists.

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or “ill-typed” if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

- (a) $\lambda x \rightarrow x$
Example answer:
 $a \rightarrow a$
- (b) $\lambda x y \rightarrow (x,y)$
 $a \rightarrow b \rightarrow (a, b)$
- (c) $\lambda x y \rightarrow \text{if } x == y \text{ then show } x \text{ else show } (x,y)$
“ill-typed”
- (d) $\lambda x l \rightarrow x : l ++ l ++ [x]$
 $a \rightarrow [a] \rightarrow [a]$
- (e) $\text{getLine} >>= \text{putStrLn}$
 $\text{IO String} \rightarrow (\text{String} \rightarrow \text{IO ()}) \rightarrow \text{IO ()}$
- (f) $\text{putStrLn} 42 >>= \text{putStrLn} 43$
“ill-typed”
- (g) $(,) "42"$
 $\text{String} \rightarrow (\text{Char}, \text{Char})$
- (h) $\text{reverse} . \text{foldMap} \text{return}$
“ill-typed”
- (i) $\lambda l \rightarrow [(x,y) | x < -1, y < -1, x /= y]$
 $\exists a \rightarrow [a] \rightarrow [[a, a]]$
- (j) $\text{let } f x = x \text{ in } (f 'a', f \text{ True})$
 $(\text{Char} \rightarrow a) \rightarrow (\text{Bool} \rightarrow b) \rightarrow (a, b)$
- (k) $\text{filterM} (\text{const} [\text{True}, \text{False}])$
“ill-typed”

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix, do syntax, list comprehensions, or any valid Haskell.

- (a) $\text{Int} \rightarrow \text{Int}$
Example answers:
 $\lambda x \rightarrow x + 1$
(+1)
- (b) $\text{Bool} \rightarrow [\text{Bool}]$
 $\lambda x \rightarrow \text{if } x \text{ then } [x] \text{ else } [\neg x]$
- (c) $a \rightarrow \text{Maybe } b$
 $\lambda x \rightarrow \text{Nothing}$
- (d) $(\text{Int} \rightarrow \text{Char} \rightarrow \text{Bool}) \rightarrow [\text{Int}] \rightarrow [\text{Char}] \rightarrow [\text{Bool}]$
 $\lambda f x y \rightarrow \text{foldr}(\text{foldr}(\text{foldr}(\lambda u v \rightarrow f u v) x) y)$
- (e) $(a \rightarrow b \rightarrow c) \rightarrow \text{IO } a \rightarrow \text{IO } b \rightarrow \text{IO } c$
- (f) $(a \rightarrow b) \rightarrow (b \rightarrow \text{Bool}) \rightarrow [a] \rightarrow [b]$
 $\lambda f g xs \rightarrow \text{foldr}(\lambda x acc \rightarrow \text{if } g(f x) \text{ then } f x : acc \text{ else } acc) xs$
- (g) $\text{Maybe } a \rightarrow (a \rightarrow \text{Gen } b) \rightarrow \text{Gen } (a, b)$
 $\lambda f x y \rightarrow \text{if } \text{isJust } x \text{ then arbitrary}$
- (h) $\text{Eq } a \Rightarrow a \rightarrow [a] \rightarrow [a]$
 $\lambda x \rightarrow (\lambda =:= \text{id } x) : [$
- (i) $\text{Show } a \Rightarrow [a] \rightarrow \text{IO String}$
 $\lambda xs \rightarrow \text{getLine}$
- (j) $(a, b) \rightarrow (a \rightarrow b \rightarrow c) \rightarrow c$
 $\lambda f g \rightarrow (\lambda t f = (x, y) \rightarrow g x y)$

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a) `foo :: [Int] -> [Int]`
`foo l = [x * x | x <- 1, x > 0]`

Example answer:

Calculates the squares of all positive numbers in a list.
`foo [] = []`
`foo [1,0,2,-1] = [1, 4]`

(b) `foo :: [Int] -> [Int]`
`foo l = [(x,y) | x <- 1, y <- 1, x /= y]`

Answer: Creates a list of tuples of all unequal elements in a list

`foo [1,1,2,3] = [(1,2),(1,3),(2,3)]`

(c) `foo :: a -> [a] -> [a]`
`foo x l = reverse (x : reverse l)`

Answer: appends `x` to the end of `l`

`foo 4 [1,2,3] = [1,2,3,4]`

(d) `bar :: (a -> Maybe b) -> [a] -> [b]`
`bar f [] = []`
`bar f (x:xs) = Just x : bar f xs`

`let rs = bar f xs in`
case `f x` of
Nothing -> rs
Just r -> r:rs

`foo :: [Maybe a] -> [a]`
`foo = bar id`

Answer: Composes a list of elements that aren't Nothing

`foo [Just (Nothing,Nothing)] = []`

(e) `foo :: [Int] -> Int -> (Int, [Int])`
`foo [] m = (m, [])`
`foo [x] m = (x, [m])`
`foo (x : xs) m = (max m' x, m : xs')`
`where (m', xs') = foo xs m`

Answer: Returns a tuple of the maximum element of the given argument
and the list and a list of maximum elements at each part of the list

`foo [1,2,3] 4 = (4, [1,2,4])`

`foo [1,2,3] 1 = (3, [1,2,3])`

`foo [4,5,6] 5 = (6, [5,5,6])`

(f) Bonus!

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM _ [] = return []
dropWhileM p (x:xs) = do
    q <- p x
    if q then dropWhileM p xs else return (x:xs)
```

```
foo :: ??
```

```
foo = dropWhileM (const [True, False])
```

Answer:

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

`weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]`

You can assume that the lists have the same length.

$$\begin{aligned} \text{weave } [] &= [] \\ \text{weave } (x:xs), (y:ys) &= x:y:(\text{weave } xs\ ys) \end{aligned}$$

- (b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

`toMax [1,4,2,5,3] = [5,5,5,5,5]`

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

$$\begin{aligned} \text{maxList } (x:xs) &= \text{case foo } x\ xs \text{ of} \\ &\quad (a,b) \rightarrow \text{Just } a \\ &\quad _ \rightarrow \text{Nothing} \\ \text{maxList } _ &= \text{Nothing} \end{aligned}$$

$$\text{toMax} = \text{foldr } (\text{let } a = \text{maxList } \text{in } a) []$$

Typeclass Definitions

```
class Semigroup a where
  (<>)
    :: a -> a -> a

class Semigroup m => Monoid m where
  mempty :: m

class Show a where
  show
    :: a -> String

class Eq a where
  (==)
    :: a -> a -> Bool
  (/=)
    :: a -> a -> Bool

class Eq a => Ord a where
  compare
    :: a -> a -> Ordering
  (, (=), (=), (>) )
    :: a -> a -> Bool
  max, min
    :: a -> a -> a

class Functor f where
  fmap
    :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure
    :: a -> f a
  ( <*> )
    :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return
    :: a -> m a
  ( >>= )
    :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap
    :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary
    :: Gen a
  shrink
    :: a -> [a]

class Num a where
  (+), (-), (*)
    :: a -> a -> a
  negate
    :: a -> a
  abs
    :: a -> a
  signum
    :: a -> a
  fromInteger
    :: Integer -> a
```

Aaron Ortevin

CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
 - (i) True
 - (ii) False
- (b) The constraint `Semigroup a => Monoid a` implies that:
 - (i) Every type that has a `Semigroup` instance, also has a `Monoid` instance.
 - (ii) Every type that has a `Monoid` instance, also has a `Semigroup` instance.
 - (iii) Both of the above.
 - (iv) None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler.
 - (i) True
 - (ii) False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a main function:
 - (i) The program will fail to typecheck.
 - (ii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `Int` and `Char` to generate inputs and test `foo`.
 - (iii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `()` as default to generate inputs and test `foo`.
 - (iv) Haskell will require user-provided generators for integers and characters in order to run the tests

Part 2 - 12pts

The standard library defines `foldMap` with the following type:

```
foldMap : (Monoid m, Foldable t) => (a -> m) -> t a -> m
```

For each of the following `foldMap` calls, select all options that are true:

(a) `foldMap (:)` [1..10]`

- (i) The expression will fail to typecheck.
- (ii) The monoid in this call is `Int`.
- (iii) The monoid in this call is `[Int]`.
- (iv) The monoid in this call is `String`.
- (v) The expression is equivalent to the identity function.
- (vi) The foldable in this call is `[]` - the instance for lists.

(b) `foldMap show "123456"`

- (i) The expression will fail to typecheck.
- (ii) The monoid in this call is `Int`.
- (iii) The monoid in this call is `[Int]`.
- (iv) The monoid in this call is `String`.
- (v) The expression is equivalent to the identity function.
- (vi) The foldable in this call is `[]` - the instance for lists.

Question 2 (20 points)

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or “ill-typed” if it contains

- $a \rightarrow a$

(b) $\lambda x y \rightarrow (x,y)$
 $a \rightarrow b \rightarrow (a,b)$

(c) $\lambda x y \rightarrow \text{if } x == y \text{ then show } x \text{ else show } (x,y)$

$\text{Eq } a \Rightarrow a \rightarrow a \rightarrow \text{String}$

(d) $\lambda x \ 1 \rightarrow x : 1 + + 1 + + [x]$
 $a \rightarrow [a] \rightarrow [a]$

(e) `getLine >>= putStrLn`

IO ()

(f) `putStrLn "42" >>= putStrLn "43"`

!-typed

(g) `(,) "42"`

(h) `reverse . foldMap return`

$[a] \rightarrow [a]$

(i) $\lambda 1 \rightarrow [(x,y) \mid x < -1, y < -1, x / = y]$
 $[a] \rightarrow [(a,a)]$

(j) `let f x = x in (f 'a', f True)`

$(\text{Char}, \text{Bool})$

(k) `filterM (\const [True, False])`

$[a] \rightarrow [[a]]$

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix, do syntax, list comprehensions, or any valid Haskell.

- (a) $\text{Int} \rightarrow \text{Int}$

Example answers:

$\lambda x \rightarrow x + 1$

(+1)

- (b) $\text{Bool} \rightarrow [\text{Bool}]$
 $\lambda x \rightarrow \text{if } x \text{ then } [x] \text{ else } [x]$

- (c) $a \rightarrow \text{Maybe } b$

id

- (d) $(\text{Int} \rightarrow \text{Char} \rightarrow \text{Bool}) \rightarrow [\text{Int}] \rightarrow [\text{Char}] \rightarrow [\text{Bool}]$

$\lambda f i c \rightarrow f (\text{head } i) (\text{head } c)$

- (e) $(a \rightarrow b \rightarrow c) \rightarrow \text{IO } a \rightarrow \text{IO } b \rightarrow \text{IO } c$

liftM2

- (f) $(a \rightarrow b) \rightarrow (b \rightarrow \text{Bool}) \rightarrow [a] \rightarrow [b]$

$\lambda f g l \rightarrow \text{map } (\lambda x \rightarrow \text{if } g x \text{ then } f x \text{ else } f x) l$

- (g) $\text{Maybe } a \rightarrow (\text{a} \rightarrow \text{Gen } b) \rightarrow \text{Gen } (a, b)$

$\lambda m g \rightarrow$

- (h) $\text{Eq } a \Rightarrow a \rightarrow [a] \rightarrow [a]$

$\lambda x l \rightarrow \text{if } x == x \text{ then } x : l \text{ else } l$

- (i) Show $a \Rightarrow [a] \rightarrow \text{IO String}$

- (j) $(a, b) \rightarrow (a \rightarrow b \rightarrow c) \rightarrow c$

flip uncurry

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a) `foo :: [Int] -> [Int]`

`foo l = [x * x | x <- 1, x > 0]`

Example answer:

Calculates the squares of all positive numbers in a list.

`foo [] = []`

`foo [1,0,2,-1] = [1, 4]`

(b) `foo :: [Int] -> [Int]`

`foo l = [(x,y) | x <- 1, y <- 1, x /= y]`

Answer: Creates pairs out of every permutation of two distinct elements in a list

`foo [1,2] = [(1,2),(2,1)]`

`foo [1,2,3] = [(1,2),(1,3),(2,1),(2,3),(3,1),(3,2)]`

`foo :: a -> [a] -> [a]`

`foo x l = reverse (x : reverse l)`

Answer: Moves the head of a non-empty list to be its last element

`foo [1] = [1]`

`foo [1,2,3,4,5] = [2,3,4,5,1]`

(d) `bar :: (a -> Maybe b) -> [a] -> [b]`

`bar f [] = []`

`let rs = bar f xs in`

`case f x of`

`Nothing -> rs`

`Just r -> r:rs`

`foo :: [Maybe a] -> [a]`

`foo = bar id`

Answer: Extracts the values from a list of monadic Maybe values

`foo [Nothing] = []`

`foo [Just 1, Just 2, Nothing, Just 3] = [1,2,3]`

(e) `foo :: [Int] -> Int -> (Int, [Int])`

`foo [] m = (m, [])`

`foo [x] m = (x, [m])`

`foo (x : xs) m = (max m' x, m : xs')`

`where (m', xs') = foo xs m`

Answer: Returns a pair consisting of the maximum element of the list (or a default value `m` for empty lists) and a list of the same length where all elements are `m`

`foo [] 5 = (5,[])`

`foo [1] 5 = (1,[5])`

`foo [1,2,3,4,5] 5 = (5,[5,5,5,5,5])`

(f) Bonus!

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM [] = return []
dropWhileM p (x:xs) = do
    q <- p x
    if q then dropWhileM p xs else return (x:xs)
```

```
foo :: ??
```

```
foo = dropWhileM (const [True, False])
```

Answer:

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

```
weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]
```

You can assume that the lists have the same length.

```
weave :: [a] -> [a] -> [a]
weave [] [] = []
weave (x:xs) (y:ys) = x:y : weave xs ys
```

- (b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

```
toMax [1,4,2,5,3] = [5,5,5,5,5]
```

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

```
toMax :: [Int] -> [Int]
toMax [] = []
toMax [x] = [x]
toMax (x:xs) = let (m,_) = foo (x:xs) x in snd (foo (x:xs) m)
```

Typeclass Definitions

```
class Semigroup a where
  (<>)
    :: a -> a -> a

class Semigroup m => Monoid m where
  mempty :: m

class Show a where
  show
    :: a -> String

class Eq a where
  (==)
    :: a -> a -> Bool
  (/=)
    :: a -> a -> Bool

class Eq a => Ord a where
  compare
    :: a -> a -> Ordering
  (<), (=<), (=>), (>)
    :: a -> a -> Bool
  max, min
    :: a -> a -> a

class Functor f where
  fmap
    :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure
    :: a -> f a
  (*>)
    :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return
    :: a -> m a
  (=>)
    :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap
    :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary
    :: Gen a
  shrink
    :: a -> [a]

class Num a where
  (+), (-), (*)
    :: a -> a -> a
  negate
    :: a -> a
  abs
    :: a -> a
  signum
    :: a -> a
  fromInteger
    :: Integer -> a
```

Hitesh Nukalapati

CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
- (i) True
 - (ii) False
- (b) The constraint $\text{Semigroup } a \Rightarrow \text{Monoid } a$ implies that:
- (i) Every type that has a `Semigroup` instance, also has a `Monoid` instance.
 - (ii) Every type that has a `Monoid` instance, also has a `Semigroup` instance.
 - (iii) Both of the above.
 - (iv) None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler.
- (i) True
 - (ii) False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a `main` function:
- (i) The program will fail to typecheck.
 - (ii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `Int` and `Char` to generate inputs and test `foo`.
 - (iii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `()` as default to generate inputs and test `foo`.
 - (iv) Haskell will require user-provided generators for integers and characters in order to run the tests

Part 2 - 12pts

The standard library defines `foldMap` with the following type:

```
foldMap :: (Monoid m, Foldable t) => (a -> m) -> t a -> m
```

For each of the following `foldMap` calls, select all options that are true:

(a) `foldMap (:) [] [1..10]`

- (i) The expression will fail to typecheck.
- (ii) The monoid in this call is `Int`.
- (iii) The monoid in this call is `[Int]`.
- (iv) The monoid in this call is `String`.
- (v) The expression is equivalent to the identity function.
- ~~(vi)~~ The foldable in this call is `[]` - the instance for lists.

(b) `foldMap show "123456"`

- (i) The expression will fail to typecheck.
- (ii) The monoid in this call is `Int`.
- (iii) The monoid in this call is `[Int]`.
- ~~(iv)~~ The monoid in this call is `String`.
- ~~(v)~~ The expression is equivalent to the identity function.
- ~~(vi)~~ The foldable in this call is `[]` - the instance for lists.

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or “ill-typed” if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

- (a) $\lambda x \rightarrow x$

Example answer:

$a \rightarrow a$

- (b) $\lambda x y \rightarrow (x, y)$

$a \rightarrow b \rightarrow (a, b)$

- (c) $\lambda x y \rightarrow \text{if } x == y \text{ then show } x \text{ else show } (x, y)$

~~Monoid Eq a, Show a~~ $\Rightarrow a \rightarrow a \rightarrow \text{String}$

- (d) $\lambda x l \rightarrow x : l ++ 1 ++ [x]$

~~Num~~ $\Rightarrow \text{ill-typed}$

- (e) $\text{getLine} >>= \text{putStrLn}$

$IO()$

- (f) $\text{putStrLn} 42 >>= \text{putStrLn} 43$

$IO()$

- (g) $(,) "42"$

$a \rightarrow (\text{String}, a)$

- (h) $\text{reverse} \cdot \text{foldMap} \text{return}$

~~Monoid m, Foldable t~~ $\Rightarrow t a \rightarrow t(m a)$. -

- (i) $\lambda l \rightarrow [(x, y) \mid x < -1, y < -1, x / y]$

$(\forall a) \Rightarrow [a] \rightarrow [a, a]$

- (j) $\text{let } f x = x \text{ in } (f 'a', f \text{ True})$

$(\text{Char}, \text{Bool})$

- (k) $\text{filterM} (\text{const} [\text{True}, \text{False}])$

~~$[Bool] \rightarrow m[Bool]$~~

$a \rightarrow m a$.

$(a \rightarrow m \text{Bool}) \Rightarrow [a] \rightarrow m[a]$.

$a \rightarrow b \rightarrow a$.

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix, do syntax, list comprehensions, or any valid Haskell.

- (a) $\text{Int} \rightarrow \text{Int}$

Example answers:

$\lambda x \rightarrow x + 1$

(+1)

- (b) $\text{Bool} \rightarrow [\text{Bool}]$

Answer $\lambda n \rightarrow \text{if } n == \text{True} \text{ then } [n] \text{ else } [\text{False}]$.

- (c) $\text{a} \rightarrow \text{Maybe b}$

- (d) $(\text{Int} \rightarrow \text{Char} \rightarrow \text{Bool}) \rightarrow [\text{Int}] \rightarrow [\text{Char}] \rightarrow [\text{Bool}]$

Answer $\lambda l c \rightarrow \text{id} \circ (\text{head } l) (\text{head } c) = \text{True} \text{ then } [\text{True}] \text{ else } [\text{False}]$.

- (e) $(\text{a} \rightarrow \text{b} \rightarrow \text{c}) \rightarrow \text{IO a} \rightarrow \text{IO b} \rightarrow \text{IO c}$

- (f) $(\text{a} \rightarrow \text{b}) \rightarrow (\text{b} \rightarrow \text{Bool}) \rightarrow [\text{a}] \rightarrow [\text{b}]$

- (g) $\text{Maybe a} \rightarrow (\text{a} \rightarrow \text{Gen b}) \rightarrow \text{Gen (a,b)}$

- (h) $\text{Eq a} \Rightarrow \text{a} \rightarrow [\text{a}] \rightarrow [\text{a}]$

Answer $\lambda x \rightarrow \text{id} \circ (\text{head } x) \text{ then } x \text{ else } x \cdot x$

- (i) $\text{Show a} \Rightarrow [\text{a}] \rightarrow \text{IO String}$

- (j) $(\text{a}, \text{b}) \rightarrow (\text{a} \rightarrow \text{b} \rightarrow \text{c}) \rightarrow \text{c}$

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a)

```
foo :: [Int] -> [Int]  
foo l = [ x * x | x <- 1, x > 0 ]
```

Example answer:

Calculates the squares of all positive numbers in a list.

```
foo [] = []  
foo [1,0,2,-1] = [1,4]
```

(b)

```
foo :: [Int] -> [Pair]  
foo l = [ (x,y) | x <- 1, y <- 1, x /= y ]
```

Answer:

Values in int list, creates Pairs with ~~unusual~~ elements ~~other than~~ (from the same list).

~~foo [1,0]~~ = [(1,0), (0,1)] .

(c)

```
foo :: a -> [a] -> [a]  
foo x l = reverse (x : reverse l)
```

Answer:

`foo 3 [1,2]`

Picks an element to the front of a reversed list & then reverses the list .

(d)

```
bar :: a -> Maybe b -> [a] -> [b]  
bar f [] = []  
bar f (x:xs) =  
let rs = bar f xs in  
case f x of  
Nothing -> rs  
Just r -> r:rs
```

```
foo :: [Maybe a] -> [a]  
foo = bar id
```

Answer:

(e)

```
foo :: [Int] -> Int -> [Int] -> (Int, [Int])  
foo [] m = (m, [])  
foo [x] m = (x, [m])  
foo (x : xs) m = (max m' x, m' : xs')  
where (m', xs') = foo xs m
```

Answer:

~~foo [1,2] 3 = (2, [3])~~ ~~Choose~~

= (2, [1,3])

for

This function returns a pair - where the first element is the maximum of the current list (list that is passed to it).

↳ the record element of the pair is a list with the rest of the list and 2 rd parameter passed to the list .

