Typeclass Definitions

```
class Semigroup a where
  (<>)   :: a -> a -> a

class Semigroup m => Monoid m where
  mempty :: m

class  Show a  where
  show   :: a   -> String

class  Eq a  where
  (==)   :: a -> a -> Bool
  (/=)   :: a -> a -> Bool

class Eq a => Ord a where
  compare :: a -> a -> Ordering
  (<), (<=), (>=), (>) :: a -> a -> Bool
  max, min             :: a -> a -> a

class Functor f where
  fmap   :: (a -> b) -> f a -> f b

class Functor f => Applicative f where
  pure   :: a -> f a
  (<*>)  :: f (a -> b) -> f a -> f b

class Applicative m => Monad m where
  return :: a -> m a
  (>>=)  :: m a -> (a -> m b) -> m b

class Foldable t where
  foldMap :: Monoid m => (a -> m) -> t a -> m

class Arbitrary a where
  arbitrary :: Gen a
  shrink    :: a -> [a]

class Num a where
  (+), (-), (*)       :: a -> a -> a
  negate              :: a -> a
  abs                 :: a -> a
  signum              :: a -> a
  fromInteger         :: Integer -> a
```

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CMSC 488B: Midterm Exam (Spring 2022)

Question 1 (20 points)

Part 1 - 8pts

For each of the following questions, select the appropriate response.

(a) There exist OCaml programs that don't terminate, whose Haskell equivalents do terminate.

(i) True

(ii) False

(b) The constraint `Semigroup a => Monoid a` implies that:

(i) Every type that has a `Semigroup` instance, also has a `Monoid` instance.

(ii) Every type that has a `Monoid` instance, also has a `Semigroup` instance.

(iii) Both of the above.

(iv) None of the above.

(c) Typeclass laws are enforced by the Haskell compiler.

(i) True

(ii) False

(d) Given a function `foo :: Int -> Char -> Bool`, consider the function call `quickCheck foo`. Select what will happen if that was inside a `main` function:

(i) The program will fail to typecheck.

(ii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `Int` and `Char` to generate inputs and test `foo`.

(iii) After typeclass resolution, the resulting program will use the `Arbitrary` instance for `()` as default to generate inputs and test `foo`.

(iv) Haskell will require user-provided generators for integers and characters in order to run the tests

Part 2 - 12pts

The standard library defines `foldMap` with the following type:

```
foldMap :: (Monoid m, Foldable t) => (a -> m) -> t a -> m
```

For each of the following `foldMap` calls, select all options that are true:

(a) `foldMap (:[]) [1..10]`

- (i) The expression will fail to typecheck.
- (ii) The monoid in this call is `Int`.
- (iii) The monoid in this call is `[Int]`.
- (iv) The monoid in this call is `String`.
- (v) The expression is equivalent to the identity function.
- (vi) The foldable in this call is [] - the instance for lists.

(b) `foldMap show "123456"`

- (i) The expression will fail to typecheck.
- (ii) The monoid in this call is `Int`.
- (iii) The monoid in this call is `[Int]`.
- (iv) The monoid in this call is `String`.
- (v) The expression is equivalent to the identity function.
- (vi) The foldable in this call is [] - the instance for lists.

Question 2 (20 points)

For each of the Haskell expressions below, write their (most general) Haskell type or "ill-typed" if it contains a type error. The type signatures of all functions below are provided in the appendix at the end.

(a) `\x -> x`
Example answer:
`a -> a`

(b) `\x y -> (x,y)`
a → b → (a,b)

(c) `\x y -> if x == y then show x else show (x,y)`
Show a ⇒ a → a → String

(d) `\x l -> x : l ++ l ++ [x]`
a → [a] → [a]

(e) `getLine >>= putStrLn`
String → IO String → IO ()

(f) `putStrLn 42 >>= putStrLn 43`
IO ()

(g) `(,) "42"`
a → (a, String)

(h) `reverse . foldMap return`
Monad m ⇒ [a] → m a

(i) `\l -> [(x,y) | x <- l, y <- l, x /= y]`
Ord a ⇒ a → [(a,a)]

(j) `let f x = x in (f 'a', f True)`
(Char, Bool)

(k) `filterM (const [True, False])`
Monad m ⇒ [a] → m [a]

Question 3 (20 points)

For each of the types below, write a Haskell expression that has that type. Don't write trivial expressions (such as `[]`, `Nothing`, or `undefined`) unless there is no other option. You can use any function from the appendix, do syntax, list comprehensions, or any valid Haskell.

