Last Name _		
First Name		
Student No.	 <u></u>	

Instructions:

- Answer the questions in the spaces provided on the question sheets. Use the backs of sheets for rough work.
- No aids (notes, textbooks, electronic devices) are allowed.
- If you use results discussed in lecture, tutorial, or assignments in your solutions to the questions, cite what you are using precisely.
- You have 50 hittps://ppweGoder.come starts.
- Good luck on the test!

Total Marks: 3 ddstweeth 3t marks 4 credit

- 1. (15 points) Determine whether the statements below are true or false. If true, provide a proof. If false, explain why the statement is false. Recall that a language L is non-trivial if $L \neq \emptyset$ and $L \neq \Sigma^*$.
 - (a) (5 points) For any non-trivial semi-decidable language A, there is a computable mapping reduction $A \leq_m \overline{A}$ where \overline{A} is the complement.

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(b) (5 points) For any non-trivial decidable language B, there is a computable mapping reduction $B \leq_m \overline{B}$. Add Wechat powcoder

(c) (5 points) If A is an infinite non-trivial decidable language, there is a subset $B \subseteq A$ that is not decidable

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2. (10 points) Consider the language

$$SEP = \{ \langle M_1, M_2 \rangle : L(M_1) = \overline{L(M_2)} \}$$

consisting pairs of Turing machines $\langle M_1, M_2 \rangle$ where for every string $x \in \Sigma^*$, exactly one of M_1 or M_2 accepts x. Is SEP semi-decidable? Prove your answer.

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3. (5 points) Recall the definition of the Kolmogorov complexity K(x) of a string and recall that the set of Kolmogorov-incompressible strings is defined as

$$I = \{x \in \{0, 1\}^* : K(x) \ge |x|\}.$$

(a) (5 points) Show that I is co-semidecidable.

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(b) (3 points) EXTRA CREDIT (so only if you have finished all other problems!): Let A be a decidable language where $C_n = A$ (c. $C_n = A$) (c. $C_n = A$) (c. $C_n = A$) (b. $C_n = A$) (b. $C_n = A$). Show that A can have only finitely many incompressible strings (i.e. $|A \cap I| < \infty$).

This page may be used to continue solutions from previous pages in case there is no space. If you are finished writing all your solutions, you may use this space to draw a meme or otherwise write about your feelings about CSC 463.

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