(f) *Bonus!*

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM [] = return []
dropWhileM p (x:xs) = do
    q <- p x
    if q then dropWhileM p xs else return (x:xs)
```

```
foc :: ???
foc = dropWhileM (const [True, False])
```

Answer:

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

`weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]`

You can assume that the lists have the same length.

~~weave l t = reverse (weaveHelper l t)~~
weave l t = .reverse (weaveHelper l t)

```
weaveHelper l acc : (a) -> [a] -> [a]
weaveHelper [] acc = acc
weaveHelper (h1:t1) (h2:t2) acc = weaveHelper t1 t2 (h1:h2:acc)
```

- (b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

`toMax [1,4,2,5,3] = [5,5,5,5,5]`

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

```
toMax l = let len = length l in
    let (max, temp) = fold l 0 in
        foldl (\listBuild max len .
```

```
listBuild ele nix : 'Int -> 'Int -> ['Int]
```

```
listBuild _ 0 = []
```

```
listBuild ele nix = ele : (listBuild ele (nix - 1))
```

Typeclass Definitions

```
class Semigroup a where
  (++) :: a -> a -> a

class Semigroup m => Monoid m where
  mempty :: m

class Show a where
  show :: a -> String

class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool

class Eq a => Crd a where
  compare :: a -> a -> Ordering
  (<), (=<), (=>), (>) :: a -> a -> Bool
  max, min :: a -> a -> a

class Functor f where
  fmap :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure :: a -> f a
  ( <*> ) :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return :: a -> m a
  ( >> ) :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary :: Gen a
  shrink :: a -> [a]

class Nur a where
  (+), (-), (*) :: a -> a -> a
  negate :: a -> a
  abs :: a -> a
  signum :: a -> a
  fromInteger :: Integer -> a
```

CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
- (i) True
 (ii) False
- (b) The constraint `Semigroup a => Monoid a` implies that:
- (i) Every type that has a `Semigroup` instance, also has a `Monoid` instance.
 (ii) Every type that has a `Monoid` instance, also has a `Semigroup` instance.
 (iii) Both of the above.
 (iv) None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler.
- (i) True
 (ii) False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a `main` function:
- (i) The program will fail to typecheck.
 (ii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `Int` and `Char` to generate inputs and test `foo`.
 (iii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `()` as default to generate inputs and test `foo`.
 (iv) Haskell will require user-provided generators for integers and characters in order to run the tests

Part 2 - 12pts

The standard library defines `foldMap` with the following type:

```
foldMap :: (Monoid m, Foldable t) => (a -> m) -> t a -> m
```

For each of the following `foldMap` calls, select all options that are true:

- (a) `foldMap (:) [] [1..10]`
- (i) The expression will fail to typecheck.
 - (ii) The monoid in this call is `Int`.
 - (iii) The monoid in this call is `[Int]`.
 - (iv) The monoid in this call is `String`.
 - (v) The expression is equivalent to the identity function.
 - (vi) The foldable in this call is `[]` - the instance for lists.
- (b) `foldMap show "123456"`
- (i) The expression will fail to typecheck.
 - (ii) The monoid in this call is `Int`.
 - (iii) The monoid in this call is `[Int]`.
 - (iv) The monoid in this call is `String`.
 - (v) The expression is equivalent to the identity function.
 - (vi) The foldable in this call is `[]` - the instance for lists.

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or “ill-typed” if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

- (a) $\backslash x \rightarrow x$
Example answer:
 $a \rightarrow a$
- (b) $\backslash x y \rightarrow (x,y)$
 $a \rightarrow b \rightarrow (a,b)$
- (c) $\backslash x y \rightarrow \text{if } x == y \text{ then show } x \text{ else show } (x,y)$
Eq a => a #> a -> String
- (d) $\backslash x l \rightarrow x : l ++ l ++ [x]$
- $a \rightarrow [a] \rightarrow a$
- (e) `getLine >>= putStrLn`
 $\mathcal{T} O \epsilon$
- (f) `putStrLn "42" >>= putStrLn "43"`
 $!l \rightsquigarrow \text{type}$
- (g) `(,) "42"`
 $a \rightarrow (a, String)$
- (h) `reverse . foldl (\return .`
 $M o r e \ m \Rightarrow [a] \rightarrow [m \circ]$
- (i) $\backslash l \rightarrow [(x,y) \mid x < -1, y < -1, x /= y]$
Eq a => [a] -> [(a,a)]
- (j) `let f x = x in (f 'a', f True)`
Char, Bool
- (k) `filterM (const [True, False])`
~~ill typed~~ / ill typed

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as [], Nothing, or undefined) unless there is no other option. You can use any function from the appendix, do syntax, list comprehensions, or any valid Haskell.

- (b) $\text{Bool} \rightarrow [\text{Bool}]$
 $f\ s = [s \{ \text{true}\}]$

(c) $a \rightarrow \text{Maybe } b$

(d) $(\text{Int} \rightarrow \text{Char} \rightarrow \text{Bool}) \rightarrow [\text{Int}] \rightarrow [\text{Char}] \rightarrow [\text{Bool}]$

(e) $(a \rightarrow b \rightarrow c) \rightarrow \text{IO } a \rightarrow \text{IO } b \rightarrow \text{IO } c$

Z:ρ Write
list Mx

(f) $(a \rightarrow b) \rightarrow (b \rightarrow \text{Bool}) \rightarrow [a] \rightarrow [b]$
 ~~$f\ g\ h\ l s t = n o p\ g\ (f i l t e r\ h\ l s t)$~~
 $f\ g\ h\ l s t = f i l t e r\ h\ (n o p\ g\ l s t)$

(g) $\text{Maybe } a \rightarrow (a \rightarrow \text{Gen } b) \rightarrow \text{Gen } (a, b)$

$>>=$

(h) $\text{Eq } a \Rightarrow a \rightarrow [a] \rightarrow [a]$
 $f\ a\ l s t = f i l t e r\ (a ==) l s t$

(i) Show $a \Rightarrow [a] \rightarrow \text{IO String}$

return

$f\ (a, s)\ g = g\ a\ b$

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a) `foo :: [Int] -> [Int]`

`foo l = [x * x | x <- l, x > 0]`

Example answer:

Calculates the squares of all positive numbers in a list.

`foo [] = []`

`foo [1,0,2,-1] = [1, 4]`

(b) `foo :: [Int] -> [Int] [C1, C2, C3]`

`foo l = [(x,y) | x <- l, y <- l, x /= y]`

Example answer:

`foo 1 = [(x,y) | x <- 1, y <- 1, x /= y]`

Answer: `fooles` a list of `(x,y)` created a new list of all combinations of elements in the original list, so long as `x` and `y` aren't equal.

(c) `foo :: a -> [a]`

`foo x l = reverse (x : reverse l)`

Answer: `foo` reverses the first argument to the reversed second argument

`foo 3 [1,2] = [3, 2, 1]`

(d) `bar :: (a -> Maybe b) -> [a] -> [b]`

`bar f (x:xs) =`

`let rs = bar f xs in`

`case f x of`

`Nothing -> rs`

`Just r -> r:rs`

`foo :: [Maybe a] -> [a]`

`foo = bar id`

Answer: `foo` takes a list of `Nothing`'s, removes all `Nothing`'s and returns a list of all values inside `Just`'s.

`foo [Just 2, Just 3] = [2, 3]`

(e) `foo :: [Int] -> Int -> (Int, [Int])`

`foo [] m = (m, [])`

`foo [x] m = (x, [m])`

`foo (x : xs) m = (max m' x, m : xs')`

`where (m', xs') = foo xs m`

Answer: `foo` takes a list of ints and an int and returns tuple of form (`max` value of list, list of second value repeated (length list) times)

`foo [] 3 = (3, [])`

`foo [1,2] 3 = (3, [3, 3])`

Example for 15:

`foo [1, 1, 2] = [C1, C2]`

`foo [1, 2, 3] = [C1, C2, C3]`

`C1, C2, C3`

(f) *Bonus!*

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM _ [] = return []
dropWhileM p (x:xs) = do
    q <- p x
    if q then dropWhileM p xs else return (x:xs)

foo :: ???
foo = dropWhileM (const [True, False])
```

Answer:

Drops all elements that satisfy the predicate.

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

weave [$1, 2, 3$] [$4, 5, 6$] = [$1, 4, 2, 5, 3, 6$]

we have $\{ \} \{ \} = \{ 3 \}$

$$w_{\text{ref}}(x:y_1:y_2) = x:y:(w_{\text{ref}}\,x\,y_1\,y_2)$$

You can assume that the lists have the same length.

(b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

```
toMax [1,4,2,5,3] = [5,5,5,5,5]
```

BONUS: Implement `toMax` so that it only traverses a list.

to Max [] = []
to Max list = let len = length list in
replicate len m
Bunny version: to Max [] = []

to max left

left arr (= foldl (\acc x => if x > (fst acc) then (x, acc) else acc))

C 473 + 0

(二)

Typeclass Definitions

```
class Semigroup a where
  (<>) :: a -> a -> a

class Semigroup m => Monoid m where
  mempty :: m

class Show a where
  show :: a -> String

class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool

class Eq a => Ord a where
  compare :: a -> a -> Ordering
  (<), (=<), (=>), (>) :: a -> a -> Bool
  max, min :: a -> a -> a

class Functor f where
  fmap :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure :: a -> f a
  (*)> :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return :: a -> m a
  (=>) :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary :: Gen a
  shrink :: a -> [a]

class Num a where
  (+), (-), (*) :: a -> a -> a
  negate :: a -> a
  abs :: a -> a
  signum :: a -> a
  fromInteger :: Integer -> a
```

CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
- (i) True
 (ii) False
- (b) The constraint `Semigroup a => Monoid a` implies that:
- (i) Every type that has a `Semigroup` instance, also has a `Monoid` instance.
 (ii) Every type that has a `Monoid` instance, also has a `Semigroup` instance.
 (iii) Both of the above.
 (iv) None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler.
- (i) True
 (ii) False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a main function:
- (i) The program will fail to typecheck.
 (ii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `Int` and `Char` to generate inputs and test `foo`.
 (iii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `()` as default to generate inputs and test `foo`.
 (iv) Haskell will require user-provided generators for integers and characters in order to run the tests

Part 2 - 12pts

The standard library defines `foldMap` with the following type:

```
foldMap :: (Monoid m, Foldable t) => (a -> m) -> t a -> m
```

For each of the following `foldMap` calls, select all options that are true:

(a) `foldMap (:) [] [-..10]`

(i) The expression will fail to typecheck.

(ii) The monoid in this call is `Int`.

(iii) The monoid in this call is `[Int]`.

(iv) The monoid in this call is `String`.

(v) The expression is equivalent to the identity function.

(vi) The foldable in this call is `[]` - the instance for lists.

(b) `foldMap show "123456"`

(i) The expression will fail to typecheck.

(ii) The monoid in this call is `Int`.

(iii) The monoid in this call is `[Int]`.

(iv) The monoid in this call is `String`.

(v) The expression is equivalent to the identity function.

(vi) The foldable in this call is `[]` - the instance for lists.

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or “ill-typed” if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

(a) $\backslash x \rightarrow x$

Example answer:

$a \rightarrow a$

(b) $\backslash x y \rightarrow (x,y)$

$a \rightarrow b \rightarrow (a,b)$

(c) $\backslash x y \rightarrow \text{if } x == y \text{ then show } x \text{ else show } (x,y)$

$\text{Eq } a, \text{ show } a = a \rightarrow a \rightarrow \text{String}$

(d) $\backslash x \rightarrow x : 1 ++ 1 ++ [x]$

$a \rightarrow [a] \rightarrow [a]$

(e) $\text{getLine} >>= \text{putStrLn}$

$\text{IO } \text{String} \rightarrow \text{IO ()}$

(f) $\text{putStrLn "42"} >>= \text{putStrLn "43"}$

$\text{IO ()} \rightarrow \text{IO ()}$

(g) $(,) "42"$

$a \rightarrow (\text{String}, a)$

(h) $\text{reverse} \cdot \text{foldMap} \text{return}$

$[a] \rightarrow [a]$

(i) $\backslash l \rightarrow [(x,y) \mid x <- l, y <- l, x /= y]$

$\text{Eq } a \Rightarrow [a] \rightarrow [(a,a)]$

(j) $\text{let } f x = x \text{ in } (f `a` f \text{ True})$

$(\text{Char}, \text{Bool})$

(k) $\text{filterM} (\text{const} [\text{True}, \text{False}])$

$[a] \rightarrow [[a]]$

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix, do syntax, list comprehensions, or any valid Haskell.

- (a) $\text{Int} \rightarrow \text{Int}$

Example answers:

$$\lambda x \rightarrow x + 1$$

(+1)

- (b) $\text{Bool} \rightarrow [\text{Bool}]$

$$\lambda x \rightarrow [x \wedge x, x \vee x]$$

- (c) $\text{a} \rightarrow \text{Maybe b}$

$$\lambda x \rightarrow \text{Nothing}$$

- (d) $(\text{Int} \rightarrow \text{Char} \rightarrow \text{Bool}) \rightarrow [\text{Int}] \rightarrow [\text{Char}] \rightarrow [\text{Bool}]$

$$\lambda f(x:xs) (y:ys) \rightarrow \text{replicate } x (y \cdot c' \equiv z')$$

- (e) $(\text{a} \rightarrow \text{b} \rightarrow \text{c}) \rightarrow \text{IO a} \rightarrow \text{IO b} \rightarrow \text{IO c}$

- (f) $(\text{a} \rightarrow \text{b}) \rightarrow (\text{b} \rightarrow \text{Bool}) \rightarrow [\text{a}] \rightarrow [\text{b}]$

$$\lambda f g xs \rightarrow [y | y \leftarrow f xs, \text{not}(g y)]$$

- (g) $\text{Maybe a} \rightarrow (\text{a} \rightarrow \text{Gen b}) \rightarrow \text{Gen (a,b)}$

- (h) $\text{Eq a} \Rightarrow \text{a} \rightarrow [\text{a}] \rightarrow [\text{a}]$

$$\lambda x ys \rightarrow \text{map } (\lambda y \rightarrow \text{if } x == y \text{ then } x \text{ else } y) ys$$

- (i) $\text{Show a} \Rightarrow [\text{a}] \rightarrow \text{IO String}$

$$\lambda (x:xs) \rightarrow \text{putStrLn } (\text{show } x)$$

- (j) $(\text{a}, \text{b}) \rightarrow (\text{a} \rightarrow \text{b} \rightarrow \text{c}) \rightarrow \text{c}$

$$\lambda (x,y) f \rightarrow f x y$$

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a) `foo :: [Int] -> [Int]`

`foo 1 = [x * x | x <- 1, x > 0]`

Example answer:

Calculates the squares of all positive numbers in a list.

`foo [] = []`

`foo [1,0,2,-1] = [1, 4]`

(b) `foo :: [Int] -> [Int]`

`foo 1 = [(x,y) | x <- 1, y <- 1, x /= y]`

Answer:

`foo [] -> []`

(c) `foo :: a -> [a] -> [a]`

`foo x 1 = reverse (x : reverse 1)`

Answer: adds `x` to the end of `list`

`foo s [] = [s]`

`foo 5 [1,2,3,4] = [1,2,3,4,5]`

(d) `bar :: (a -> Maybe b) -> [a] -> [b]`

`bar f [] = []`

`let rs = bar f xs in`

`case f x of`

`Nothing -> rs`

`Just r -> r:rs`

`foo :: [Maybe a] -> [a]`

`foo = bar id`

Answer: takes in a list of maybes and removes the maybe, returning the elements

`foo [] = []`

(e) `foo :: [Int] -> Int -> (Int, [Int])`

`foo [] m = (m, [])`

`foo [x] m = (x, [m])`

`foo (x : xs) m = (max m' x, m : xs')`

where `(m', xs') = foo xs m`

Answer: finds the max of a list and return it along with the remain from the list

`foo [] s = (s, [])`

`foo [1] s = (1, [s])`

`foo [1,2,7] s = (7`

(f) *Bonus!*

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM _ [] = return []
dropWhileM p (x:xs) = do
    q <- p x
    if q then dropWhileM p xs else return (x:xs)
foo :: ???
foo = dropWhileM (const [True, False])
```

Answer:

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

```
weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]
```

You can assume that the lists have the same length.

```
weave :: [a] -> [a] -> [a]
weave [] [] = []
weave (x:xs) (y:ys) = x : (y : (weave xs ys)))
```

- (b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

```
toMax [1,4,2,5,3] = [5,5,5,5,5]
```

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

```
toMax :: Ord a => [a] -> [a]
toMax [] = []
toMax [x:xs] = max x xs > toMax xs
toMax (x:xs) = max x (toMax xs)
toMax (m, l) = replicate m m
```

```
_ -> []
```

```
findmax :: Ord a => a -> [a] -> (a, Int)
findmax m [] = (m, 0)
findmax m (x:xs) = 
  | x > m = findmax x xs (l+1)
  | otherwise = findmax m xs (l+1)
```

Typeclass Definitions

```
class Semigroup a where
  (++) :: a -> a -> a

class Semigroup m => Monoid m where
  mempty :: m

class Show a where
  show :: a -> String

class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool

class Eq a => Ord a where
  compare :: a -> a -> Ordering
  (<), (=<), (>=), (>) :: a -> a -> Bool
  max, min :: a -> a -> a

class Functor f where
  fmap :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure :: a -> f a
  (*>) :: f a -> b) -> f a -> f b

class Applicative m => Monad m where
  return :: a -> m a
  (=>) :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary :: Gen a
  shrink :: a -> [a]

class Num a where
  (+), (-), (*) :: a -> a -> a
  negate :: a -> a
  abs :: a -> a
  signum :: a -> a
  fromInteger :: Integer -> a
```

CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
- (i) True
 - (ii) False
- (b) The constraint `Semigroup a => Monoid a` implies that:
- (i) Every type that has a `Semigroup` instance, also has a `Monoid` instance.
 - (ii) Every type that has a `Monoid` instance, also has a `Semigroup` instance.
 - (iii) Both of the above.
 - (iv) None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler.
- (i) True
 - (ii) False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a `main` function:
- (i) The program will fail to typecheck.
 - (ii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `Int` and `Char` to generate inputs and test `foo`.
 - (iii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `()` as default to generate inputs and test `foo`.
 - (iv) Haskell will require user-provided generators for integers and characters in order to run the tests

Part 2 - 12pts

The standard library defines `foldMap` with the following type:

```
foldMap :: (Monoid m, Foldable t) => (a -> m) -> t a -> m
```

For each of the following `foldMap` calls, select all options that are true:

- (a) `foldMap (:) [1..10]`
- (i) The expression will fail to typecheck.
 - (ii) The monoid in this call is `Int`.
 - (iii) The monoid in this call is `[Int]`.
 - (iv) The monoid in this call is `String`.
 - (v) The expression is equivalent to the identity function.
 - (vi) The foldable in this call is `[]` - the instance for lists.
- (b) `foldMap show "123456"`
- (i) The expression will fail to typecheck.
 - (ii) The monoid in this call is `Int`.
 - (iii) The monoid in this call is `[Int]`.
 - (iv) The monoid in this call is `String`.
 - (v) The expression is equivalent to the identity function.
 - (vi) The foldable in this call is `[]` - the instance for lists.

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or “ill-typed” if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

(a) $\backslash x \rightarrow x$

Example answer:

$a \rightarrow a$

(b) $\backslash x y \rightarrow (x,y)$

$a \rightarrow b \rightarrow (a, b)$

(c) $\backslash x y \rightarrow \text{if } x == y \text{ then show } x \text{ else show } (x,y)$

$\text{Eq } a \Rightarrow a \rightarrow a \rightarrow \text{String}$

(d) $\backslash x \rightarrow x : 1 \uparrow\uparrow 1 \uparrow\uparrow [x]$

$a \rightarrow [a] \rightarrow [a]$

(e) $\text{getLine} >>= \text{putStrLn}$

IO ()

(f) $\text{putStrLn "42"} >>= \text{putStrLn "43"}$

IO String

(g) $() \rightarrow "42"$

$a \rightarrow (\text{String}, a)$

(h) $\text{reverse} \cdot \text{foldMap return}$

$[a] \mapsto [a]$

(i) $\backslash l \rightarrow [(x,y) \mid x <- 1, y <- 1, x / = y]$

$\text{Eq } a \Rightarrow [a] \rightarrow [(a, a)]$

(j) $\text{let } f x = x \text{ in } (f 'a', f \text{ True})$

Char, Bool

(k) $\text{filterM} (\text{const} [\text{True}, \text{False}])$

$[a] \mapsto [a]$

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix, do syntax, list comprehensions, or any valid Haskell.

- (a) $\text{Int} \rightarrow \text{Int}$

Example answers:

$\lambda x \rightarrow x + 1$

(+1)

- (b) $\text{Bool} \rightarrow [\text{Bool}]$
 $\lambda x \rightarrow [not\;x]$

- (c) $a \rightarrow \text{Maybe}\;b$

$\lambda x \rightarrow Nothing$

- (d) $(\text{Int} \rightarrow \text{Char} \rightarrow \text{Bool}) \rightarrow [\text{Int}] \rightarrow [\text{Char}] \rightarrow [\text{Bool}]$

listM2

- (e) $(a \rightarrow b \rightarrow c) \rightarrow IO\;a \rightarrow IO\;b \rightarrow IO\;c$

listM2

- (f) $(a \rightarrow b) \rightarrow (b \rightarrow \text{Bool}) \rightarrow [a] \rightarrow [b]$

$\lambda f\;g\;\lambda x\;f\;g\;(\text{filter}\;g\;(\text{map}\;f\;x))$

- (g) $\text{Maybe}\;a \rightarrow (a \rightarrow \text{Gen}\;b) \rightarrow \text{Gen}\;(a,b)$

$\lambda x\;f\;\lambda y\;f\;(\text{map}\;f\;(\text{mkList}\;x)) \Rightarrow (\lambda y \rightarrow$

- (h) $\text{Eq}\;a \Rightarrow a \rightarrow [a] \rightarrow [a]$

$\lambda x\;f\;\lambda y\;f\;(\text{mkList}\;x) \Rightarrow (\lambda y \rightarrow$

- (i) Show $a \Rightarrow [a] \rightarrow IO\;\text{String}$

$\lambda x \rightarrow \rho \leftarrow \text{String}\;x \gg getLine$

- (j) $(a,b) \rightarrow (a \rightarrow b \rightarrow c) \rightarrow c$

$\lambda (x,y)\;f\;\rightarrow f\;x\;y$

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a) `foo :: [Int] -> [Int]`

`foo 1 = [x * x | x <- 1, x > 0]`

Example answer:

Calculates the squares of all positive numbers in a list.

`foo [] = []`

`foo [1,0,2,-1] = [1, 4]`

(b) `foo :: [Int] -> [Int]`

`foo 1 = [(x,y) | x <- 1, y <- 1, x /= y]`

Answer: Swap pairs of consecutive elements

`foo [1, 0, 0, 1] = [(1, 0), (0, 1)]`

(c) `foo :: a -> [a] -> [a]`

`foo x l = reverse (x : reverse l)`

Answer: (flip id) X to end of l

`foo 4 [1,2,3] = [1,2,3,4]`

(d) `bar :: (a -> Maybe b) -> [a] -> [b]`

`bar [] = []`

`bar f (x:xs) =`

`let rs = bar f xs in`

`case f x of`

`Nothing -> rs`

`Just r -> r:rs`

`foo :: [Maybe a] -> [a]`

`foo = bar id`

Answer: removes Nones from list of Maybes and returns elements in Just,

`foo [Just 1, Nothing, Just 2, Just 3] = [1,2,3]`

(e) `foo :: [Int] -> Int -> (Int, [Int])`

`foo [] m = (m, [])`

`foo [x] m = (x, [m])`

`foo (x : xs) m = (max m' x, m : xs')`

`where (m', xs') = foo xs m`

Answer: tuple of max of list 1:3:2, 6 → (3, 4:4:4)

1:3:2 and list of m of length 3:2, 6 → (3, 4:4:4)

at first list

`foo [1, 2] 5 = (3, [1, 5])`

`foo [1, 3, 2] 2 = (3, [1, 3, 2, 2])`

(f) *Bonus!*

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM = []
dropWhileM p (x:xs) = do
    q <- p x
    if q then dropWhileM p xs else return (x:xs)
```

```
foo :: ??
```

```
foo = dropWhileM (const [True, False])
```