(a) `Int -> Int`

Example answers:

```
\x -> x + 1
(+1)
```

(b) `Bool -> [Bool]`

```
\x -> replicate 5 x
```

(c) `a -> Maybe b`

```
Just
```

(d) `(Int -> Char -> Bool) -> [Int] -> [Char] -> [Bool]`

```
\x y -> x > 0 && y == 'a'
```

(e) `(a -> b -> c) -> IO a -> IO b -> IO c`

```
liftA2
```

(f) `(a -> b) -> (b -> Bool) -> [a] -> [b]`

```
\f g l -> foldr (g . f) [] l
```

(g) `Maybe a -> (a -> Gen b) -> Gen (a,b)`

```
\x f -> do
  y <- x
  z <- f y
  return (y, z)
```

(h) `Eq a => a -> [a] -> [a]`

```
\x l -> case l of
  []    -> []
  (h:r) -> if x==h then r else [x]
```

(i) `Show a => [a] -> IO String`

```
\l -> case l of
  []    -> do getLine
  (h:t) -> do putStrLn h
              getLine
```

(j) `(a,b) -> (a -> b -> c) -> c`

```
\(x,y) f -> f x y
```

Question 4 (20 points + 10pt bonus!)

For each of the following functions, write down a short description of what `foo` does, and some output examples.

(a)
```
foo :: [Int] -> [Int]
foo l = [ x * x | x <- l, x > 0 ]
```

Example answer:
Calculates the squares of all positive numbers in a list.
`foo [] = []`
`foo [1,0,2,-1] = [1, 4]`

(b)
```
foo :: [Int] -> [Int]
foo l = [ (x,y) | x <- l, y <- l, x /= y]
```

Answer: Constructs a list of all pairs of non-equal ints in a list.
Foo [1,2] = [(1,2), (2,1)]

(c)
```
foo :: a -> [a] -> [a]
foo x l = reverse (x : reverse l)
```

Answer: Adds an element to the end of a list

Foo 3 [1, 2] = [1,2,3]
Foo 'c' "ab" = "abc"

(d)
```
bar          :: (a -> Maybe b) -> [a] -> [b]
bar _ []     = []
bar f (x:xs) =
  let rs = bar f xs in
  case f x of
    Nothing -> rs
    Just r  -> r:rs

foo :: [Maybe a] -> [a]
foo = bar id
```

Answer: Removes the maybe monad from a list.
Foo [Nothing] = []
Foo [Maybe 2, Nothing, Maybe 4] = [2,4]
Foo [] = []

(e)
```
foo :: [Int] -> Int -> (Int, [Int])
foo []  m = (m, [])
foo [x] m = (x, [m])
foo (x : xs) m = (max m' x, m : xs')
  where (m', xs') = foo xs m
```

Answer: On non-empty list: replace all elements of the list with m and return (largest element in list, list of ms)
On empty list: return (m, [])

foo [] 2 = (2, [])
foo [2,4,3] 5 = (4, [5,5,5])

(f) *Bonus!*

```
dropWhileM :: (Monad m) => (a -> m Bool) -> [a] -> m [a]
dropWhileM _ []     = return []
dropWhileM p (x:xs) = do
    q <- p x
    if q then dropWhileM p xs else return (x:xs)

foo :: ??
foo = dropWhileM (const [True, False])
```

Answer: Drops elements from ~~the~~ ~~start~~ of ~~the~~ ~~list~~, each with a 50% chance, and stops when an element is not dropped.

Example:
Foo [1,2,3] could be const [1,2,3]
or const [3]
but not const [2]

Question 5 (20 points + 10pt bonus!)

Implement the following Haskell functions:

(a) Implement a function `weave` that given two lists with elements of the same type, returns a list with elements alternating between the two lists. For example:

```
weave [1,2,3] [4,5,6] = [1,4,2,5,3,6]
```

You can assume that the lists have the same length.

```
weave [] [] = []
weave (x:xs) (y:ys) = x : y : (weave xs ys)
weave _ _ = error "lists not same length"
```

(b) Implement a function `toMax`, that given a non-empty list of integers, returns a list of the same length, where each element has been replaced by the maximum element of the list. For example:

```
toMax [1,4,2,5,3] = [5,5,5,5,5]
```

You can use the `foo` function of problem (4e) if it helps.

BONUS: Implement `toMax` so that it only traverses a list once!

```
toMax xs = replicate (length xs) (maximum xs)
```

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