## Contents

1	Ranking Algorithm, v1			
	1.1	Description of the problem	1	
	1.2	Rankings	2	
	1.3	Groups	2	

# 1 Ranking Algorithm, v1

## 1.1 Description of the problem

The ranking algorithm in myocardio operates on "exercises". In nonformal language an exercise has

- 1. a time when it was were last executed, which might be "never"
- 2. a list of associated muscles involved (with every muscle involved to the same degree)

To model this mathematically, assume we have a (finite) set  $\mathbf{Muscle}$  of muscles. For example:

$$\mathbf{Muscle} = \{ \mathbf{biceps}, \mathbf{triceps} \} \tag{1}$$

We'd like to model a point in time as a value from  $\mathbb{N}$ , the natural numbers. But we have to deal with the special value "never". So, we define  $T = \mathbb{N} \cup \{\Omega\}$ , where  $\Omega$  stands for this special value. This makes T a set that is not a ring anymore, it's not even ordered.

Modeling all possible exercises as simply

$$E = \mathcal{P}(\mathbf{Muscle}) \tag{2}$$

where  $\mathcal{P}$  is the power set operator — doesn't work, though, because you might have two exercises which have the same muscle groups but aren't the same.

So we assume another (finite) set **Exercise** of exercise *names*. We then assign two functions

 $m: \mathbf{Exercise} \to \mathcal{P}(\mathbf{Muscle})$ 

descibing the muscles of an exercise and

 $l: \mathbf{Exercise} \to T$ 

describing the latest execution time point.

The **input** of the algorithm is the three-tuple (**Exercise**, m, l). Its **output** should be a **reordering of the exercises**, which we can model with a function  $o : \mathbb{N} \to \mathbf{Exercise}$ .

### 1.2 Rankings

We define two rankings for an exercise. One ranks by time  $\rho_t$  and one by complexity  $\rho_c$  (i.e. the number of muscles involved).

Ranking by complexity is easy:  $\rho_c(e) = |m(e)|$ , it's just the number of muscles involved. More muscles equals a better ranking.

Ranking by time is a bit more complicated. We want to interpolate all exercises' times by the latest/oldest one. However, we cannot interpolate across T because we have no ordering (because of the special element  $\Omega$ ).

To fix this, we model  $\rho_t$  as follows:

- 1.  $\rho_t(e) = 0$  for all  $e \in \mathbf{Exercise}$  if  $\Omega \in l(\mathbf{Exercise})$ . Meaning the ranking is most if one of the exercises has never been performed.
- 2. Otherwise determine the minimum and maximum time stamps:  $l_{\min}, l_{\max}$  (which is now well-defined). Linearly interpolate between the two and rescale to [0,100].

This gives exercises that were just executed a low ranking (i.e. close to 0) and exercises that weren't performed recently higher ones (more towards 100).

The total ranking for an exercise is simply  $\rho(e) = \rho_t(e) + \rho_c(e)$ 

### 1.3 Groups

We could now just rank all our exercises by  $\rho$ . However, two exercises that feature the same or similar muscle groups could be included back-to-back in this plan, and that's a non-goal.

In order to rank the exercises, we employ a greedy algorithm in order to construct an order  $o_i$  for exercises (where  $i \in \mathbb{N}$ ). We assume  $|\mathbf{Exercise}| \geq 1$ .

- 1. Let i = 0. Take the exercise  $e_i = \operatorname{argmax}_{e \in \mathbf{Exercise}} \{ \rho(e) \}$  with the highest ranking. Define  $o_i = e_i$  Define the rest  $R_i = \mathbf{Exercise} \setminus \{o_i\}$
- 2. If  $|R_i| = \{e_{i+1}\}$ , choose  $o_{i+1} = e_{i+1}$  and terminate.
- 3. Define  $d_i: R_i \to \mathbb{N}$  as  $d_i(e) = |m(e) \cap m(o_i)|$ . This is a ranking of how many muscle groups are the same as the first exercise (d for "Durchschnitt", meaning intersection in German).

4. Define  $D_i: \mathbb{N} \to \mathcal{P}(R_i)$  as

$$D_i(n) = \{ e \in R_i | d_i(e) = n \}$$
 (3)

This is a ranking of how many muscle groups are the same as the first exercise.

- 5. Define  $N_i = \operatorname{argmin}_{n \in \mathbb{N}} \{D_i(n) | D_i(n) \neq \emptyset\}$ . Thus,  $D_i(N_i)$  will be the group of exercises with the least number of muscles in common with the chosen one,  $o_i$ . This exists, because we assumed to have at least one exercise left in step 2, and even if all exercises have all muscles in common, we will have a group for them.
- 6. From  $D_i(N_i)$ , choose the exercise with the highest rank  $\rho$  as the next exercise  $o_{i+1}$ . Define  $R_{i+1} = R_i \setminus \{o_{i+1}\}$ . Go to step 2 (reindexing  $i \to i+1$ ).

This algorithm will terminate after at most  $|\mathbf{Exercise}|$  steps, since  $|R_i|$  is strictly monotonically decreasing as i increases.