Answer:

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

```
weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]
```

You can assume that the lists have the same length.

```
w weave :: [a] -> [a] -> [a]
weave [] [] = []
weave (x:xs) (y:ys) = x:y:(weave xs ys)
```

- (b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

```
toMax [1,4,2,5,3] = [5,5,5,5,5]
```

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

```
+> toMax [] = []
+> toMax (x:xs) = replicate (length x) (maximum x)
```

Typeclass Definitions

```
class Semigroup a where
  (<>)
    :: a -> a -> a

class Semigroup m => Monoid m where
  mempty
    :: m

class Show a where
  show
    :: a -> String

class Eq a where
  (==)
    :: a -> a -> Bool
  (/=)
    :: a -> a -> Bool

class Eq a => Ord a where
  compare
    :: a -> a -> Ordering
  (<), (<=), (>=), (>)
    :: a -> a -> Bool
  max, min
    :: a -> a -> a

class Functor f where
  fmap
    :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure
    :: a -> f a
  (*>)
    :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return
    :: a -> m a
  (=>)
    :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap
    :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary
    :: Gen a
  shrink
    :: a -> [a]

class Num a where
  (+), (-), (*)
    :: a -> a -> a
  negate
    :: a -> a
  abs
    :: a -> a
  signum
    :: a -> a
  fromInteger
    :: Integer -> a
```

Chris Jose

CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
- (i) True
 (ii) False
- (b) The constraint `Semigroup a => Monoid a` implies that:
- (i) Every type that has a `Semigroup` instance, also has a `Monoid` instance.
 (ii) Every type that has a `Monoid` instance, also has a `Semigroup` instance.
 (iii) Both of the above.
 (iv) None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler.
- (i) True
 (ii) False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a `main` function:
- (i) The program will fail to typecheck.
 (ii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `Int` and `Char` to generate inputs and test `foo`.
 (iii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `()` as default to generate inputs and test `foo`.
 (iv) Haskell will require user-provided generators for integers and characters in order to run the tests

Part 2 - 12pts

The standard library defines `foldMap` with the following type:

`foldMap :: (Monoid m, Foldable t) => (a -> m) -> t a -> m`

For each of the following `foldMap` calls, select all options that are true:

(a) `foldMap (:) [] [1..10]`

- (i) The expression will fail to typecheck.
- (ii) The monoid in this call is Int.
- (iii) The monoid in this call is [Int].
- (iv) The monoid in this call is String.
- (v) The expression is equivalent to the identity function.
- (vi) The foldable in this call is [] - the instance for lists.

(b) `foldMap show "123456"`

- (i) The expression will fail to typecheck.
- (ii) The monoid in this call is Int.
- (iii) The monoid in this call is [Int].
- (iv) The monoid in this call is String.
- (v) The expression is equivalent to the identity function.
- (vi) The foldable in this call is [] - the instance for lists.

$>> = m \circ \rightarrow (a \rightarrow m b) \rightarrow m b$

$\text{IO string} \rightarrow \text{Set}$

Question 2 (20 points) $\text{IO string} \rightarrow (\text{String} \rightarrow \text{IO}$

For each of the Haskell expressions below, write their (most general) Haskell type or “ill-typed” if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

(a) $\lambda x \rightarrow x$

Example answer:

$a \rightarrow a$

(b) $\lambda x y \rightarrow (x, y)$

(c) $\lambda x y \rightarrow \text{if } x == y \text{ then show } x \text{ else show } (x, y)$

$a \rightarrow b \rightarrow (a, b)$

(d) $\lambda x \ 1 \rightarrow x : 1 \quad 1 \rightarrow [x]$

$a \rightarrow [a] \rightarrow [a]$

(e) $\text{getLine} >>= \text{putStrLn}$

$\text{IO String} \rightarrow (\text{String} \rightarrow \text{IO ()}) \rightarrow \text{IO ()}$

(f) $\text{putStrLn "42"} >>= \text{putStrLn "43"}$

$\text{IO String} \rightarrow (\text{String} \rightarrow \text{IO String}) \rightarrow \text{IO String}$

(g) $(.) "42"$

(h) $\text{reverse} \circ \text{foldMap} \text{return}$

$\text{Monad} \Rightarrow [a] \rightarrow [\text{IO a}]$

(i) $\lambda l \rightarrow [(x, y) \mid x <- l, y <- l, x /= y]$

$[a] \rightarrow [(\text{IO a}, \text{IO a})]$

(j) $\text{let } f x = x \text{ in } (f 'a', f \text{ True})$

ill typed

(k) $\text{filterM} (\text{const} [\text{True}, \text{False}])$

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix, do syntax, list comprehensions, or any valid Haskell.

(a) $\text{Int} \rightarrow \text{Int}$

Example answers:

$\lambda x \rightarrow x + 1$

(+1)

(b) $\text{Bool} \rightarrow [\text{Bool}]$

$f x = (x \parallel \text{False}) : []$

(c) $a \rightarrow \text{Maybe } b$

$\lambda x \rightarrow \text{pure } x >> \text{Maybe}$

(d) $(\text{Int} \rightarrow \text{Char} \rightarrow \text{Bool}) \rightarrow [\text{Int}] \rightarrow [\text{Char}] \rightarrow [\text{Bool}]$

$f m1 m2 = (\lambda f ((\text{head } m1) + 1) (\text{read } m2) : [(\text{a})]) : []$

(e) $(a \rightarrow b \rightarrow c) \rightarrow \text{IO } a \rightarrow \text{IO } b \rightarrow \text{IO } c$

liftm2

(f) $(a \rightarrow b) \rightarrow (b \rightarrow \text{Bool}) \rightarrow [a] \rightarrow [b]$

$\lambda f g \text{ lst} \rightarrow g f (\text{head } \text{lst}) : []$

(g) $\text{Maybe } a \rightarrow (a \rightarrow \text{Gen } b) \rightarrow \text{Gen } (a, b)$

$\lambda x \rightarrow \text{Gen } b$

(h) $\text{Eq } a \Rightarrow a \rightarrow [a] \rightarrow [a]$

$\lambda x m1 \rightarrow \text{intersperse } x m1$

(i) $\text{Show } a \Rightarrow [a] \rightarrow \text{IO String}$

$\lambda x \rightarrow (\text{head } x) ++ \text{getline}$

(j) $(a, b) \rightarrow (a \rightarrow b \rightarrow c) \rightarrow c$

$\lambda tup \ell \rightarrow f (\text{fst } \text{tup}) (\text{snd } \text{tup})$

$\lambda f m1 m2 \rightarrow [f (x + 1) | x \in m1, y \in m2]$

10 [1,2,3]
10 [3,2,1]

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a) `foo :: [Int] -> [Int]`

`foo l = [x * x | x <- l, x > 0]`

Example answer:

Calculates the squares of all positive numbers in a list.

`foo [] = []`

`foo [1,0,2,-1] = [1, 4]`

(b) `foo :: [Int] -> [Int]`

`foo l = [(x,y) | x <- l, y <- l, x /= y]`

Example answer:

Return a list of tuples of pairs of elements of each tuple are different. $\text{foo } [1,2,2] = [(1,2), (1,3), (2,3)]$

(c) `foo :: a -> [a] -> [a]`

`foo x l = reverse (x : reverse l)`

Answer:

Returns the original list along with element x appended to the end of the list.

$\text{foo } [1,2,3] = [1,2,3,10]$; $\text{foo } [10] = [10]$

(d) `bar :: (a -> Maybe b) -> [a] -> [b]`

`bar f [] = []`

`bar f (x:xs) =`

`let rs = bar f xs in`

`case f x of`

`Nothing -> rs`

`Just r -> r:rs`

`foo :: [Maybe a] -> [a]`

`foo = bar id`

Answer:

(e) `foo :: [Int] -> Int -> (Int, [Int])`

`foo [] m = (m, [])`

`foo [x] m = (x, [m])`

`foo (x : xs) m = (max m' x, m : xs')`

`where (m', xs') = foo xs m`

Answer:

$\text{foo } [3,2,1] \ 6 = (3, [6,6,6])$

Returns a $(\text{Int}, [\text{Int}])$, where the 1st element of tuple is the max element of input list and 2nd element is a list of the 2nd arg with the same length as input list.

$\text{foo } [3,2,1] \ 6 = (3, [6,6,6])$

(f) Bonus!

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM _ [] = return []
dropWhileM p (x:xs) = do
    q <- p x
    if q then dropWhileM p xs else return (x:xs)
foo :: ???
foo = dropWhileM (const [True, False])
```

Answer:

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

```
weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]
```

You can assume that the lists have the same length.

```
weave [] [] = []
weave [] b = b.
weave a [] = a.
weave xs@(x:xs') ys@(y:ys') =
    x:y:weave xs' ys.
```

- (b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length,

where each element has been replaced by the maximum element of the list. For example:

```
toMax [1,4,2,5,3] = [5,5,5,5,5]
```

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

```
toMax lst = let max = (fst $ foo lst) 0) in
            lst & map (\x -> max) lst
```

→ get Gen b.

Typeclass Definitions

```

class Semigroup a where
  (<>) :: a -> a -> a

class Semigroup m => Monoid m where
  mempty :: m

class Show a where
  show :: a -> String

class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool

class Eq a => Ord a where
  compare :: a -> a -> Ordering
  ((<)), ((<=)), (=>), (>) :: a -> a -> Bool
  max, min :: a -> a -> a

class Functor f where
  fmap :: (a -> b) -> f a -> f b

class Applicative f => Applicative f where
  pure :: a -> f a
  ( <* >) :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return :: a -> m a
  (">>=) :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary :: Gen a
  shrink :: a -> [a]

class Num a where
  (+), (-), (*) :: a -> a -> a
  negate :: a -> a
  abs :: a -> a
  signum :: a -> a
  fromInteger :: Integer -> a

```

$\alpha \rightarrow \text{m} \alpha$

$3 : \mathbb{Z}, 1 \] 6 = (\max m, 3), 6 : xs$

$\text{foo} [\mathbb{Z}, 1 \] 6$

$(\max m, 2), 6 : xs$

$\text{foo} [\mathbb{I}] 6 = (1, [6])$

Samuel Howard
115960176

CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
- True
 - False
- (b) The constraint `Semigroup a => Monoid a` implies that:
- Every type that has a `Semigroup` instance, also has a `Monoid` instance.
 - Every type that has a `Monoid` instance, also has a `Semigroup` instance.
 - Both of the above.
 - None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler.
- True
 - False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a `main` function:
- The program will fail to typecheck.
 - After typeclass resolution, the resulting program will use the Arbitrary instance for `Int` and `Char` to generate inputs and test `foo`.
 - After typeclass resolution, the resulting program will use the `Arbitrary` instance for `()` as default to generate inputs and test `foo`.
 - Haskell will require user-provided generators for integers and characters in order to run the tests

Part 2 - 12pts

The standard library defines `foldMap` with the following type:

```
foldMap :: (Monoid m, Foldable t) => (a -> m) -> t a -> m
```

For each of the following `foldMap` calls, select all options that are true.

- (a) `foldMap (:) [] [1..10]`
- (i) The expression will fail to typecheck.
 - (ii) The monoid in this call is `Int`.
 - (iii) The monoid in this call is `[Int]`.
 - (iv) The monoid in this call is `String`.
 - (v) The expression is equivalent to the identity function.
 - (vi) The foldable in this call is `[]` - the instance for `lists`.
- (b) `foldMap show "123456"`
- (i) The expression will fail to typecheck.
 - (ii) The monoid in this call is `Int`.
 - (iii) The monoid in this call is `[Int]`.
 - (iv) The monoid in this call is `String`.
 - (v) The expression is equivalent to the identity function.
 - (vi) The foldable in this call is `[]` - the instance for `lists`.

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or “ill-typed” if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

(a) $\backslash x \rightarrow x$

Example answer:

$a \rightarrow a$

(b) $\backslash x y \rightarrow (x,y)$

$a \rightarrow b \rightarrow (a,b)$

(c) $\backslash x y \rightarrow \text{if } x == y \text{ then show } x \text{ else show } (x,y)$

$Eq a \Rightarrow a \rightarrow a \rightarrow String$

(d) $\backslash x 1 \rightarrow x : 1 ++ 1 ++ [x]$

$a \rightarrow [a] \rightarrow [a]$

(e) $\text{getLine} >>= putStrLn$

\Box

(f) $\text{putStrLn} 42 >>= \text{putStrLn} 43$

\Box

(g) $\lambda () \text{ ``42''}$

$a \rightarrow (String, a)$

(h) $\text{reverse}, \text{foldMap}, \text{return}$

$Foldable f \Rightarrow f a \rightarrow [a]$

(i) $\backslash 1 \rightarrow [(x,y) | x <- 1, y <- 1, x /= y]$

$Ell a \Rightarrow [a] \rightarrow [(a,a)]$

(j) $\text{let } f x = x \text{ in } (f `a` f, \text{True})$

$(Char, Bool)$

(k) $\text{filterM} (\text{const} [\text{True}, \text{False}])$

$\text{Monad } m \Rightarrow [a] \rightarrow m [a]$

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix, do syntax, list comprehensions, or any valid Haskell.

- (a) $\text{Int} \rightarrow \text{Int}$

Example answers:

$$\lambda x \rightarrow x + 1$$

(+1)

- (b) $\text{Bool} \rightarrow [\text{Bool}]$

$$\lambda x \rightarrow \text{if } x \text{ then } [x] \text{ else } [x, x]$$

- (c) $a \rightarrow \text{Maybe } b$

Undefined

- (d) $(\text{Int} \rightarrow \text{Char} \rightarrow \text{Bool}) \rightarrow [\text{Int}] \rightarrow [\text{Char}] \rightarrow [\text{Bool}]$

$$\lambda f \; l; l c \rightarrow \text{map } ((\lambda (a, b) \rightarrow f a b) \; (zip \; l; l))$$

- (e) $(a \rightarrow b \rightarrow c) \rightarrow \text{IO } a \rightarrow \text{IO } b \rightarrow \text{IO } c$

~~$$\lambda f \; a \rightarrow f a$$~~

- (f) $(a \rightarrow b) \rightarrow (b \rightarrow \text{Bool}) \rightarrow [a] \rightarrow [b]$

$$\lambda f_a \; f_b \; l a \rightarrow \text{filter } (\lambda a \rightarrow f_b (f_a a)) \; l a$$

- (g) $\text{Maybe } a \rightarrow (a \rightarrow \text{Gen } b) \rightarrow \text{Gen } (a, b)$

~~$$\lambda f \; a \rightarrow f a$$~~

- (h) $\text{Eq } a \Rightarrow a \rightarrow [a] \rightarrow [a]$

$$\lambda a \; l a \rightarrow \text{filter } (\lambda b \rightarrow a == b) \; l a$$

- (i) $\text{Show } a \Rightarrow [a] \rightarrow \text{IO String}$

$$\lambda L \rightarrow \text{map } \text{putStrLn } L$$

- (j) $(a, b) \rightarrow (a \rightarrow b \rightarrow c) \rightarrow c$

$$\lambda (a, b) \; f \rightarrow (f^a \; b)$$

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a) `foo :: [Int] -> [Int]`

`foo l = [x * x | x <- l, x > 0]`

Example answer:

Calculates the squares of all positive numbers in a list.

`foo [] = []`

`foo [1,0,2,-1] = [1, 4]`

(b) `foo :: [Int] -> [Int]`

`foo l = [(x,y) | x <- l, y <- l, x /= y]`

Answer:

Returns all pairs of ints in a list that are not equal

`foo [] = []`

`foo [1,2,3] = [(1,2), (1,3), (2,1), (2,3)]`

`foo [1,2,3,4] = [(1,2), (1,3), (1,4), (2,3), (2,4), (3,1), (3,2), (3,4), (4,1), (4,2), (4,3)]`

`foo x l = reverse (x : reverse l)`

Answer:

Appends X to the end of L

`foo l [7,8,9] = [7,8,9,l]`

`foo 'a' [] = ['a']`

`bar :: (a -> Maybe b) -> [a] -> [b]`

`bar [] = []`

`bar f (x:xs) = f x : bar xs`

`let rs = bar f xs in`

`case f x of`

`Nothing -> rs`

`Just r -> r:rs`

`foo :: [Maybe a] -> [a]`

`foo = bar id`

Answer:

Removes all 'Nothings' from a list of 'Maysbes'
`foo [Nothing, Maybe 1, Maybe 2, Nothing] = [Maybe 1, Maybe 2]`

`foo [Nothing] = []`

`foo :: [Int] -> Int -> (Int, [Int])`

`foo [] m = (m, [])`

`foo [x] m = (x, [m])`

`foo (x : xs) m = (max m' x, m : xs')`

`where (m', xs') = foo xs m`

Answer:

Returns a pair of the max element of a list and a list with m repeated n times where n is the length of the first argument.

Or returns second arg paired with empty list if argument list is empty

(f) Bonus!

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM = []
dropWhileM p (x:xs) = do
    q <- p x
    if q then dropWhileM p xs else return (x:xs)
```

```
foo :: ??  
foo = dropWhileM (const [True, False])
```

Answer:

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

```
weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]
```

You can assume that the lists have the same length.

```
weave :: [a] → [a] → [a]
```

```
weave [] [] = []
weave (x:xs) (y:ys) = x:y:(weave xs ys)
```

-- for invalid cases:

`weave` -- = [] -- Not possible with assumption

- (b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

```
toMax [1,4,2,5,3] = [5,5,5,5,5]
```

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

```
+toMax :: [Int] → [Int]
```

```
+toMax [] = [] -- Not possible with assumption
```

```
+toMax (x:xs) = a
```

where (l,a) = foo (x:xs) b

where (b,_) = foo (x:xs) 0

Typeclass Definitions

```
class Semigroup a where
  (++) :: a -> a -> a

class Semigroup m => Monoid m where
  mempty :: m

class Show a where
  show :: a -> String

class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool

class Eq a => Ord a where
  compare :: a -> a -> Ordering
  (<), (<=), (>=), (>) :: a -> a -> Bool
  max, min :: a -> a -> a

class Functor f where
  fmap :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure :: a -> f a
  (*>) :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return :: a -> m a
  (=>) :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary :: Gen a
  shrink :: a -> [a]

class Num a where
  (+), (-), (*) :: a -> a -> a
  negate :: a -> a
  abs :: a -> a
  signum :: a -> a
  fromInteger :: Integer -> a
```

CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
laziness? Is OCaml lazy?
- (i) True
 (ii) False
- (b) The constraint `Semigroup a => Monoid a` implies that:
- (i) Every type that has a Semigroup instance, also has a Monoid instance.
 (ii) Every type that has a Monoid instance, also has a Semigroup instance.
 (iii) Both of the above.
 (iv) None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler.
- (i) True
 (ii) False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a main function:
- (i) The program will fail to typecheck.
 (ii) After typeclass resolution, the resulting program will use the Arbitrary instance for Int and Char to generate inputs and test `foo`.
 (iii) After typeclass resolution, the resulting program will use the Arbitrary instance for () as default to generate inputs and test `foo`.
 (iv) Haskell will require user-provided generators for integers and characters in order to run the tests

[7] W

The standard library defines `foldMap` with the following type:

$$\text{foldMap} :: (\text{Monoid m}, \text{Foldable t}) \Rightarrow ((a \rightarrow m) \rightarrow (t \rightarrow m)) \rightarrow [a] \rightarrow m$$

For each of the following `foldMap` calls, select all options that are true:

(a) `foldMap (:) [] [1..10]`

- (i) The expression will fail to typecheck.
- (ii) The monoid in this call is `Int`.
- (iii) The monoid in this call is `[Int]`.
- (iv) The monoid in this call is `String`.
- (v) The expression is equivalent to the identity function.
- (vi) The foldable in this call is `[]` - the instance for lists.

(b) `foldMap show "123456"`

- (i) The expression will fail to typecheck.
- (ii) The monoid in this call is `Int`.
- (iii) The monoid in this call is `[Int]`.
- (iv) The monoid in this call is `String`.
- (v) The expression is equivalent to the identity function.
- (vi) The foldable in this call is `[]` - the instance for lists.

$(a \rightarrow m) \rightarrow (t a) \rightarrow m$

$(a \rightarrow \text{Char}) \rightarrow [\text{Char}] \rightarrow [\text{Char}]$

(one)

`newtype Char`

`instance Foldable []`

$a = a$ or Char ?

(a) `Char`

`String` \rightarrow `Show`
`[Char]`

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or "ill-typed" if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

(a) $\lambda x \rightarrow x$

Example answer:

$a \rightarrow a$

(b) $\lambda x y \rightarrow (x,y)$

$a \rightarrow b \rightarrow (a,b)$

(c) $\lambda x y \rightarrow \text{if } x == y \text{ then } \text{show } x \text{ else } \text{show } (x,y)$

$\text{Show} :: a \rightarrow \text{String}$

(d) $\lambda x \rightarrow (x:1)++1++[x]$

$a \rightarrow [a] \rightarrow [a]$

(e) $\text{getLine} >= \text{putStrLn} (\lambda x \rightarrow (a \rightarrow m b) \rightarrow m b)$

(f) $\text{putStrLn} 42 >= \text{putStrLn} 43$

~~||| -Typed~~

(g) $\lambda () \rightarrow 42$

$a \rightarrow (\text{String}, a)$

(h) $\text{reverse} . \text{foldMap} \text{return}$

~~Foldable t~~ $\Rightarrow t a \rightarrow [a]$

(i) $\lambda l \rightarrow [(x,y) | x < -1, y < -1, x \neq y]$

~~Eq a~~ $\Rightarrow [a] \rightarrow [a, a]$

(j) $\text{let } f x = x \text{ in } (f 'a', f \text{ True})$

$(\text{Char}, \text{Bool})$

(k) $\text{filterM} (\text{const} [\text{True}, \text{False}])$

$[a] \rightarrow [[a]]$

$\text{filterM} :: \text{Monad m} \Rightarrow$

$(a \rightarrow m \text{ Bool}) \rightarrow ([a] \rightarrow [a]) \rightarrow m [a]$

$(\text{last}, \text{filter})$

$b \rightarrow [Bool]$

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix, do syntax, list comprehensions, or any valid Haskell.

- (a) $\text{Int} \rightarrow \text{Int}$
Example answers:
 $\lambda x \rightarrow x + 1$
(+1)
- (b) $\text{Bool} \rightarrow [\text{Bool}]$
 $\lambda x \rightarrow \text{if } x \text{ then } [x] \text{ else } [\text{true}]$
- (c) $a \rightarrow \text{Maybe } b$
 $\lambda x \rightarrow \text{Nothing}$
- (d) $(\text{Int} \rightarrow \text{Char} \rightarrow \text{Bool}) \rightarrow [\text{Int}] \rightarrow [\text{Char}] \rightarrow [\text{Bool}]$
- ~~liftM2~~
- (e) $(a \rightarrow b \rightarrow c) \rightarrow \text{IO } a \rightarrow \text{IO } b \rightarrow \text{IO } c$
- ~~liftM2~~
- (f) $(a \rightarrow b) \rightarrow (b \rightarrow \text{Bool}) \rightarrow [a] \rightarrow [b]$ ~~$\lambda f1 \rightarrow \lambda f2 \rightarrow \lambda xs \rightarrow [f1 a | a \leftarrow xs, f2 (f1 a)]$~~
- (g) $\text{Maybe } a \rightarrow (a \rightarrow \text{Gen } b) \rightarrow \text{Gen } (a, b)$ ~~$\lambda f \text{ = do } b \leftarrow f a$~~
 ~~$f \text{ = } \text{Just } a$~~
 ~~$\text{return } (a, b)$~~
- (h) $\text{Eq } a \Rightarrow a \rightarrow [a] \rightarrow [a]$ ~~$\lambda f1 \in [f1 a | a \leftarrow xs, f1 a == h \text{ then } [a] \text{ else } []]$~~
- (i) $\text{Show } a \Rightarrow [a] \rightarrow \text{IO } \text{String}$ ~~$\lambda f1 \in \text{genLine}$~~
 ~~$f1 (w:t) \in \text{do showIn genLine}$~~
- (j) $(a, b) \rightarrow (a \rightarrow b \rightarrow c) \rightarrow c$
- $\lambda (a, b) \rightarrow \lambda f \rightarrow f a b$

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a) `foo :: [Int] -> [Int]`

`foo l = [x * x | x <- 1, x > 0]`

Example answer:

Calculates the squares of all positive numbers in a list.

`foo [] = []`

`foo [1,0,2,-1] = [1, 4]`

(b) `foo :: [Int] -> [[Int]]`

`foo l = [(x,y) | x <- 1, y <- 1, x /= y]`

Answer: Gets all possible pairs of elements in the list except those where both elements are equal

(c) `foo :: a -> [a]`

`foo x l = reverse (x : reverse l)`

Answer: Appends x to the end of the input list!

`foo 4 [1,2,3] = [1,2,3,4]`

(d) `bar :: (a -> Maybe b) -> [a] -> [b]`

`bar f [] = []`

`bar f (x:xs) =`

`let rs = bar f xs in`

`case x of`

`Nothing -> rs`

`Just r -> r:rs`

`foo :: [Maybe a] -> [a]`

`foo = bar id`

Answer: Extracts the elements out of the "Just -"s in the list into their own list, ignoring NoltinGs

`foo [Just 3, Nothing, Just 4] = [3,4]`

(e) `foo :: [Int] -> Int -> (Int, [Int])`

`foo [] m = (m, [])`

`foo [x] m = (x, [m])`

`foo (x : xs) m = (max m' x, m' : xs')`

`where (m', xs') = foo xs m`

Answer: Returns a 2-Tuple where the first element is the maximum element of the input list, or the input Int if the list is empty, and the second element is a list of the input lists that is of the same length as the original input list

`foo [] 3 = (3,[])`

`foo [3] 4 = (3,[4])`

`foo [2,3,4] 5 = (4, [5,5,5])`

(f) *Bonus!*

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM _ [] = return []
dropWhileM p (x:xs) = do
    q <- p x
    if q then dropWhileM p xs else return (x:xs)
```

```
foo :: ??  
foo = dropWhileM (const [True, False])
```

Answer:

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

`weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]`

You can assume that the lists have the same length.

`weave [] [] = []`

`weave (h1:t1) (h2:t2) = h1 : h2 : (weave t1 t2)`

- (b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

`toMax [1,4,2,5,3] = [5,5,5,5,5]`

✓ what we understand
now (we) too operators?

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

unreasonable case

`toMax [] = []`

`toMax (h:t) = let m = getMax (h:t) in h : toMax t`

`length (h:t) = 1 + length t`

where

`length [] = 0`

`length (h:t) = 1 + length t`

`getMax [] m = m`

`getMax (h:t) m = if h > m then getMax h m`

else getMax t m

Typeclass Definitions

```
class Semigroup a where
  (++)  :: a -> a -> a

class Semigroup m => Monoid m where
  mempty :: m

class Show a where
  show :: a -> String

class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool

class Eq a => Ord a where
  compare :: a -> a -> Ordering
  (<), (<=), (>=), (>) :: a -> a -> Bool
  max, min :: a -> a -> a

class Functor f where
  fmap :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure :: a -> f a
  (<>*) :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return :: a -> m a
  (=>) :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary :: Gen a
  shrink :: a -> [a]

class Num a where
  (+), (-), (*) :: a -> a -> a
  negate :: a -> a
  abs :: a -> a
  signum :: a -> a
  fromInteger :: Integer -> a
```

Yuvraj Nayak

CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
- (i) True
 - (ii) False
- (b) The constraint `Semigroup a => Monoid a` implies that:
- (i) Every type that has a `Semigroup` instance, also has a `Monoid` instance.
 - (ii) Every type that has a `Monoid` instance, also has a `Semigroup` instance.
 - (iii) Both of the above.
 - (iv) None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler.
- (i) True
 - (ii) False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a `main` function:
- (i) The program will fail to typecheck.
 - (ii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `Int` and `Char` to generate inputs and test `foo`.
 - (iii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `()` as default to generate inputs and test `foo`.
 - (iv) Haskell will require user-provided generators for integers and characters in order to run the tests

Part 2 - 12pts

The standard library defines `foldMap` with the following type:

```
foldMap : (Monoid m, Foldable t) => (a -> m) -> t a -> m
```

For each of the following `foldMap` calls, select all options that are true:

- (a) `foldMap (:) [] [1..10]`
- (i) The expression will fail to typecheck.
 - (ii) The monoid in this call is `Int`.
 - (iii) The monoid in this call is `[Int]`.
 - (iv) The monoid in this call is `String`.
 - (v) The expression is equivalent to the identity function.
 - (vi) The foldable in this call is `[]` - the instance for lists.
- (b) `foldMap show "123456"`
- (i) The expression will fail to typecheck.
 - (ii) The monoid in this call is `Int`.
 - (iii) The monoid in this call is `[Int]`.
 - (iv) The monoid in this call is `String`.
 - (v) The expression is equivalent to the identity function.
 - (vi) The foldable in this call is `[]` - the instance for lists.

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or “ill-typed” if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

- (a) $\lambda x \rightarrow x$
Example answer:
 $a \rightarrow a$
- (b) $\lambda x y \rightarrow (x,y)$
 $a \rightarrow b \rightarrow (a,b)$
- (c) $\lambda x y \rightarrow \text{if } x == y \text{ then show } x \text{ else show } (x,y)$
~~Eq a, Show a => a → a → String~~
- (d) $\lambda x l \rightarrow x : l ++ l ++ [x]$
 $a \rightarrow [a] \rightarrow [a]$
- (e) `getLine >>= putStrLn`
- (f) `putStrLn "42" >>= putStrLn "43"`
ill-typed
- (g) `() "42"`
 $a \rightarrow (\text{String}, a)$
- (h) `reverse . foldMap return`
ill-typed
- (i) $\lambda l \rightarrow [(x,y) | x < -1, y < -1, x /= y]$
 $[a] \rightarrow [[(a,a)]]$
- (j) `let f x = x in (f 'a', f True)`
 $(\text{Char}, \text{Bool})$
- (k) `filterM (const [True, False])`
 $\text{Monad m} \Rightarrow [a] \rightarrow m [a]$

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix, do syntax, list comprehensions, or any valid Haskell.

- (a) $\text{Int} \rightarrow \text{Int}$

Example answers:

$$\lambda x \rightarrow x + 1$$

(+1)

- (b) $\text{Bool} \rightarrow [\text{Bool}]$

$$\lambda b \rightarrow [b, b]$$

- (c) $a \rightarrow \text{Maybe } b$

$$\lambda x \rightarrow \text{Nothing}$$

- (d) $(\text{Int} \rightarrow \text{Char} \rightarrow \text{Bool}) \rightarrow [\text{Int}] \rightarrow [\text{Char}] \rightarrow [\text{Bool}]$

$$\lambda f \text{ list } c \text{ list } \rightarrow [f i c | i \leftarrow \text{list}, c \leftarrow \text{list}, f i c]$$

- (e) $(a \rightarrow b \rightarrow c) \rightarrow \text{IO } a \rightarrow \text{IO } b \rightarrow \text{IO } c$

$$\text{fmap}$$

- (f) $(a \rightarrow b) \rightarrow (b \rightarrow \text{Bool}) \rightarrow [a] \rightarrow [b]$

$$\lambda f \text{ list } g \text{ list } \rightarrow [f e | e \leftarrow \text{list}, g(f e)]$$

- (g) $\text{Maybe } a \rightarrow (a \rightarrow \text{Gen } b) \rightarrow \text{Gen } (a, b)$

$$\lambda m f \rightarrow$$

- (h) $\text{Eq } a \Rightarrow a \rightarrow [a] \rightarrow [a]$

$$\lambda x \text{ list } \rightarrow \text{if list } \neq [] \text{ then } [x] \text{ else if head list } \neq x \text{ then } x : \text{list} \text{ else list}$$

- (i) Show $a \Rightarrow [a] \rightarrow \text{IO String}$

- (j) $(a, b) \rightarrow (a \rightarrow b \rightarrow c) \rightarrow c$

$$\lambda (x, y) f \rightarrow f x y$$

1 2 3 4

5 4 3 2 1

1 2 3 4 5

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a) `foo :: [Int] -> [Int]`

`foo 1 = [x * x | x <= 1, x > 0]`

Example answer:

Calculates the squares of all positive numbers in a list.

`foo [] = []`

`foo [1,0,2,-1] = [1, 4]`

(b) `foo :: [Int] -> [[Int]]`

`foo 1 = [x, y | x <= 1, y <= 1, x /= y]`

Answer: Prints all pairs of elements in `l` s.t. no pairs w/ same element

`foo [1,2,3] = [(1,2), (1,3), (2,1), (2,3), (3,1), (3,2)]`

(c) `foo :: a -> [a] -> [a]`

`foo x l = reverse (x : reverse l)`

Answer: Adds `x` to end of `list`

`foo 5 [1,2,3,4] = [1,2,3,4,5]`

`foo 5 [] = [5]`

(d) `bar :: (a -> Maybe b) -> [a] -> [b]`

`bar f [] = []`

`bar f (x:xs) =`

`let rs = bar f xs in`

`case f x of`

`Nothing -> rs`

`Just r -> r:rs`

`foo :: [Maybe a] -> [a]`

`foo = bar id`

Answer: Takes all `Just`s in a list of `Maybe`s and returns a list of elements inside `Just`

`foo [Just 1, Just 2, Nothing, Just 3] = [1,2,3]`

(e) `foo :: [Int] -> Int -> (Int, [Int])`

`foo [] m = (m, [])`

`foo [x] m = (x, [x])`

`foo (x : xs) m = (max m' x, m : xs')`

`where (m', xs') = foo xs m`

Answer: finds the max element of a list and return it in a tuple with a list of ints.

(f) *Bonus!*

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM _ [] = return []
dropWhileM p (x:xs) = do
    q <- p x
    if q then dropWhileM p xs else return (x:xs)
```

```
foo :: ??  
foo = dropWhileM (const [True, False])
```

Answer:

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

```
weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]
```

You can assume that the lists have the same length.

```
weave :: [α] → [α] → [α]
weave [] [] = []
weave (x:xs) (y:ys) = x:y:(weave xs ys)
```

- (b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

```
toMax [1,4,2,5,3] = [5,5,5,5,5]
```

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

```
toMax :: [Int] → [Int]
```

```
toMax [] =
```

Typeclass Definitions

```
class Semigroup a where
  (++) :: a -> a -> a

class Semigroup m => Monoid m where
  mempty :: m

class Show a where
  show :: a -> String

class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool

class Eq a => Ord a where
  compare :: a -> a -> Ordering
  (<), (=<), (=>), (>) :: a -> a -> Bool
  max, min :: a -> a -> a

class Functor f where
  fmap :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure :: a -> f a
  (<>*) :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return :: a -> m a
  (=>) :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary :: Gen a
  shrink :: a -> [a]

class Num a where
  (+), (-), (*) :: a -> a -> a
  negate :: a -> a
  abs :: a -> a
  signum :: a -> a
  fromInteger :: Integer -> a
```

Maverick View

CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
- (i) True
 (ii) False
- (b) The constraint `Semigroup a => Monoid a` implies that:
- (i) Every type that has a `Semigroup` instance, also has a `Monoid` instance.
 (ii) Every type that has a `Monoiod` instance, also has a `Semigroup` instance.
 (iii) Both of the above.
 (iv) None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler.
- (i) True
 (ii) False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a `main` function:
- (i) The program will fail to typecheck.
 (ii) After typeclass resolution, the resulting program will use the Arbitrary instance for `Int` and `Char` to generate inputs and test `foo`.
 (iii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `()` as default to generate inputs and test `foo`.
 (iv) Haskell will require user-provided generators for integers and characters in order to run the tests

Part 2 - 12pts

The standard library defines `foldMap` with the following type:

```
foldMap :: (Monoid m, Foldable t) => (a -> m) -> t a -> m
```

For each of the following `foldMap` calls, select all options that are true:

- (a) `foldMap (:) [] [1..10]`
- (i) The expression will fail to typecheck.
 - (ii) The monoid in this call is `Int`.
 - (iii) The monoid in this call is `[Int]`.
 - (iv) The monoid in this call is `String`.
 - (v) The expression is equivalent to the `identity` function.
 - (vi) The foldable in this call is `[]` - the instance for lists.
- (b) `foldMap show "123456"`
- (i) The expression will fail to typecheck.
 - (ii) The monoid in this call is `Int`.
 - (iii) The monoid in this call is `[Int]`.
 - (iv) The monoid in this call is `String`.
 - (v) The expression is equivalent to the `identity` function.
 - (vi) The foldable in this call is `[]` - the instance for lists.

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or “ill-typed” if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

(a) $\lambda x \rightarrow x$

Example answer:

$a \rightarrow a$

(b) $\lambda x y \rightarrow (x,y)$

$a \rightarrow b \rightarrow (a,b)$

(c) $\lambda x y \rightarrow \text{if } x == y \text{ then show } x \text{ else show } (x,y)$

~~ill-typed~~

(d) $\lambda x \ 1 \rightarrow x : (1 \mapsto (1 \mapsto [x]))$

$a \rightarrow [b] \rightarrow [b]$

(e) $\text{getLine} >= \text{putStrLn}$

$(\text{IO String}) \rightarrow (\text{String} \rightarrow \text{IO ()}) \rightarrow \text{IO ()}$

(f) $\text{putStrLn} \ 42 >= \text{putStrLn} \ 43$

~~ill-typed~~

(g) $(,) \ "42"$

$(a \rightarrow b \rightarrow (a,b)) \rightarrow [\text{Char}] \rightarrow [\text{Char}] \rightarrow ([\text{Char}], [\text{Char}])$

(h) $\text{reverse} \cdot \text{foldMap} \text{return}$

$[a] \rightarrow [m a]$

(i) $\lambda l \rightarrow [(x,y) \mid x < -1, y < -1, x /= y]$

$[Int] \rightarrow [Int]$

(j) $\text{let } f x = x \text{ in } (f \ a, f \ \text{True})$

~~ill-typed~~

(k) $\text{filterM}(\text{const} [\text{True}, \text{False}])$

$a \rightarrow [Bool]$

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix, do syntax, list comprehensions, or any valid Haskell.

(a) $\text{Int} \rightarrow \text{Int}$

Example answers:

$\lambda x \rightarrow x + 1$

(+1)

(b) $\text{Bool} \rightarrow [\text{Bool}]$

(c) $\text{a} \rightarrow \text{Maybe b}$

$\lambda x \rightarrow \text{Just } x$

(d) $(\text{Int} \rightarrow \text{Char} \rightarrow \text{Bool}) \rightarrow [\text{Int}] \rightarrow [\text{Char}] \rightarrow [\text{Bool}]$

$\text{foo } a \ b = \text{if head } a > 0 \text{ then } [\text{head } b == 'a'] \text{ else } [\text{head } b == 'b']$

(e) $(\text{a} \rightarrow \text{b} \rightarrow \text{c}) \rightarrow \text{IO a} \rightarrow \text{IO b} \rightarrow \text{IO c}$

$\lambda \quad \text{undefined}$

(f) $(\text{a} \rightarrow \text{b}) \rightarrow (\text{b} \rightarrow \text{Bool}) \rightarrow [\text{a}] \rightarrow [\text{b}]$

$\text{foo } f \ g \ lst \rightarrow \text{let } b = \text{head } (\text{map } f \ lst) \text{ in if } (f \ b) \text{ then } [b] \text{ else } [a]$

(g) $\text{Maybe a} \rightarrow (\text{a} \rightarrow \text{Gen b}) \rightarrow \text{Gen (a,b)}$

undefined

(h) $\text{Eq a} \Rightarrow \text{a} \rightarrow [\text{a}] \rightarrow \text{Eq a b} \doteq \text{if a} > \text{head b} \text{ then } [\text{a}] \text{ else } [\text{b}]$

(i) Show $\text{a} \Rightarrow [\text{a}] \rightarrow \text{IO String}$

(j) $(\text{a}, \text{b}) \rightarrow (\text{a} \rightarrow \text{b} \rightarrow \text{c}) \rightarrow \text{c}$

$\text{foo } (a, b) \ f \ = \ f \ a \ b$

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a)

```
foo :: [Int] -> [Int]
foo l = [x * x | x <- l, x > 0]
```

Example answer:

Calculates the squares of all positive numbers in a list.

```
foo [] = []
foo [1,0,2,-1] = [1, 4]
```

(b)

```
foo :: [Int] -> [Int]
foo l = [ (x,y) | x <- l, y <- l, x /= y]
```

Answer:

Returns a list of numbers if it is not equal to itself.

(c)

```
foo :: a -> [a] -> [a]
foo x l = reverse (x : reverse l) [1,3,2,1]
```

Answer:

Appends to the end of list with extra steps

↳ $1 [] = [1]$

$f 1 [1,2,3] = [1,2,3,1]$

(d)

```
bar :: (a -> Maybe b) -> [a] -> [b]
bar [] = []
bar f (x:xs) =
  let rs = bar f xs in
  case f x of
    Nothing -> rs
    Just r -> r:rs
```

```
foo :: [Maybe a] -> [a]
foo = bar id
```

Answer:

$\text{max } 2 \ 1$

(e)

```
foo :: [Int] -> Int -> (Int, [Int])
foo [] m = (m, [])
foo [x] m = (x, [m])
foo (x : xs) m = (max m' x, m' : xs')
where (m', xs') = foo xs m
```

Answer:

$\text{foo } [2] \ 3 = (2, [3])$

$\text{foo } [1,3] \ 3 = (1, [3])$

$\text{foo } [1,2] \ 3 = (2, [3,3])$

(2) Bonus!

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM [] = return []
dropWhileM p (x:xs) = do
    q <- p x
    if q then dropWhileM p xs else return (x:xs)
```

```
foo :: ??  
foo = dropWhileM (const [True, False])
```

Answer:

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

`weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]`

You can assume that the lists have the same length.

```
weave :: [Int] → [Int] → [Int]
weave [] [] → []
weave (x:xs) (y:ys) = x:y:(weave xs ys)
```

- (b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

`toMax [1,4,2,5,3] = [5,5,5,5,5]`

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

```
toMaxHelper :: Int → [Int] → Int
toMaxHelper [] a = a
toMaxHelper a (x:xs) = if a < x then toMaxHelper x xs else
    toMaxHelper a x
toMax (x:xs) = fmap (y → maxHelper x xs) (x:xs)
```

Typeclass Definitions

```
class Semigroup a where
  (<>) :: a -> a -> a

class Semigroup m => Monoid m where
  mempty :: m

class Show a where
  show :: a -> String

class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool

class Eq a => Ord a where
  compare :: a -> a -> Ordering
  (<), (<=), (>=), (>) :: a -> a -> Bool
  max, min :: a -> a -> a

class Functor f where
  fmap :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure :: a -> f a
  (*>*) :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return :: a -> m a
  (=>) :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary :: Gen a
  shrink :: a -> [a]

class Num a where
  (+), (-), (*) :: a -> a -> a
  negate :: a -> a
  abs :: a -> a
  signum :: a -> a
  fromInteger :: Integer -> a
```

Segev Elazar Mittelman

CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
 - (i) True
 - (ii) False
- (b) The constraint `Semigroup a => Monoid a` implies that:
 - (i) Every type that has a `Semigroup` instance, also has a `Monoid` instance.
 - (ii) Every type that has a `Monoid` instance, also has a `Semigroup` instance.
 - (iii) Both of the above.
 - (iv) None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler.
 - (i) True
 - (ii) False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a `main` function:
 - (i) The program will fail to typecheck.
 - (ii) After typeclass resolution, the resulting program will use the Arbitrary instance for `Int` and `Char` to generate inputs and test `foo`.
 - (iii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `()` as default to generate inputs and test `foo`.
 - (iv) Haskell will require user-provided generators for integers and characters in order to run the tests

Part 2 - 12pts

The standard library defines `foldMap` with the following type:

```
foldMap :: (Monoid m, Foldable t) => (a -> m) -> t a -> m
```

For each of the following `foldMap` calls, select all options that are true:

(a) `foldMap ([] [1..10])`

(i) The expression will fail to typecheck.

(ii) The monoid in this call is `Int`.

(iii) The monoid in this call is `[Int]`.

(iv) The monoid in this call is `String`.

(v) The expression is equivalent to the identity function.

(vi) The foldable in this call is `[]` - the instance for lists.

(b) `foldMap show "123456"`

(i) The expression will fail to typecheck.

(ii) The monoid in this call is `Int`.

(iii) The monoid in this call is `[Int]`.

(iv) The monoid in this call is `String`.

(v) The expression is equivalent to the identity function.

(vi) The foldable in this call is `[]` - the instance for lists.

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or “ill-typed” if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

- (a) $\lambda x \rightarrow *$
Example answer:
 $a \rightarrow a$
- (b) $\lambda x y \rightarrow (x,y)$
 $a \rightarrow b \rightarrow (a,b)$
- (c) $\lambda x y \rightarrow \text{if } x == y \text{ then show } x \text{ else show } (x,y)$
 $(Eq a, Show a) \Rightarrow a \rightarrow a \rightarrow String$
- (d) $\lambda x \rightarrow x : 1 ++ 1 ++ [x]$
 $a \rightarrow [a] \Rightarrow [a]$
- (e) $\text{getLine} >>= \text{putStrLn}$
 $IO()$
- (f) $\text{putStrLn} 42 >>= \text{putStrLn} 43$
ill-typed, putStrLn not a function type
- (g) $(.)^n 42$
 $a \rightarrow (String, a)$
- (h) $\text{reverse} \cdot \text{foldMap} \text{return}$
ill-typed, return doesn't return a monoid, it returns a monad
- (i) $\lambda l \rightarrow [(x,y) | x < -1, y < -1, x /= y]$
 $(Eq a) \Rightarrow IO \Rightarrow [(a, a)]$
- (j) $\text{let } f x = x \text{ in } (f 'a', f \text{ True})$
 $(Char, Bool)$
- (k) $\text{filterM} (\text{const} [\text{True}, \text{False}])$
 $[a] \Rightarrow [[a]]$

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix, do syntax, list comprehensions, or any valid Haskell.

(e) $\text{Int} \rightarrow \text{Int}$

Example answers:

$\lambda x \rightarrow x + 1$

(+1)

(b) $\text{Bool} \rightarrow [\text{Bool}]$

$\lambda b \rightarrow [(b, b)]$

(c) $a \rightarrow \text{Maybe } b$

$\lambda a \rightarrow \text{Nothing}$

(d) $(\text{Int} \rightarrow \text{Char}) \rightarrow [\text{Int}] \rightsquigarrow [\text{Char}] \rightarrow [\text{Bool}]$

ZipWith

(e) $(a \rightarrow b \rightarrow c) \rightarrow \text{IO } a \rightarrow \text{IO } b \rightarrow \text{IO } c$

liftM2

(f) $(a \rightarrow b) \rightarrow (b \rightarrow \text{Bool}) \rightarrow [a] \rightarrow [b]$

If p as → filter p (fmap f as)

(g) $\text{Maybe } a \rightarrow (a \rightarrow \text{Gen } b) \rightarrow \text{Gen } (a, b)$

UnDefined

(can't handle the Nothing case)

(h) $\text{Eq } a \Rightarrow a \rightarrow [a] \rightarrow [a]$

$\lambda a \text{ as } \rightarrow \text{if } a = a \text{ then } (a : \text{as}) \text{ else as}$

(i) $\text{Show } a \Rightarrow [a] \rightarrow \text{IO String}$

$\lambda a \text{ as } \rightarrow \text{foldMap show as}$

(j) $(a, b) \rightarrow (a \rightarrow b \rightarrow c) \rightarrow c$

fmap worry

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a) `foo :: [Int] -> [Int]`

`foo 1 = [x * x | x <- 1, x > 0]`

Example answer:

Calculates the squares of all positive numbers in a list.

`foo [] = []`

`foo [1,0,2,-1] = [1, 4]`

(b)

`foo :: [Int] -> [Int]`

`foo 1 = [(x,y) | x <- 1, y <- 1, x /= y]`

Answer: Calculates list of all pairs of nonequal elements of the input list of ints

`foo [] = []`

`foo [1] = []`

`foo [1,2] = [(1,2), (2,1)]`

`foo :: a -> [a] -> [a]`

`foo x 1 = reverse (x : reverse 1)`

Answer: Appends the element x to the end of the list.

`foo 1 [2] = [2,1]`

(d) `bar :: (a -> Maybe b) -> [a] -> [b]`

`bar f [] = []`

`let rs = bar f xs in`

`case f x of`

`Nothing -> rs`

`Just r -> r:rs`

`foo :: [Maybe a] -> [a]`

`foo = bar id`

Answer: foo takes a list of Maybe a values, and returns a list of all the values in Just constructors in the input list, removing the Nolthings.

`foo [] = []`

`foo [x] m = (x, [m])`

`foo (x : xs) m = (max m' x, m : xs')`

`where (m', xs') = foo xs m`

Answer: Returns a pair of the maximum element in the list and a list repeating m a number of times equal to the length of the input list

`foo [1,2,3] 0 = (3,[0,0,0])`

`foo [2,3] 0 = (3,[0,0])`

`foo [3] 0 = (3,[0])`

`foo [] 0 = (3,[0])`

(f) *Eonus!*

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM [] = return []
dropWhileM p (x:xs) = do
    q <- p x
    if q then dropWhileM p xs else return (x:xs)
```

```
foo :: ?? [a] -> [a]
foo = dropWhileM (const [True, False])
```

Answer: returns the list of all tails of a list including the original list

foo [] = [[]]

foo [1, 2, 3] = [[1, 2, 3], [2, 3], [3], []]

foo "lol" = ["lol", "ol", "l", ""]

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

```
weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]
```

You can assume that the lists have the same length.

```
weave :: [a] -> [a] -> [a]
weave [] [] = []
weave (a:as) (b:bs) = a:b : weave as bs
weave _ _ = error "lists diff size"
```

- (b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

```
toMax [1,4,2,5,3] = [5,5,5,5,5]
```

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

```
toMax :: [Int] -> [Int]
toMax [] = []
toMax (x:xs) = foo (x:xs) X
  in fmap (const m) as
```

Bonus: `toMax`

`toMax [] = []`

`toMax (x:xs) = let (m, l) = toMax' x 1 xs in replicate m`

`where toMax' m l [] = (m, l)`

`toMax' m (a:as) = toMax' a (l+1) as`

`otherwise = toMax' m (l+1) as`

$\left\{ \begin{array}{l} \text{if } \text{length } m \leq 0 = [] \\ \text{otherwise} = m : \text{replicate}(n-1)m \end{array} \right.$

Typeclass Definitions

```
class Semigroup a where
  (++) :: a -> a -> a

class Semigroup m => Monoid m where
  mempty :: m

class Show a where
  show :: a -> String

class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool

class Eq a => Ord a where
  compare :: a -> a -> Ordering
  (<), (<=), (=>), (>) :: a -> a -> Bool
  max, min :: a -> a -> a

class Functor f where
  fmap :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure :: a -> f a
  (*)> :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return :: a -> m a
  (=>) :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary :: Gen a
  shrink :: a -> [a]

class Num a where
  (+), (-), (*) :: a -> a -> a
  negate :: a -> a
  abs :: a -> a
  signum :: a -> a
  fromInteger :: Integer -> a
```

Arbitrary Fayerz

CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
- (i) True
 (ii) False
- (b) The constraint `Semigroup a => Monoid a` implies that:
- (i) Every type that has a Semigroup instance, also has a Monoid instance.
 (ii) Every type that has a Monoid instance, also has a Semigroup instance.
 (iii) Both of the above.
 (iv) None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler.
- (i) True
 (ii) False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a `main` function:
- (i) The program will fail to typecheck.
 (ii) After typeclass resolution, the resulting program will use the Arbitrary instance for Int and Char to generate inputs and test `foo`.
 (iii) After typeclass resolution, the resulting program will use the Arbitrary instance for () as default to generate inputs and test `foo`.
 (iv) Haskell will require user-provided generators for integers and characters in order to run the tests

Part 2 - 12pts

The standard library defines `foldMap` with the following type:

```
foldMap :: (Monoid m, Foldable t) => (a -> m) -> t a -> m
```

For each of the following `foldMap` calls, select all options that are true:

 (a) `foldMap (:) [] [1..10]`

(i) The expression will fail to typecheck.

(ii) The monoid in this call is `Int`.

(iii) The monoid in this call is `[Int]`.

(iv) The monoid in this call is `String`.

(v) The expression is equivalent to the identity function.

(vi) The foldable in this call is `[]` - the instance for lists.

 (c) `foldMap show "123456"`

(i) The expression will fail to typecheck.

(ii) The monoid in this call is `Int`.

(iii) The monoid in this call is `[Int]`.

(iv) The monoid in this call is `String`.

(v) The expression is equivalent to the identity function.

(vi) The foldable in this call is `[]` - the instance for lists.

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or "ill-typed" if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

(a) $\lambda x \rightarrow x$

Example answer:

$a \rightarrow a$

(b) $\lambda x y \rightarrow (x,y)$

(c) $\lambda x y \rightarrow \text{if } x == y \text{ then show } x \text{ else show } (x,y)$

$\text{Eq } a \Rightarrow a \rightarrow \text{String}$

(d) $\lambda x \rightarrow x : 1 \uparrow \uparrow 1 \uparrow \uparrow [x]$

$a \Rightarrow [a] \rightarrow [a]$

(e) $\text{getLine} >>= \text{putStrLn}$

$\overline{\text{IO }} u$

(f) $\text{putStrLn } 42 >>= \text{putStrLn } 43$

i) -Type Q

(g) $(,) "42"$

$a \rightarrow (a, \text{String})$

$\text{Monoid } m \Rightarrow t \rightarrow m a$

(h) $\text{reverse} : \text{foldMap return}$

(i) $\lambda l \rightarrow [(x,y) | x < -1, y < -1, x / = y]$

$(\text{Ord } a, \text{Eq } a) \Rightarrow [a] \rightarrow [(a,a)]$

(j) $\lambda f x = x \in (f a', f \text{ True})$

iii) **Hyped**

(k) $\text{filterM} (\text{const } [\text{True}, \text{False}])$

$[a] \rightarrow [[a]]$ ~~$a \Rightarrow [\text{Bool}] \rightarrow [\text{List } [a]]$~~

Answers

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix; do syntax, list comprehensions, or any valid Haskell.

- (a) $\text{Int} \rightarrow \text{Int}$

Example answers:

$$\lambda x \rightarrow x + 1$$

(+1)

- (b) $\text{Bool} \rightarrow [\text{Bool}]$
 $\lambda a \rightarrow \text{if } a \text{ then replicate } a \text{ else } [a]$

- (c) $a \rightarrow \text{Maybe } b$
 $\lambda a \rightarrow \text{Just } a$

- (d) $(\text{Int} \rightarrow \text{Char} \rightarrow \text{Bool}) \rightarrow [\text{Int}] \rightarrow [\text{Char}] \rightarrow [\text{Bool}]$

- (e) $(a \rightarrow b \rightarrow c) \rightarrow \text{IO } a \rightarrow \text{IO } b \rightarrow \text{IO } c$

~~liftM2~~

- (f) $(a \rightarrow b) \rightarrow (b \rightarrow \text{Bool}) \rightarrow [a] \rightarrow [b]$

~~map f~~

- (g) $\text{Maybe } a \rightarrow (a \rightarrow \text{Gen } b) \rightarrow \text{Gen } (a, b)$

~~for ma f = do a <- ma
 b <- (f a)
 return (a, b)~~

- (h) $\text{Eq } a \Rightarrow a \rightarrow [a] \rightarrow [a]$

~~\lambda lst \rightarrow filter (==a) lst~~

- (i) Show $a \Rightarrow [a] \rightarrow \text{IO String}$

~~\lambda lst \rightarrow do map show lst
 getLine~~

- (j) $(a, b) \rightarrow (a \rightarrow b \rightarrow c) \rightarrow c$

~~\lambda x y \rightarrow uncurry y x~~

Question 4 (20 points ± 10pt bonus)

For each of the following functions, write down a short description of what examples.

(a) `foo :: [Int] -> [Int]`

Example answer:

`foo` = `l` calculates the squares of all positive numbers in a list.

$$100 [1,0,2,-1] = [1,4]$$

```
foo l = [ (x,y) |
```

Greeks list of battles after -
Answer:

$$\{1, 2, 3\} = \{(1, 2), (1,$$

```
foo x l = reverse (x : reverse l)
```

卷之三

卷之三

bar :: (a -> Maybe b) -> [a] = [1,2,3,4]

```
bar f (x:xs) = [
```

```
case f x of  
Nothing >  
    _
```

Just R -> R:TS

```
foo = bar id
```

Answer:

卷之三

foo : [Just 1, Just 2, Just 3, Just 4, Just 5] = Just 180

... , limit) = [1, 4]

100 (X : xs) m = (max m' x, m : x
where (m', xs') = fOO ys m

answer: 6 [116]

returns a tuple with the first element as the biggest element in the first argument (list) and the second element of the tuple as a list where each element is the second argument and has a length that is equal to the length of the first argument

Returns a list of the top 1000 entries.

```
(f` Bonus!
drcpWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM = []
dropWhileM p (x:xs) = do
    q <- p x
    if q then dropWhileM p xs else return (x:xs)
```

```
foo :: ??  
foo = dropWhileM (const [True, False])
```

Answer:

foo :: [a] → [[a]]

foo [1,2,3] =

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function weave that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

```
weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]
```

You can assume that the lists have the same length ✓

weave :: [a] → [a] → [a]

weave [] [] = []

weave (x:xs) (y:ys) = x:y:weave xs ys

- (b) Implement a function toMax, that given a non-empty list of integers, returns a list of the same length,

where each element has been replaced by the maximum element of the list. For example:
toMax [1,4,2,5,3] = [5,5,5,5,5]

You can use the foo function of problem (4e) if it helps.

BONUS: Implement toMax so that it only traverses a list once!

toMax :: [Int] → [Int]

~~toMax~~

to Max lst = replicate (maximum lst) (length lst)
~~and maximum Bore the same index as xs~~

Typeclass Definitions

```
class Semigroup a where
  (++) :: a -> a -> a

class Semigroup m => Monoid m where
  mempty :: m

class Show a where
  show :: a -> String

class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool

class Eq a => Ord a where
  compare :: a -> a -> Ordering
  (<), (=<), (=>), (>) :: a -> a -> Bool
  max, min :: a -> a -> a

class Functor f where
  fmap :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure :: a -> f a
  (*>) :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return :: a -> m a
  (=>) :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary :: Gen a
  shrink :: a -> [a]

class Num a where
  (+), (-), (*) :: a -> a -> a
  negate :: a -> a
  abs :: a -> a
  signum :: a -> a
  fromInteger :: Integer -> a
```

Susan
wen

CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
- (i) True
 (ii) False
- (b) The constraint `Semigroup a => Monoid a` implies that:
- (i) Every type that has a `Semigroup` instance, also has a `Monoid` instance.
 (ii) Every type that has a `Monoid` instance, also has a `Semigroup` instance.
 (iii) Both of the above.
 (iv) None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler.
- (i) True
 (ii) False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a `main` function:
- (i) The program will fail to typecheck.
 (ii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `Int` and `Char` to generate inputs and test `foo`.
 (iii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `()` as default to generate inputs and test `foo`.
 (iv) Haskell will require user-provided generators for integers and characters in order to run the tests

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or “ill-typed” if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

(a) $\lambda x \rightarrow x$

Example answer:

$a \rightarrow a$

(b) $\lambda x y \rightarrow (x,y)$

$a \rightarrow b \rightarrow (a,b)$

(c) $\lambda x y \rightarrow \text{if } x == y \text{ then show } x \text{ else show } (x,y)$

$(\text{show} \ a, \text{Eq} \ a) \Rightarrow a \rightarrow a \rightarrow \text{String}$

(d) $\lambda x l \rightarrow x : l ++ l ++ [x]$

$a \rightarrow [a] \rightarrow [a]$

(e) $\text{getLine} >>= \text{putStrLn}$

IO ()

(f) $\text{putStrLn} \ 42 >>= \text{putStrLn} \ 43$

~~!!-typed~~

(g) $(,) "42"$

$a \rightarrow (\text{String}, a)$

(h) $\text{reverse} \cdot \text{foldMap} \text{return}$

$[a] \rightarrow [\text{Maybe } a]$

(i) $\lambda l \rightarrow [(x,y) \mid x < -l, y < -l, x /= y]$

$\text{Eq } a \Rightarrow [a] \rightarrow \text{List } [(a,a)]$

(j) $\text{let } f x = x \text{ in } (f 'a', f \text{ True})$

$(\text{Char}, \text{Bool})$

(k) $\text{filterM} \ (\text{const} [\text{True}, \text{False}])$

~~!!-typed~~

$[a] \rightarrow [a]$

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix, do syntax, list comprehensions, or any valid Haskell.

(a) $\text{Int} \rightarrow \text{Int}$

Example answers:

$\lambda x \rightarrow x + 1$

(+1)

(b) $\text{Bool} \rightarrow [\text{Bool}]$

$\lambda x \rightarrow (x \& \text{True}) : []$

(c) $\text{a} \rightarrow \text{Maybe b}$

~~foo x = undefined~~

(d) $(\text{Int} \rightarrow \text{Char} \rightarrow \text{Bool}) \rightarrow [\text{Int}] \rightarrow [\text{Char}] \rightarrow [\text{Bool}]$

$\lambda f x y \rightarrow [f x' y' | x' \leftarrow x, y' \leftarrow y]$

(e) $(\text{a} \rightarrow \text{b} \rightarrow \text{c}) \rightarrow \text{IO a} \rightarrow \text{IO b} \rightarrow \text{IO c}$

(f) $(\text{a} \rightarrow \text{b}) \rightarrow (\text{b} \rightarrow \text{Bool}) \rightarrow [\text{a}] \rightarrow [\text{b}]$

$\lambda f g xs \rightarrow \text{filter } g (\text{map } f xs)$

(g) $\text{Maybe a} \rightarrow (\text{a} \rightarrow \text{Gen b}) \rightarrow \text{Gen (a,b)}$

$\lambda x f \rightarrow \text{case } x \text{ of } \text{Nothing} \rightarrow \text{Nothing}$

$\text{Just y} \rightarrow \text{do}$

$z \leftarrow fy$

$\text{return } (y, z)$

(h) $\text{Eq a} \Rightarrow \text{a} \rightarrow [\text{a}] \rightarrow [\text{a}]$

$\lambda x ls \rightarrow \text{filter } (== x) ls$

(i) $\text{Show a} \Rightarrow [\text{a}] \rightarrow \text{IO String}$

~~filter/concat~~ $\lambda foo = \text{getLine}$

(j) $(\text{a}, \text{b}) \rightarrow (\text{a} \rightarrow \text{b} \rightarrow \text{c}) \rightarrow \text{c}$

$\lambda (x, y) f \rightarrow f x y$

$\lambda f g xs \rightarrow (\text{map } f xs)$

$\lambda f g$

λf

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a)

```
foo :: [Int] -> [Int]
foo l = [x * x | x <- 1, x > 0]
```

Example answer:

Calculates the squares of all positive numbers in a list.

```
foo [] = []
foo [1,0,2,-1] = [1, 4]
```

(b)

```
foo :: [Int] -> [[Int, Int]]
foo l = [(x,y) | x <- 1, y <- 1, x /= y]
```

Answer:

create list of all pairings of non-equal numbers in list l.

(c)

```
foo :: a -> [a] -> [a]
foo x l = reverse (x : reverse l)
```

Answer:

add x to end of list l

```
foo o [1,2,3] = [1]
```

(d)

```
bar :: (a -> Maybe b) -> [a] -> [b]
bar [] = []
bar f (x:xs) =
```

let rs = bar f xs in

case f x of Nothing -> rs

Just x -> rs

Value to list

Answer:

```
foo :: [Maybe a] -> [a]
foo = bar id
```

Answer:

remove all `Nothing`s and keep values in `Just`'s

`foo [] = []`

```
foo [ Just l, Just 2 ] = [ 1, 2 ]
```

(e)

```
foo :: [Int] -> Int -> (Int, [Int])
foo [] m = (m, [])
foo [x] m = (x, [m])
foo (x : xs) m = (max m' x, m : xs')
where (m', xs') = foo xs m
```

Answer:

return make a tuple where first is the largest number in the list plus m and second is

a list of m's length list of (x:xs)

```
foo [ ] o = (o, [])
foo [2,3] 4 = (3, [4])
```

(f) Bonus!

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM _ [] = return []
dropWhileM p (x:xs) = do
    q <- p x
    if q then dropWhileM p xs else return (x:xs)

foo :: ???
foo = dropWhileM (const [True, False])
```

Answer:

verans. monad
generates list with False

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

```
weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]
```

You can assume that the lists have the same length.

```
weave [] [] = []
```

```
weave (x:xs) (y:ys) = x: y: (weave xs ys)
```

- (b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

```
toMax [1,4,2,5,3] = [5,5,5,5,5]
```

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

```
+o Max (x: xs) = \x y a y = foldr (\y a -> if y > a then y else a) x xs
  \n
  \n
  \n
  \n
+o Max ls @ (x: xs) m a x
  \n
  \n
  \n
  \n
+o Max ls @ (x: xs) = snd (foo (ls m))
```

```
where m = foldr (\y a -> if y > a then y else a) x ls
```

Typeclass Definitions

```
class Semigroup a where
  (++) :: a -> a -> a

class Semigroup m => Monoid m where
  mempty :: m

class Show a where
  show :: a -> String

class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool

class Eq a => Ord a where
  compare :: a -> a -> Ordering
  (<), (=<), (=>), (>) :: a -> a -> Bool
  max, min :: a -> a -> a

class Functor f where
  fmap :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure :: a -> f a
  ( <*> ) :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return :: a -> m a
  (">>>") :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary :: Gen a
  shrink :: a -> [a]

class Num a where
  (+), (-), (*) :: a -> a -> a
  negate :: a -> a
  abs :: a -> a
  signum :: a -> a
  fromInteger :: Integer -> a
```

Siddharth Taneja

CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
- (i) True
 (ii) False
- (b) The constraint `Semigroup a => Monoid a` implies that:
- (i) Every type that has a `Semigroup` instance, also has a `Monoid` instance.
 (ii) Every type that has a `Monoid` instance, also has a `Semigroup` instance.
 (iii) Both of the above.
 (iv) None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler.
- (i) True
 (ii) False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a main function:
- (i) The program will fail to typecheck.
 (ii) After typeclass resolution, the resulting program will use the Arbitrary instance for `Int` and `Char` to generate inputs and test `foo`.
 (iii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `()` as default to generate inputs and test `foo`.
 (iv) Haskell will require user-provided generators for integers and characters in order to run the tests

m = sum

f = f(a)

t = [a]

a = 1..10

Part 2 - 12pts

The standard library defines `foldMap` with the following type:

```
foldMap :: (Monoid m, Foldable t) => (a -> m) -> t a -> m
```

For each of the following `foldMap` calls, select all options that are true:

- (a) `foldMap (:) [] [1..10]`
- (i) The expression will fail to typecheck.
 - (ii) The monoid in this call is `Int`.
 - (iii) The monoid in this call is `[Int]`.
 - (iv) The monoid in this call is `String`.
 - (v) The expression is equivalent to the identity function.
 - (vi) The foldable in this call is `[]` - the instance for lists.
- (b) `foldMap show "123456"`
- (i) The expression will fail to typecheck.
 - (ii) The monoid in this call is `Int`.
 - (iii) The monoid in this call is `[Int]`.
 - (iv) The monoid in this call is `String`.
 - (v) The expression is equivalent to the identity function.
 - (vi) The foldable in this call is `[]` - the instance for lists.

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or “ill-typed” if it contains a type error. The type signatures of all functions are given.

- (b) $\backslash x y -> (x,y)$
 $a \rightarrow b \rightarrow (a,b)$

(c) $\backslash x y -> \text{if } x == y \text{ then show } x \text{ else show } (x,y)$
 $E_2 a, \text{Show } a => a \rightarrow a \rightarrow \text{String}$

(d) $\backslash x l -> x : l ++ l ++ [x]$
 $a \rightarrow [a] \rightarrow [a]$

(e) `getLine >>= putStrLn`

(f) `putStrLn "42" >>= putStrLn "43"`
 $\text{if } \neg \text{typed}$

(g) $(,) "42"$

$a \rightarrow (\text{String}, a)$

(h) `reverse . foldMap return`
 $[a] \rightarrow [a]$

(i) $\backslash l -> [(x,y) | x < -1, y < -1, x /= y]$
 $E_2 a \Rightarrow [a] \rightarrow [(a,a)]$

(j) $\text{let } f x = x \text{ in } (f `a`, f \text{ True})$
 $(\text{Char}, \text{Bool})$

(k) `filterM (const [True, False])`

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as [], Nothing, or undefined) unless there is no other option. You can use any function from the appendix, do syntax, list comprehensions, or any valid Haskell.

- (a) $\text{Int} \rightarrow \text{Int}$

Example answers:

$$\lambda x \rightarrow x + 1$$

(+1)

(b) $\text{Bool} \rightarrow [\text{Bool}]$
 $\lambda x \rightarrow [x \& \text{True}]$

(c) $a \rightarrow \text{Maybe } b$

$\lambda x \rightarrow \text{Nothing}$

(d) $(\text{Int} \rightarrow \text{Char} \rightarrow \text{Bool}) \rightarrow [\text{Int}] \rightarrow [\text{Char}] \rightarrow [\text{Bool}]$

zipWith

(e) $(a \rightarrow b \rightarrow c) \rightarrow \text{IO } a \rightarrow \text{IO } b \rightarrow \text{IO } c$

liftA2

(f) $(a \rightarrow b) \rightarrow (b \rightarrow \text{Bool}) \rightarrow [a] \rightarrow [b]$

\f g → map f

(g) $\text{Maybe } a \rightarrow (a \rightarrow \text{Gen } b) \rightarrow \text{Gen } (a,b)$
 $\lambda (Just x) f \rightarrow do y <- f x ; return (x,y)$

(h) $\text{Eq } a \Rightarrow a \rightarrow [a] \rightarrow [a]$
 $\lambda x s \rightarrow [y | y \leftarrow xs, x /= y]$

(i) Show $a \Rightarrow [a] \rightarrow \text{IO String}$

$\lambda xs \rightarrow do x <- xs ; putStrLn (show x); getLine$

(j) $(a,b) \rightarrow (a \rightarrow b \rightarrow c) \rightarrow c$

$\lambda (x,y) f \rightarrow f x y$

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a) `foo :: [Int] -> [Int]`

Example answer:

Calculates the squares of all positive numbers in a list.

`foo [] = []`

`foo [1,0,2,-1] = [1, 4]`

(b) `foo :: [Int] -> [[(Int, Int, Int)]]`

Answer: $\text{foo} [1] = \{\}$ all pairs of unequal elements in a list

`foo [1,2,3] = [(1,2), (1,3), (2,1), (2,3), (3,1), (3,2)]`

Answer: Pairs x of x and of the given list L

`foo [] [2,3,4] = [2, 3, 4, 1]`

`foo [] [] = []`

Answer: $\text{bar} :: \text{Maybe } a \rightarrow \text{Maybe } b$

`bar f (x:xs) =`

`let rs = bar f xs in`

`case f x of`

`Nothing -> rs`

`Just r -> r:rs`

Answer: Takes a list of `Maybe a`'s and removes all the `Nothing`'s

Answer: $\text{foo} :: \text{List } \text{Nothing}, \text{Nothing} \rightarrow \text{List } \text{Nothing}$

`foo [] [] = []`

`foo [] [m] = [m]`

`foo (x:xs) m = (max m' x, m : xs')`

`where (m', xs') = foo xs m`

Answer: `foo` returns the maximum of all integers in the list, along with a list with each element replaced by `m`. If the list is empty then "default" `m` as the max value.

`foo [1,2,4,5] 3 = (5, [3,3,3,3])`

`foo [1,2,3] 3 = (3, [2,2,2])`

`foo [] 4 = (4, [])`

$m = \boxed{?}$

(ii) Bonus!

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM [] = return []
dropWhileM p (x:xs) = do
    q <- p x
    if q then dropWhileM p xs else return (x:xs)
```

foo :: ??[q] → [[a]]

foo = dropWhileM (const [True, False])

Answer: foo takes a list ℓ and returns all suffixes

of ℓ in decreasing size order

foo [1, 2, 3] = [[1, 2, 3], [2, 3], [3], []]

foo "abcd" = ["abcd", "bcd", "cd", "d", []]

foo [] = [[]]

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

`weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]`

You can assume that the lists have the same length.

`weave :: [a] → [a] → [a]`

$$\text{weave } (x : xs) \ (y : ys) = x : (y : (\text{weave } xs \ ys))$$

`weave = _ = []`

↑ If the lists are of unequal length then we return [].

- (b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

`toMax [1,4,2,5,3] = [5,5,5,5,5]`

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

`toMax :: [Int] → [Int]`

`toMax ℓ = replicate (length ℓ) (maximum ℓ)`

Bonus:

$$\begin{aligned} \text{dfold } &: (\text{Int}^+ \rightarrow (\text{Int}^+ \rightarrow \text{Int}^+) \rightarrow (\text{Int}^+ \rightarrow \text{Int}^+)) \rightarrow (\text{Int}^+ \rightarrow \text{Int}^+) \rightarrow (\text{Int}^+ \rightarrow \text{Int}^+ \rightarrow [\text{Int}^+]) \\ &\quad \text{dfold } p \ f_{\text{acc}} \ acc \ () = [] \\ &\quad \text{dfold } p \ f_{\text{acc}} \ acc \ (x : xs) = do \\ &\quad \quad (f', q) \leftarrow \text{dfold } p \ (p \times f_{\text{acc}}) \ acc \ xs \\ &\quad \quad (p' \times f') \ (f' x) ; q \end{aligned}$$

$\text{dfold } x = \text{sum} (\text{ofold } (\lambda x \ f \rightarrow \lambda y \ \text{max} \ x (f y)) \ id \ [7 \ x])$

Typeclass Definitions

```
class Semigroup a where
  (++) :: a -> a -> a

class Semigroup m => Monoid m where
  mempty :: m

class Show a where
  show :: a -> String

class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool

class Eq a => Ord a where
  compare :: a -> a -> Ordering
  (<), (==), (>) :: a -> a -> Bool
  max, min :: a -> a -> a

class Functor f where
  fmap :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure :: a -> f a
  (<*>) :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return :: a -> m a
  (">>>") :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary :: Gen a
  shrink :: a -> [a]

class Num a where
  (+), (-), (*) :: a -> a -> a
  negate :: a -> a
  abs :: a -> a
  signum :: a -> a
  fromInteger :: Integer -> a
```

Reid Huntley

CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8 pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
- True
 - False
- (b) The constraint `Semigroup a => Monoid a` implies that:
- Every type that has a `Semigroup` instance, also has a `Monoid` instance.
 - Every type that has a `Monoid` instance, also has a `Semigroup` instance.
 - Both of the above.
 - None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler.
- True
 - False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a `main` function:
- The program will fail to typecheck.
 - After typeclass resolution, the resulting program will use the Arbitrary instance for `Int` and `Char` to generate inputs and test `foo`.
 - After typeclass resolution, the resulting program will use the `Arbitrary` instance for `()` as default to generate inputs and test `foo`.
 - Haskell will require user-provided generators for integers and characters in order to run the tests

Part 2 - 12pts

The standard library defines `foldMap` with the following type:

```
foldMap :: (Monoid m, Foldable t) => (a -> m) -> t a -> m
```

For each of the following `foldMap` calls, select all options that are true:

- (a) `foldMap (:) [] [1..10]`
- (i) The expression will fail to typecheck.
 - (ii) The monoid in this call is `Int`.
 - (iii) The monoid in this call is `[Int]`.
 - (iv) The monoid in this call is `String`.
 - (v) The expression is equivalent to the identity function.
 - (vi) The foldable in this call is `[]` - the instance for lists.
- (b) `foldMap show "123456"`
- (i) The expression will fail to typecheck.
 - (ii) The monoid in this call is `Int`.
 - (iii) The monoid in this call is `[Int]`.
 - (iv) The monoid in this call is `String`.
 - (v) The expression is equivalent to the identity function.
 - (vi) The foldable in this call is `[]` - the instance for lists.

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or “ill-typed” if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

(a) $\lambda x \rightarrow x$

Example answer:

$a \rightarrow a$

(b) $\lambda x y \rightarrow (x,y)$

$a \rightarrow b \rightarrow (a,b)$

(c) $\lambda x y \rightarrow \text{if } x == y \text{ then show } x \text{ else show } (x,y)$

$(Eq, Show) \triangleright a \rightarrow String$

(d) $\lambda x l \rightarrow x : l ++ l ++ [x]$

$a \rightarrow [a] \rightarrow [a]$

(e) $\text{getLine} >>= \text{putStrLn}$

$I\ O ()$

(f) $\text{putStrLn "42"} >>= \text{putStrLn "43"}$

~~ill-typed~~

(g) $() \ "42"$

$a \rightarrow (String, a)$

(h) $\text{reverse} . \text{foldMap} \text{return}$

$[a] \rightarrow [a]$

(i) $\lambda l \rightarrow [(x,y) | x < -1, y < -1, x /= y]$

$Eq a \Rightarrow [a] \rightarrow [(a,a)]$

(j) $\text{let } f x = x \text{ in } (f `a`, f \text{ True})$

$(Char, Bool)$

(k) $\text{filterM} (\text{const} [\text{True}, \text{False}])$

$[a] \rightarrow [[a]]$

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix, do syntax, list comprehensions, or any valid Haskell.

(a) `Int -> Int`

Example answers:

$\lambda x \rightarrow x + 1$

(+1)

(b) `Bool -> [Bool]`

$\lambda x \rightarrow [x]$

(c) `a -> Maybe b`

const Nothing

(d) `(Int -> Char -> Bool) -> [Int] -> [Char] -> [Bool]`

$\lambda f x y \rightarrow f \langle x \rangle \times \langle * \rangle y$

(e) `(a -> b -> c) -> IO a -> IO b -> IO c`

$\lambda f x y \rightarrow f \langle x \rangle \times \langle * \rangle y$

(f) `(a -> b) -> (b -> Bool) -> [a] -> [b]`

$\lambda f p x \rightarrow f \text{ filter } p \text{ (map } f \text{ x)}$

(g) `Maybe a -> (a -> Gen b) -> Gen (a,b)`

$\lambda n f \rightarrow \text{return undefined}$

(h) `Eq a => a -> [a] -> [a]`

$\lambda x \rightarrow \text{filter } (x ==)$

(i) `Show a => [a] -> IO String`

`return . foldMap show`

(j) `(a,b) -> (a -> b -> c) -> c`

flip uncurry

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a) `foo :: [Int] -> [Int]`

`foo l = [x * x | x <- l, x > 0]`

Example answer:

Calculates the squares of all positive numbers in a list.

`foo [] = []`

`foo [1,0,2,-1] = [1, 4]`

(b) `foo :: [Int] -> [Int]`

`foo l = [(x,y) | x <- l, y <- l, x /= y]`

Answer:

Computes every pair of distinct Ints that can be made using the elements of a passed-in list.

(c) `foo :: a -> [a] -> [a]`

`foo x l = reverse (x : reverse l)`

Answer:

Inserts an element at the end of a list

(d) `bar :: (a -> Maybe b) -> [a] -> [b]`

`bar f [] = []`

`let rs = bar f xs in`

`case f x of`

`Nothing -> rs`

`Just r -> r:rs`

`foo :: [Maybe a] -> [a]`

`foo = bar id`

Answer:

Takes a list of `Maybes` and returns a list of the values contained in the `Just` elements in the same order

(e) `foo :: [[Int]] -> Int -> (Int, [Int])`

`foo [] m = (m, [])`

`foo [x] m = (x, [m])`

`foo (x : xs) m = (max m' x, m : xs')`

`where (m', xs') = foo xs m`

Answer:

Returns the max value amongst a list of ints, as well as a list that's the same length as the passed-in list

or a passed-in Int if the list is empty,

and only contains copies of the passed-in int

(f) *Bonus!*

```
cropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM :: (Monad m) => [a] -> m [a]
dropWhileM p [] = return []
dropWhileM p (x:xs) = do
    q <- p x
    if q then cropWhileM p xs else return (x:xs)
foo :: ?? [Bool] -> [Bool]
foo = dropWhileM (const [True, False])
```

Answer:

~~fails~~, a list and returns every slice of that list (subsequence) which ends with the last element, as well as the empty list.

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

```
weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]
```

You can assume that the lists have the same length.

```
weave :: [a] → [a] → [a]  
weave [] _ = []  
weave _ [] = []  
weave (x:xs) (y:ys) = x:y:weave xs ys
```

- (b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

```
toMax [1,4,2,5,3] = [5,5,5,5,5]
```

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

```
toMax :: [Int] → [Int]  
toMax l = replicate (length l) max  
where max _ = foo l 0
```

Typeclass Definitions

```
class Semigroup a where
  (<>) :: a -> a -> a

class Semigroup m => Monoid m where
  mempty :: m

class Show a where
  show :: a -> String

class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool

class Eq a => Ord a where
  compare :: a -> a -> Ordering
  (<), (=), (>=), (>) :: a -> a -> Bool
  max, min :: a -> a -> a

class Functor f where
  fmap :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure :: a -> f a
  (<>*) :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return :: a -> m a
  (=>) :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary :: Gen a
  shrink :: a -> [a]

class Num a where
  (+), (-), (*) :: a -> a -> a
  negate :: a -> a
  abs :: a -> a
  signum :: a -> a
  fromInteger :: Integer -> a
```

Claude
Zou

CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
 (i) True
 (ii) False
- (b) The constraint `Semigroup a => Monoid a` implies that:
 (i) Every type that has a `Semigroup` instance, also has a `Monoid` instance.
 (ii) Every type that has a `Monoid` instance, also has a `Semigroup` instance.
 (iii) Both of the above.
 (iv) None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler.
 (i) True
 (ii) False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a `main` function:
 (i) The program will fail to typecheck.
 (ii) After typeclass resolution, the resulting program will use the Arbitrary instance for `Int` and `Char` to generate inputs and test `foo`.
 (iii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `()` as default to generate inputs and test `foo`.
 (iv) Haskell will require user-provided generators for integers and characters in order to run the tests

Part 2 - 12pts

The standard library defines `foldMap` with the following type:

```
foldMap :: (Monoid m, Foldable t) => (a -> m) -> t a -> m
```

For each of the following `foldMap` calls, select all options that are true:

- (a) `foldMap (:) [] [1..10]`
- (i) The expression will fail to typecheck.
 - (ii) The monoid in this call is `Int`.
 - (iii) The monoid in this call is `[Int]`.
 - (iv) The monoid in this call is `String`.
 - (v) The expression is equivalent to the identity function.
 - (vi) The foldable in this call is `[]` - the instance for lists.
- (b) `foldMap show "123456"`
- (i) The expression will fail to typecheck.
 - (ii) The monoid in this call is `Int`.
 - (iii) The monoid in this call is `[Int]`.
 - (iv) The monoid in this call is `String`.
 - (v) The expression is equivalent to the identity function.
 - (vi) The foldable in this call is `[]` - the instance for lists.

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or “ill-typed” if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

- (a) $\lambda x \rightarrow x$

Example answer:

$a \rightarrow a$

- (b) $\lambda x y \rightarrow (x, y)$

- (c) $\lambda x y \rightarrow \text{if } x == y \text{ then show } x \text{ else show } (x, y)$

$$(E_{\lambda} a) \Rightarrow a \rightarrow a \rightarrow \text{String}$$

- (d) $\lambda x_1 \rightarrow x_1 ++ 1 ++ [x]$

$$a \rightarrow [a] \rightarrow [a]$$

- (e) $\text{getLine} >= \text{putStrLn}$

IO()

- (f) $\text{putStrLn} 42 >= \text{putStrLn} 43$

ill typed

- (g) $(,) "42"$

a $\rightarrow (\text{String}, a)$

- (h) $\text{reverse} . \text{foldMap} \text{return}$

ill typed

- (i) $\lambda l \rightarrow [(x, y) | x < -1, y < -1, x / = y]$

$(E_{\lambda} a) \Rightarrow [a] \rightarrow [(\alpha, \alpha)]$

- (j) $\text{let } f x = x \text{ in } (f 'a', f \text{ True})$

$(\text{char}, \text{Bool})$

- (k) $\text{filterM} (\text{const} [\text{True}, \text{False}])$

$[a] \rightarrow [[a]]$

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix, dc syntax list comprehensions, or any valid Haskell.

- (a) $\text{Int} \rightarrow \text{Int}$

Example answers:

$$\lambda x \rightarrow x + 1$$

(+1)

- (b) $\text{Bool} \rightarrow [\text{Bool}]$

$$\lambda x \rightarrow [\neg x]$$

- (c) $a \rightarrow \text{Maybe } b$

$$\lambda x \rightarrow \text{Nothing}$$

- (d) $(\text{Int} \rightarrow \text{Char} \rightarrow \text{Bool}) \rightarrow [\text{Int}] \rightarrow [\text{Char}] \rightarrow [\text{Bool}]$

$$\lambda f \lambda L \rightarrow f \text{zipWith}$$

- (e) $(a \rightarrow b \rightarrow c) \rightarrow \text{IO } a \rightarrow \text{IO } b \rightarrow \text{IO } c$

$$\lambda f \lambda M2$$

- (f) $(a \rightarrow b) \rightarrow (b \rightarrow \text{Bool}) \rightarrow [a] \rightarrow [b]$

$$\lambda f1 \lambda f2 \lambda L \rightarrow f1 \text{filter} (\lambda x \rightarrow f2 x) L$$

- (g) $\text{Maybe } a \rightarrow (a \rightarrow \text{Gen } b) \rightarrow \text{Gen } (a, b)$

$$\lambda x \lambda f \rightarrow do a <- x, b <- f a, return (a, b)$$

- (h) $\text{Eq } a \Rightarrow a \rightarrow [a] \rightarrow [a]$

$$\lambda x \lambda L \rightarrow filter (\lambda y \rightarrow y == x) L$$

- (i) $\text{Show } a \Rightarrow [a] \rightarrow \text{IO String}$

$$\lambda x \lambda L \rightarrow pure (\text{Show } (head x))$$

- (j) $(a, b) \rightarrow (a \rightarrow b \rightarrow c) \rightarrow c$

$$\lambda f \lambda (a, b) \lambda f1 = f1 a b$$

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a) `foo :: [Int] -> [Int]`

```
foo l = [x * x | x <- l, x > 0 ]
```

Example answer:

Calculates the squares of all positive numbers in a list.

```
foo [] = []
foo [1,0,2,-1] = [1,4]
```

(b) `foo :: [Int] -> [Int]`

```
foo l = [ (x,y) | x <- l, y <- l, x /= y ]
```

Answer: tuples of all pairs in a list with all other non equal pairs in the list

(c) `foo :: a -> [a] -> [a]`

```
foo x l = reverse (x : reverse l)
```

Answer: append to end of list

(d) `bar :: (a -> Maybe b) -> [a] -> [b]`

```
bar f [] = []
let rs = bar f xs in
```

case f x of

Nothing -> rs

Just x -> x:rs

`foo :: [Maybe a] -> [a]`

`foo = bar id`

Answer: removes all nothing from a list and unwraps the Justs.

e.g. [Just 1, Nothing] -> [1]

(e) `foo :: [Int] -> Int -> (Int, [Int])`

```
foo [] m = (m, [])
foo [x] m = (x, [m])
```

```
foo (x : xs) m = (max m' x, m : xs')
```

```
where (m', xs') = foo xs m
```

Answer: returns a tuple of the max element of the list and a list of the same size with the second argument as the only element.

$[1, 3, 5] \quad 4 \rightarrow (5, [4, 4, 4])$

(f) Bonus!

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a].
dropWhileM _ [] = return []
dropWhileM p (x:xs) = do
    q <- p x
    if q then dropWhileM p xs else return (x:xs)
```

```
foo :: ??  
foo = dropWhileM (const [True, False])
```

Answer:

$[a] \rightarrow [[a]]$

return the powerset of a list

e.g. $[1, 0] \rightarrow [[], [1], [0], [1, 0]]$

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

`weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]`

You can assume that the lists have the same length.

`weave [] [] = []`

`weave (x:xs) (y:ys) = x: (y: (weave xs ys))`

`weave _ _ = undefined`

- (b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

`toMax [1,4,2,5,3] = [5,5,5,5,5]`

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

`toMax [] = []`

~~`toMax l = replicate (length l) (maximum l)`~~

Typeclass Definitions

```
class Semigroup a where
  (++) :: a -> a -> a

class Semigroup m => Monoid m where
  mempty :: m

class Show a where
  show :: a -> String

class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool

class Eq a => Ord a where
  compare :: a -> a -> Ordering
  (<), (<=), (=>), (>) :: a -> a -> Bool
  max, min :: a -> a -> a

class Functor f where
  fmap :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure :: a -> f a
  (<*>) :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return :: a -> m a
  (">>>=) :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary :: Gen a
  shrink :: a -> [a]

class Num a where
  (+), (-), (*) :: a -> a -> a
  negate :: a -> a
  abs :: a -> a
  signum :: a -> a
  fromInteger :: Integer -> a
```

GUIDO AMBASZ

CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
- (i) True
 (ii) False
- (b) The constraint `Semigroup a => Monoid a` implies that:
- (i) Every type that has a Semigroup instance, also has a Monoid instance.
 (ii) Every type that has a Monoid instance, also has a Semigroup instance.
 (iii) Both of the above.
 (iv) None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler. *(Assuming type checker ≠ compiler)*
- (i) True
 (ii) False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a main function:
- (i) The program will fail to typecheck.
 (ii) After typeclass resolution, the resulting program will use the Arbitrary instance for Int and Char to generate inputs and test `foo`.
 (iii) After typeclass resolution, the resulting program will use the Arbitrary instance for () as default to generate inputs and test `foo`.
 (iv) Haskell will require user-provided generators for integers and characters in order to run the tests

Part 2 - 12pts

The standard library defines `foldMap` with the following type:

```
foldMap :: (Monoid m, Foldable t) => (a -> m) -> t a -> m
```

For each of the following `foldMap` calls, select all options that are true:

(a) `foldMap (:) [] [1..10]`

- (i) The expression will fail to typecheck.
- (ii) The monoid in this call is `Int`.
- (iii) The monoid in this call is `[Int]`.
- (iv) The monoid in this call is `String`.
- (v) The expression is equivalent to the identity function.
- (vi) The foldable in this call is `[]` - the instance for lists.

(b) `foldMap show "123456"`

- (i) The expression will fail to typecheck.
- (ii) The monoid in this call is `Int`.
- (iii) The monoid in this call is `[Int]`.
- (iv) The monoid in this call is `String`.
- (v) The expression is equivalent to the identity function.
- (vi) The foldable in this call is `[]` - the instance for lists.

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or “ill-typed” if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

- (a) $\backslash x \rightarrow x$
Example answer:
 $a \rightarrow a$
- (b) $\backslash x y \rightarrow (x,y)$
 $a \rightarrow b \rightarrow (a,b)$
- (c) $\backslash x y \rightarrow \text{if } x == y \text{ then show } x \text{ else show } (x,y)$
 $a \rightarrow a \rightarrow \text{String}$
- (d) $\backslash x 1 \rightarrow x : 1 ++ 1 ++ [x]$
 $a \rightarrow [a] \rightarrow [a]$
- (e) `getLine >=> putStrLn`
 IO ()
- (f) `putStrLn 42 >>= putStrLn 43`
~~ill-typed~~
- (g) `(,) ""42"`
~~ill-typed~~ $a \rightarrow \text{String} \cdot a$
- (h) `reverse . foldMap return`
~~ill-typed~~ ~~function~~ $(\text{Foldable } c, \text{Monad } m) \Rightarrow t a \rightarrow m$
- (i) $\backslash l \rightarrow [(x,y) \mid x < -1, y < -1, x / y]$
 $\text{Eq } a \rightarrow [a] \rightarrow [(a,a)]$
- (j) `let f x = x in (f 'a', f True)`
~~ill-typed~~ $(\text{Char}, \text{Bool})$
- (k) `filterM (const [True, False])`
 $\text{Monad } m \rightarrow [a] \rightarrow m[a]$

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix, do syntax, list comprehensions, or any valid Haskell.

- (a) `Int -> Int`

Example answers.

(+1)

- (b) `Bool -> [Bool]`
 $\lambda b \rightarrow \text{if } b \text{ then } [b] \text{ else } [b]$

- (c) `a -> Maybe b`

$\lambda a \rightarrow \text{Nothing}$

- (d) `(Int -> Char -> Bool) -> [Int] -> [Char] -> [Bool]`
~~lambda x y z = x y z~~ ~~let m2 =~~ ~~head x~~ ~~head y~~ ~~head z~~ ~~m2~~

- (e) `(a -> b -> c) -> IO a -> IO b -> IO c`

$\lambda \rho \tau M_2$

- (f) `(a -> b) -> (b -> Bool) -> [a] -> [b]`
~~lambda f g =~~ ~~f g~~ $\lambda a \rightarrow \text{let } b = f (\text{head } a) \text{ in } \text{if } g b \text{ then } [b] \text{ else } [b]$

- (g) `Maybe a -> (a -> Gen b) -> Gen (a,b)`
~~lambda f =~~ $\lambda \text{ma } f \Rightarrow \text{arbitrary}((\text{fromJust ma}), F(\text{fromJust ma}))$

- (h) `Eq a => a -> [a] -> [a]`
 $\lambda a . \lambda a \Rightarrow \text{if } a == (\text{head } a) \text{ then } a \text{ else } [a]$

- (i) `Show a => [a] -> IO String`
 $\lambda a \rightarrow \text{return } (\text{Show } (\text{head } a))$

- (j) `(a,b) -> (a -> b -> c) -> c`

$\lambda (a,b) f \Rightarrow f a b$

~~QUESTION~~

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a) `foo :: [Int] -> [Int]`

`foo l = [x * x | x <- l, x > 0]`

Example answer:

Calculates the squares of all positive numbers in a list.

`foo [] = []`

`foo [1,0,2,-1] = [1, 4]`

(b) `foo :: [Int] -> [Int]`

`foo l = [(x,y) | x <- l, y <- l, x /= y]`

Answer: Returns a list with all pairs of integers that are not equal.

`foo [] = []`

~~foo~~ `foo [(1,2),(1,3),(2,1),(2,3),(3,1),(3,2)]`

`foo x l = reverse (x : reverse l)`

Answer: Appends an element to the end of the list.

`foo [] = []`

`foo [1,2,3] = [1,2,3,4]`

(d) `bar :: [a] -> [a]`

`bar [] = []`

`bar f (x:xs) =`

`let rs = bar f xs in`

`case f x of`

`Nothing -> rs`

`Just r -> r:rs`

`foo :: [Maybe a] -> [a]`

`foo = bar id`

Answer: Takes a list of maybes and returns a list with all values that are not Nothing.

`foo [] = []`

~~foo~~ `foo [Just 1, Just 2, Just 3] = [1,2,3]`

(e) `foo :: [Int] -> Int`

`foo [] m = (m, [])`

`foo [x] m = (x, [m])`

`foo (x : xs) m = (max m' x, m : xs')`

`where (m', xs') = foo xs m`

Answer: Returns a tuple with the maximum element of the list ~~first~~, the current head and the parameter m.

`foo [1,4,2] = (4, [3,4,3])`

`foo [] = (1, [])`

`foo [2] = (2, [1])`

~~ANSWER~~ `foo [1,2] = (2, [3,3])`

(f) Bonus!

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM _ [] = return []
dropWhileM p (x:xs) = do
```

```
    q <- p x
```

```
    if q then dropWhileM p xs else return (x:xs)
```

```
foo :: ?? [a] -> m [a]
```

```
foo = dropWhileM (const [True, False])
```

Answer: This will just return the empty list. ~~wrapped in a~~

~~dropWhileM~~

foo [] = []

foo [1,2,3] = []

foo ["hope", "im", "right"] = []

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

```
weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]
```

You can assume that the lists have the same length.

```
weave [] [] = []
weave [x] [y] = [x,y]
weave xs ys = weave xs ys ++ (weave xs ys)
```

- (b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

```
toMax [1,4,2,5,3] = [5,5,5,5,5]
```

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

```
traverse -- Should only traverse once.
toMax lst = maximum
           let max = maximum lst in
repeat take (length lst) (repeat max)
```

```
-- without bonus.
toMax lst = maximum
let m = max lst in
repeat
map (\_ -> m) lst
```

Typeclass Definitions

```
class Semigroup a where
  (++) :: a -> a -> a

class Semigroup m => Monoid m where
  mempty :: m

class Show a where
  show :: a -> String

class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool

class Eq a => Ord a where
  compare :: a -> a -> Ordering
  (<), (==), (>=), (>) :: a -> a -> Bool
  max, min :: a -> a -> a

class Functor f where
  fmap :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure :: a -> f a
  (*>) :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return :: a -> m a
  (=>) :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary :: Gen a
  shrink :: a -> [a]

class Num a where
  (+), (-), (*) :: a -> a -> a
  negate :: a -> a
  abs :: a -> a
  signum :: a -> a
  fromInteger :: Integer -> a
```

Gregor Wolff

CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
 - (i) True
 - (ii) False
- (b) The constraint `Semigroup a => Monoid a` implies that:
 - (i) Every type that has a `Semigroup` instance, also has a `Monoid` instance.
 - (ii) Every type that has a `Monoid` instance, also has a `Semigroup` instance.
 - (iii) Both of the above.
 - (iv) None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler.
 - (i) True
 - (ii) False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a `main` function:
 - (i) The program will fail to typecheck.
 - (ii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `Int` and `Char` to generate inputs and test `foo`.
 - (iii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `()` as default to generate inputs and test `foo`.
 - (iv) Haskell will require user-provided generators for integers and characters in order to run the tests

Part 2 - 12pts

The standard library defines `foldMap` with the following type:

```
foldMap :: (Monoid m, Foldable t) => (a -> m) -> t a -> m
```

For each of the following `foldMap` calls, select all options that are true:

(a) `foldMap (:) [] [1..10]`

(i) The expression will fail to typecheck.

(ii) The monoid in this call is `Int`.

(iii) The monoid in this call is `[Int]`.

(iv) The monoid in this call is `String`.

(v) The expression is equivalent to the identity function.

(vi) The foldable in this call is `[]` - the instance for lists.

(b) `foldMap show "123456"`

(i) The expression will fail to typecheck.

(ii) The monoid in this call is `Int`.

(iii) The monoid in this call is `[Int]`.

(iv) The monoid in this call is `String`.

(v) The expression is equivalent to the identity function.

(vi) The foldable in this call is `[]` - the instance for lists.

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or “well-typed” if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

(a) $\lambda x \rightarrow x$

Example answer:

$a \rightarrow a$

(b) $\lambda x y \rightarrow (x,y)$

$a \rightarrow b \rightarrow (a,b)$

(c) $\lambda x y \rightarrow \text{if } x == y \text{ then show } x \text{ else show } (x,y)$

$E^a \rightsquigarrow \text{Show } a \Rightarrow a \rightarrow a \rightarrow \text{String}$

(d) $\lambda x _ \rightarrow x : 1 ++ 1 ++ [x]$

$[a] \Rightarrow a \rightarrow [a]$

(e) $\text{getLine} >= \text{putStrLn}$

$IO ()$

(f) $\text{putStrLn} 42 >>= \text{putStrLn} 43$

ill typed

(g) $(,)''42''$

$a \Rightarrow ([c] a), a)$

(h) $\text{reverse}, \text{foldMap}, \text{return}$

$[a] \rightarrow [a]$

(i) $\lambda l \rightarrow [(x,y) \mid x <- 1, y <- 1, x /= y]$

$[c] \rightarrow [[a, a]]$

(j) $\text{let } f x = x \text{ in } (f a', f \text{ True})$

$([d] a'), B \otimes 1$

(k) $\text{filterM} (\text{const} [\text{True}, \text{False}])$

$[a] \rightarrow [[a]]$

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix, do syntax, list comprehensions, or any valid Haskell.

(a) `Int -> Int`

Example answers:

$\lambda x \rightarrow x + 1$

(+1)

(b) `Bool -> [Bool]`

`return`

(c) `a -> Maybe b`

`undefined`

(d) `(Int -> Char -> Bool) -> [Int] -> [Char] -> [Bool]`

`filterM`

(e) `(a -> b -> c) -> IO a -> IO b -> IO c`

`liftIO`

(f) `(a -> b) -> (b -> Bool) -> [a] -> [b]`

`let g | filter g $ map f |`

(g) `Maybe a -> (a -> Gen b) -> Gen (a,b)`

`undefined`

(h) `Eq a => a -> [a] -> [a]`

`\x I -> filter (== x) I`

(i) `Show a => [a] -> IO String`

`return $ foldMap show`

(j) `(a,b) -> (a -> b -> c) -> c`

$\lambda x \rightarrow \text{uncurry } g \ x$

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a)

```
foo :: [Int] -> [Int]
foo l = [ x * x | x <- 1, x > 0 ]
```

Example answer:

Calculates the squares of all positive numbers in a list.

(b)

```
foo :: [Int] -> [Int]
```

```
foo 1 = [ (x,y) | x <- 1, y <- 1, x /= y ]
```

Answer:

Returns all pairs of elements that differ from each other

(c)

```
foo :: [Int] -> [(Int, Int)]
foo l = reverse (x : reverse l)
```

Answer:

Adds `x` to end of list

foo 3 [1,2] = [1,2,3]

(d)

```
bar :: (a -> Maybe b) -> [a] -> [b]
```

```
bar f (x:xs) =
```

```
let rs = bar f xs in
```

```
case f x of
```

```
Nothing -> rs
```

```
Just r -> r:rs
```

```
foo :: [Maybe a] -> [a]
```

Answer:

Removes all `Nothing`s and "un-`Just`"s the remaining ones

foo [Just 1, Just 2, Nothing, Just 3] = [1,2,3]

(e)

```
foo :: [Int] -> Int -> (Int, [Int])
```

```
foo [] m = (m, [])
```

```
foo [x] m = (x, [m])
```

```
foo (x : xs) m = (max m' x, m : xs')
```

```
where (m', xs') = foo xs m
```

Answer:

Extracts the max element,
replaces each element w/ m
and returns the tuple
containing the

(max elem, new list)

(4, [2, 2, 2])

$\begin{array}{c} \text{foo } [4] \\ \downarrow \\ (4, []) \end{array}$

$\begin{array}{c} \text{foo } [4, [2]] \\ \downarrow \\ (4, [2]) \end{array}$

$\begin{array}{c} \text{foo } [4, [2, 2]] \\ \downarrow \\ (4, [2, 2, 2]) \end{array}$

(f) Bonus!

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM _ [] = return []
dropWhileM p (x:xs) = do
    q <- p x
    if q then dropWhileM p xs else return (x:xs)
```

```
foo :: ??[c] -> [[c]]
foo = dropWhileM (const [True, False])
```

Answer:

Equivalent to tails (the "true" branch drops the element and continues, the "false" branch stops the computation)

foo [1,2,3] =

[[], [2,3], [3], []]

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

```
weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]
```

You can assume that the lists have the same length.

```
weave x y = concatMap (uncurry (:) ) $ zip x y
```

- (b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

```
toMax [1,4,2,5,3] = [5,5,5,5,5]
```

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

```
toMax x = map (const $ maximum x) x
```

BONNS

```
toMax (x:xs) = snd $ f x (x:xs) where
    f [] [] = (x, [])
    f (a:(y:ys)) (q, q:(qs)) where
        (q1, qs) = f (max a y) qs
```

Typeclass Definitions

```
class Semigroup a where
  (++) :: a -> a -> a

class Semigroup m => Monoid m where
  mempty :: m

class Show a where
  show :: a -> String

class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool

class Eq a => Ord a where
  compare :: a -> a -> Ordering
  (<), (=<), (=>), (>) :: a -> a -> Bool
  max, min :: a -> a -> a

class Functor f where
  fmap :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure :: a -> f a
  (<>*) :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return :: a -> m a
  (=>) :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary :: Gen a
  shrink :: a -> [a]

class Num a where
  (+), (-), (*) :: a -> a -> a
  negate :: a -> a
  abs :: a -> a
  signum :: a -> a
  fromInteger :: Integer -> a
```

Garrett Hill

CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
 (i) True *lawy*
 (ii) False
- (b) The constraint `Semigroup a => Monoid a` implies that:
 (i) Every type that has a `Semigroup` instance, also has a `Monoid` instance.
 (ii) Every type that has a `Monoid` instance, also has a `Semigroup` instance.
 (iii) Both of the above.
 (iv) None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler.
 (i) True
 (ii) False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a `main` function:
 (i) The program will fail to typecheck.
 (ii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `Int` and `Char` to generate inputs and test `foo`.
 (iii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `()` as default to generate inputs and test `foo`.
 (iv) Haskell will require user-provided generators for integers and characters in order to run the tests

Part 2 - 12pts

The standard library defines `foldMap` with the following type:

```
foldMap : (Monoid m, Foldable t) => (a -> m) -> t a -> m
```

For each of the following `foldMap` calls, select all options that are true:

(a) `foldMap ([]) [1..10]`

(i) The expression will fail to typecheck.

(ii) The monoid in this call is `Int`.

(iii) The monoid in this call is `[Int]`.

(iv) The monoid in this call is `String`.

(v) The expression is equivalent to the identity function.

(vi) The foldable in this call is `[]` - the instance for lists.

(b) `foldMap show "123456"`

(i) The expression will fail to typecheck.

(ii) The monoid in this call is `Int`.

(iii) The monoid in this call is `[Int]`.

(iv) The monoid in this call is `String`.

(v) The expression is equivalent to the identity function.

(vi) The foldable in this call is `[]` - the instance for lists.

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or “ill-typed” if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

(a) $\backslash x \rightarrow x$

Example answer:

$a \rightarrow a$

(b) $\backslash x y \rightarrow (x,y)$

$a \rightarrow b \rightarrow (a,b)$

(c) $\backslash x y \rightarrow \text{if } x > y \text{ then show } x \text{ else show } (x,y)$

~~Eq a~~ $\rightarrow a \rightarrow a \rightarrow \text{String}$

(d) $\backslash x _1 \rightarrow x ; 1 ++ 1 ++ [x]$

$a \rightarrow [a] \rightarrow [a]$

(e) $\text{getLine} >>= \text{putStrLn}$

~~IO()~~ $\text{IO} \rightarrow \text{IO}$

(f) $\text{putStrLn} 42 >> \text{putStrLn} 43$

: ill typed

(g) $(,) "42"$

; ill typed

(h) $\text{reverse} . \text{foldMap} \text{return}$

$(\text{Foldable } k, \text{Monoid } m) \Rightarrow k \rightarrow [m]$

(i) $\backslash l \rightarrow [(x,y) | x < -1, y < -1, x / = y]$

~~Eq a~~ $\rightarrow a \rightarrow [a]$

(j) $\text{let } f x = x \text{ in } (f `a`, f \text{ True})$

$C Char, Bool$

(k) $\text{filterM} (\text{const } [\text{True}, \text{False}])$

~~Eq a~~ $\rightarrow a$

Foldable $\vdash = \vdash a \rightarrow \vdash a$

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix, do syntax, list comprehensions, or any valid Haskell.

- (a) $\text{Int} \rightarrow \text{Int}$

Example answers:

$$\lambda x \rightarrow x + 1$$

(+1)

- (b) $\text{Bool} \rightarrow [\text{Bool}]$
 $\lambda x \rightarrow \text{if } x \text{ then } [x] \text{ else } []$

- (c) $a \rightarrow \text{Maybe } b$
 $\lambda x \rightarrow \text{Nothing}$

- (d) $(\text{Int} \rightarrow \text{Char} \rightarrow \text{Bool}) \rightarrow [\text{Int}] \rightarrow [\text{Char}] \rightarrow [\text{Bool}]$
 ~~$\lambda f : \lambda i : \lambda c : \lambda b : f i c \rightarrow f i b$~~
 $\lambda f : \lambda i : \lambda c : \lambda b : f i c \rightarrow f i b$

- (e) $(a \rightarrow b \rightarrow c) \rightarrow \text{IO } a \rightarrow \text{IO } b \rightarrow \text{IO } c$

- ~~$\lambda f : \lambda a : \lambda b : \lambda c : f a b \rightarrow f a c$~~
 $\lambda f : \lambda a : \lambda b : f a b \rightarrow f a c$

- (f) $(a \rightarrow b) \rightarrow (b \rightarrow \text{Bool}) \rightarrow [a] \rightarrow [b]$
 ~~$\lambda f : \lambda g : \lambda a : \lambda b : f a \rightarrow g f a \rightarrow g f b$~~
 $\lambda f : \lambda g : \lambda a : \lambda b : f a \rightarrow g f a \rightarrow g f b$

- (g) $\text{Maybe } a \rightarrow (a \rightarrow \text{Gen } b) \rightarrow \text{Gen } (a, b)$
 ~~$\lambda f : \lambda a : \lambda g : \lambda b : f a \rightarrow g f a \rightarrow g f b$~~
 $\lambda f : \lambda a : \lambda g : \lambda b : f a \rightarrow g f a \rightarrow g f b$

- (h) $\text{Eq } a \Rightarrow a \rightarrow [a]$
 ~~$\lambda f : \lambda a : \lambda b : f a = f b \rightarrow a = b$~~
 $\lambda f : \lambda a : \lambda b : f a = f b \rightarrow a = b$

- (i) $\text{Show } a \Rightarrow [a] \rightarrow \text{IO String}$
 ~~$\lambda f : \lambda a : \lambda s : f a \rightarrow s$~~
 $\lambda f : \lambda a : \lambda s : f a \rightarrow s$

- (j) $(a, b) \rightarrow (a \rightarrow b \rightarrow c) \rightarrow c$
 ~~$\lambda f : \lambda g : \lambda h : f (g h) = h$~~
 $\lambda f : \lambda g : \lambda h : f (g h) = h$

$$\lambda f : \lambda g : \lambda h : f (g h) = h$$

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a) `foo :: [Int] -> [Int]`

`foo 1 = [x * x | x <- 1, x > 0]`

Example answer:

Calculates the squares of all positive numbers in a list.

`foo [] = []`

`foo [1,0,2,-1] = [1, 4]`

(b)

`foo :: [Int] -> [Int]`

`foo 1 = [(x,y) | x <- 1, y <- 1, x /= y]`

Answer: ~~for every x, y pair in then return the list of all (x,y) pairs for foo 1 = C~~

(c)

`foo :: a -> [a] -> [a]`

`foo x 1 = reverse (x : reverse 1)`

Answer: ~~reverses~~ appends x to 1

`foo [C] = [A]`

`foo 2 [1,3,4] = [1,3,4,2]`

(d)

`bar :: (a -> Maybe b) -> [a] -> [b]`

`bar f (x:xs) =`

`let rs = bar f xs in`

`case f x of`

`Nothing -> rs`

`Just r -> r:rs`

`foo :: [Maybe a] -> [a]`

`foo = bar id`

`foo [C] = C`

`foo [Nothing] = C`

(e) `foo :: [Int] -> Int -> (Int, [Int])`

`foo [] m = (m, [])`

`foo [x] m = (x, [m])`

`foo (x : xs) m = (max m' x, m : xs')`

`where (m', xs') = foo xs m`

Answer: ~~replaces the highest value in the list with m~~

Replaces all values lower than m with m

`foo [0,1,2,3] 2 = [2,2,2,3]`

`foo [3,4,5,6] 2 = [3,4,5,6]`

(f) Bonus!

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM _ □ = return []
dropWhileM p (x:xs) = do
    q <- p x
    if q then dropWhileM p xs else return (x:xs)
```

foo :: ?? $\text{C}[\text{a}] \rightarrow \text{M}[\text{a}]$

foo = dropWhileM (const [True, False])

Answer: Returns the list of all possible tails of a given list

foo [] = [[]]

foo [1,2] = [[1,2], [2], []]

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

```
weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]
```

You can assume that the lists have the same length.

`weave (x:xs) (y:ys) = x:y:(weave xs ys)`

`weave [] [] = []`

- (b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

```
toMax [1,4,2,5,3] = [5,5,5,5,5]
```

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

~~toMax c = []~~
~~toMax l = foo (maximum l)~~

maximum

Typeclass Definitions

```
class Semigrcup a where
  (<>) :: a -> a -> a

class Semigrcup m => Monoid m where
  mempty :: m

class Show ē where
  show :: ē -> String

class Eq a where
  (==) :: ē -> a -> Bool
  (/=) :: ē -> a -> Bool

class Eq a => Ord a where
  compare :: a -> a -> Ordering
  (⟨), (≤), (≥), (⟩) :: a -> a -> Bool
  max, min :: a -> a -> a

class Functor f where
  fmap :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure :: a -> f a
  (⟨*>) :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return :: a -> m a
  (⟨>=) :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary :: Gen a
  shrink :: a -> [a]

class Num a where
  (+), (-), (*) :: a -> a -> a
  negate :: a -> a
  abs :: a -> a
  signum :: a -> a
  fromInteger :: Integer -> a
```

Talha Muhid

CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
 (i) True
 (ii) False
- (b) The constraint `Semigroup a => Monoid a` implies that:
 (i) Every type that has a `Semigroup` instance, also has a `Monoid` instance.
 (ii) Every type that has a `Monoid` instance, also has a `Semigroup` instance.
 (iii) Both of the above.
 (iv) None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler.
 (i) True
 (ii) False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a `main` function:
 (i) The program will fail to typecheck.
 (ii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `Int` and `Char` to generate inputs and test `foo`.
 (iii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `()` as default to generate inputs and test `foo`.
 (iv) Haskell will require user-provided generators for integers and characters in order to run the tests

Part 2 - 12pts

The standard library defines `foldMap` with the following type:

```
foldMap :: (Monoid m, Foldable t) => (a -> m) -> t a -> m
```

For each of the following `foldMap` calls, select all options that are true:

- (a) `foldMap ([]) [1..10]`
- (i) The expression will fail to typecheck.
 - (ii) The monoid in this call is `Int`.
 - (iii) The monoid in this call is `[Int]`.
 - (iv) The monoid in this call is `String`.
 - (v) The expression is equivalent to the identity function.
 - (vi) The foldable in this call is `[]` - the instance for lists.
- (b) `foldMap show "123456"`
- (i) The expression will fail to typecheck.
 - (ii) The monoid in this call is `Int`.
 - (iii) The monoid in this call is `[Int]`.
 - (iv) The monoid in this call is `String`.
 - (v) The expression is equivalent to the identity function.
 - (vi) The foldable in this call is `[]` - the instance for lists.

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or “ill-typed” if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

- (a) $\lambda x \rightarrow x$
Example answer:
 $a \rightarrow a$
- (b) $\lambda x y \rightarrow (x,y)$
- $a \rightarrow b \rightarrow [a, b]$
- (c) $\lambda x y \rightarrow \text{if } x == y \text{ then show } x \text{ else show } (x,y)$
ill-typed
- (d) $\lambda x l \rightarrow x : l ++ 1 ++ [x]$
- $a \rightarrow [a] \rightarrow [a]$
- (e) `getLine >>= putStrLn`
- Applicative IO => Monad IO**
ill-typed
- (f) `putStrLn "42" >>= putStrLn "43"`
- (g) $\lambda () \rightarrow$
Char \rightarrow $(Char, Char) \rightarrow String$
- (h) `reverse . foldMap return`
 $- [a] \rightarrow [a]$
- (i) $\lambda l \rightarrow [[x,y] \mid x < -l, y < -l, x /= y]$
 $[a] \rightarrow [(a, a)]$
- (j) `let f x = x in (f 'a', f True)`
ill-typed
- (k) `filterM (const [True, False])`
 $[a] \rightarrow [[a]]$

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix, do syntax, list comprehensions, or any valid Haskell.

- (b) $\text{Bool} \rightarrow [\text{Bool}]$
 $\lambda x \rightarrow \text{if } x \text{ Then } [\text{True}] \text{ else } [\text{False}]$

(c) $a \rightarrow \text{Maybe } b$

Monad maybe $\Rightarrow (\gg=)$

(d) $(\text{Int} \rightarrow \text{Char} \rightarrow \text{Bool}) \rightarrow [\text{Int}] \rightarrow [\text{Char}] \rightarrow [\text{Bool}]$
 $\text{liftM2 } (\lambda h \rightarrow \text{True}) \text{ list1 list2}$

(e) $(a \rightarrow b \rightarrow c) \rightarrow \text{IO } a \rightarrow \text{IO } b \rightarrow \text{IO } c$
 $\text{liftM2 } f \text{ list1 list2 : underlined}$

(f) $(a \rightarrow b) \rightarrow (b \rightarrow \text{Bool}) \rightarrow [a] \rightarrow [b]$
 $\text{liftM2 } f \text{ list } \rightarrow \text{map } f \text{ list}$

(g) $\text{Maybe } a \rightarrow (a \rightarrow \text{Gen } b) \rightarrow \text{Gen } (a, b)$
 $\text{liftM } f \rightarrow \underline{\text{undefined}}$

(h) $\text{Eq } a \Rightarrow a \rightarrow [a] \rightarrow [a]$
 $\text{liftM } f \text{ a } (\lambda t \rightarrow \text{if } \text{Eq } a \text{ Then } a \text{ else } \text{unit } t) \rightarrow \text{if } \text{Eq } a \text{ Then } a \text{ else } \text{unit } t$

(i) Show $a \Rightarrow [a] \rightarrow \text{IO String}$
 $\text{liftM } f \text{ a } (\lambda t \rightarrow \text{getLine})$

(j) $(a, b) \rightarrow (a \rightarrow b \rightarrow c) \rightarrow c$

$\text{liftM2 } f \text{ a } b \rightarrow \text{unit } f \text{ a } b$

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a) `foo :: [Int] -> [Int]`
`foo l = [x * x | x <- l, x > 0]`

Example answer:

Calculates the squares of all positive numbers in a list.

`foo [] = []`

`foo [1,0,2,-1] = [1, 4]`

(b) `foo :: [Int] -> [Int]`
`foo l = [(x,y) | x <- l, y <- l, x /= y]`

Answer:

Make a list of tuples where no tuple has duplicates

(c) `foo :: a -> [a] -> [a]`
`foo x l = reverse (x : reverse l)`

Answer:

Reverse l, then prepend x, then reverse again

(d) `bar :: (a -> Maybe b) -> [a] -> [b]`
`bar f [] = []`
`bar f (x:xs) =`
`let rs = bar f xs in`

`case f x of`

`Nothing -> rs`

`Just r -> r:rs`

`foo :: [Maybe a] -> [a]`

Answer:

Filter out elements that result to Nothing and passed into f

(e) `foo :: [Int] -> Int -> (Int, [Int])`
`foo [] m = (m, [])`
`foo [x] m = (x, [m])`
`foo (x : xs) m = (max m' x, m : xs')`
`where (m', xs') = foo xs m`

Answer:

Return a tuple where the first element is the max of the list, and the second element is a list of m

(f) Bonus!

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM [] = return []
dropWhileM p (x:xs) = do
    q <- p x
    if q then dropWhileM p xs else return (x:xs)
```

```
foo :: ?? [ ] -> [ ]
foo = dropWhileM (const [True, False])
```

Answer:

dropWhileM p xs = liftM (filter p)

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

```
weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]
```

You can assume that the lists have the same length.

```
weave [] [] = []
weave (h:t) (h':t') = h:(h':(weave t t'))
```

- (b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

```
toMax [1,4,2,5,3] = [5,5,5,5,5]
```

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

```
toMax list = let m = maximum list in map (\h → m) list
```

Answers:

```
toMaxAux :: [a] → [a] → [a]
toMaxAux [] t = []
toMaxAux (h:t) t' = let m = if h > h' then [h] else [h',]
                     (toMaxAux t m) ++ m
```

Typeclass Definitions

```
class Semigroup a where
  (<>)
    :: a -> a -> a

class Semigroup m => Monoid m where
  mempty :: m

class Show a where
  show :: a -> String

class Eq a where
  (==)
    :: a -> a -> Bool
  (/=)
    :: a -> a -> Bool

class Eq a => Crd a where
  ccompare :: a -> a -> Ordering
  (<), (=<), (>=), (>)
    :: a -> a -> Bool
  max, min
    :: a -> a -> a

class Functor f where
  fmap
    :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure
    :: a -> f a
  (*>)
    :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return
    :: a -> m a
  (=>)
    :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary
    :: Gen a
  shrink
    :: a -> [a]

class Num a where
  (+), (-), (*)
    :: a -> a -> a
  negate
    :: a -> a
  abs
    :: a -> a
  signum
    :: a -> a
  fromInteger
    :: Integer -> a
```

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CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

- (a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.
- (i) True
- (ii) False
- (b) The constraint `Semigroup a => Monoid a` implies that:
- (i) Every type that has a `Semigroup` instance, also has a `Monoid` instance.
- (ii) Every type that has a `Monoid` instance, also has a `Semigroup` instance.
- (iii) Both of the above.
- (iv) None of the above.
- (c) Typeclass laws are enforced by the Haskell compiler.
- (i) True
- (ii) False
- (d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a `main` function:
- (i) The program will fail to typecheck.
- (ii) After typeclass resolution, the resulting program will use the Arbitrary instance for `Int` and `Char` to generate inputs and test `foo`.
- (iii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `()` as default to generate inputs and test `foo`.
- (iv) Haskell will require user-provided generators for integers and characters in order to run the tests

Part 2 - 12pts

The standard library defines `foldMap` with the following type:

```
foldMap :: (Monoid m, Foldable t) => (a -> m) -> t a -> m
```

For each of the following `foldMap` calls, select all options that are true:

- (a) `foldMap (:) [] [1..10]`
- (i) The expression will fail to typecheck.
 - (ii) The monoid in this call is `Int`.
 - (iii)** The monoid in this call is `[Int]`.
 - (iv) The monoid in this call is `String`.
 - (v)** The expression is equivalent to the identity function.
 - (vi)** The foldable in this call is `[]` - the instance for lists.
- (b) `foldMap show "123456"`
- (i) The expression will fail to typecheck.
 - (ii) The monoid in this call is `Int`.
 - (iii) The monoid in this call is `[Int]`.
 - (iv)** The monoid in this call is `String`.
 - (v)** The expression is equivalent to the identity function.
 - (vi)** The foldable in this call is `[]` - the instance for lists.

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or “ill-typed” if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

(a) $\backslash x \rightarrow x$

Example answer:
 $a \rightarrow a$

(b) $\backslash x y \rightarrow (x,y)$

(c) $\backslash x y \rightarrow \text{if } x == y \text{ then show } x \text{ else show } (x,y)$

Show a $\Rightarrow a \rightarrow a \rightarrow \text{String}$

(d) $\backslash x l \rightarrow x : l ++ 1 ++ [x]$

$a \rightarrow [a] \rightarrow [a]$

(e) $\text{getLine} >>= \text{putStrLn}$

String $\rightarrow \text{IO String} \rightarrow \text{IO ()}$

(f) $\text{putStrLn} 42 >>= \text{putStrLn} 43$

IO()

(g) $(,) "42"$

$a \rightarrow (a, \text{String})$

(h) $\text{reverse} . \text{foldMap} \text{return}$

Monad m $\Rightarrow [a] \rightarrow m a$

(i) $\backslash l \rightarrow [(x,y) \mid x < -1, y < -1, x /= y]$

Ord a $\Rightarrow a \rightarrow [(a,a)]$

(j) let f x = x in (f 'a', f True)

(Char, Bool)

(k) $\text{filterM} (\text{const} [\text{True}, \text{False}])$

Monad m $\Rightarrow [a] \rightarrow m [a]$

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix, do syntax, list comprehensions, or any valid Haskell.

- (a) $\text{Int} \rightarrow \text{Int}$

Example answers:

$\lambda x \rightarrow x + 1$

(+1)

- (b) $\text{Bool} \rightarrow [\text{Bool}]$

$\lambda x \rightarrow \text{replicate } 5 x$

- (c) $\text{a} \rightarrow \text{Maybe b}$

Just

- (d) $(\text{Int} \rightarrow \text{Char} \rightarrow \text{Bool}) \rightarrow [\text{Int}] \rightarrow [\text{char}] \rightarrow [\text{Bool}]$

$\lambda x \psi \rightarrow x > 0 \& \& \psi = !a$

- (e) $(\text{a} \rightarrow \text{b} \rightarrow \text{c}) \rightarrow \text{IO a} \rightarrow \text{IO b} \rightarrow \text{IO c}$

let A2

- (f) $(\text{a} \rightarrow \text{b}) \rightarrow (\text{b} \rightarrow \text{Bool}) \rightarrow [\text{a}] \rightarrow [\text{b}]$

$\lambda f g \lambda \rightarrow \text{foldr } (g \cdot f) [] \lambda$

- (g) $\text{Maybe a} \rightarrow (\text{a} \rightarrow \text{Gen b}) \rightarrow \text{Gen}^{(\text{a}, \text{b})}$

$\lambda f \rightarrow \lambda a. \lambda e. \lambda x. f e x$

- (h) $\text{Eq a} \Rightarrow \text{a} \rightarrow [\text{a}] \rightarrow \text{case } \lambda \rightarrow \text{of } \lambda c_1 \rightarrow [] \rightarrow \text{if } x = h \text{ then } r \text{ else } [x]$

- (i) $\text{Show a} \Rightarrow [\text{a}] \rightarrow \text{IO String}$

$\lambda x \rightarrow \text{case } \lambda of \lambda c_1 \rightarrow \text{do } getLine$

$c_1 \rightarrow \text{do } putStrLn h$

- (j) $(\text{a}, \text{b}) \rightarrow (\text{a} \rightarrow \text{b} \rightarrow \text{c}) \rightarrow \text{c}$

$\lambda (x, y) \rightarrow f x y$

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a)

```
foo :: [Int] -> [Int]
```

```
foo l = [ x * x | x <- l, x > 0 ]
```

Example answer:

Calculates the squares of all positive numbers in a list.

```
foo [] = []
```

```
foo [1,0,2,-1] = [1, 4]
```

(b)

```
foo :: [Int] -> [Int]
```

```
foo l = [ (x,y) | x <- l, y <- l, x /= y ]
```

Answer: Constructs all pairs of non-equal ints in a list.

```
foo [1,2] = [(1,2), (2,1)]
```

(c)

```
foo :: a -> [a] -> [a]
```

```
foo x l = reverse (x : reverse l)
```

Answer: Adds an element to the end of a list

```
foo 3 [1, 2] = [1, 2, 3]
```

```
foo 'c' "abc" = "abc"
```

(d)

```
bar :: (a -> Maybe b) -> [a] -> [b]
```

```
bar f [] = []
```

```
bar f (x:xs) =
```

```
let rs = bar f xs in
```

```
case f x of
```

```
Nothing -> rs
```

```
Just r -> r:rs
```

```
foo :: [Maybe a] -> [a]
```

```
foo = bar id
```

Answer: Removes 'None' maybe monad from a list.

```
foo [Nothing] = [],
```

```
foo [Maybe 2, Nothing, Maybe 4] = [2,4]
```

```
foo [] = []
```

```
foo :: [Int] -> Int -> (Int, [Int])
```

```
foo [] m = (m, [])
```

```
foo [x] m = (x, [m])
```

```
foo (x : xs) m = (max m' x, m : xs')
```

```
where (m', xs') = foo xs m
```

Answer: On non-empty list, replace all elements of the list with m and return (largest element in list, list of m). On empty list, return (m, []).

```
foo [] x = (x, [])
```

```
foo [2,4,3] 5 = (5, [5,5,5])
```

(f) *Bonus!*

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM _ [] = return []
dropWhileM p (x:xs) = do
    q <- p x
    if q then dropWhileM p xs else return (x:xs)
```

foo :: ??

foo = dropWhileM (const [True, False])

Answer: Drops elements from the start of the list, each with a 50% chance, and stops when an element is not dropped.

Example:
[1,2,3] could be const [1,2,3]
or const [3]
but not const [2]

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

- (a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

```
weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]
```

You can assume that the lists have the same length.

```
Weave [] [] = []
weave (x:xs) (y:ys) = x:y:(weave xs ys)
weave _ _ = error "if lists not same length"
```

- (b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

```
toMax [1,4,2,5,3] = [5,5,5,5,5]
```

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

```
toMax xs = replicate (length xs) (maximum xs)
```

Typeclass Definitions

```
class Semigroup a where
  (<>)
    :: a -> a -> a

class Semigroup m => Monoid m where
  mempty :: m

class Show a where
  show :: a -> String

class Eq a where
  (==)
    :: a -> a -> Bool
  (/=)
    :: a -> a -> Bool

class Eq a => Ord a where
  compare :: a -> a -> Ordering
  (<), (=<), (=>), (>) :: a -> a -> Bool
  max, min :: a -> a -> a

class Functor f where
  fmap :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure :: a -> f a
  (<>*)
    :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return :: a -> m a
  (=>)
    :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary :: Gen a
  shrink :: a -> [a]

class Num a where
  (+), (-), (*)
    :: a -> a -> a
  negate
    :: a -> a
  abs
    :: a -> a
  signum
    :: a -> a
  fromInteger
    :: Integer -> a
```