# PyBaMM-Python Battery Mathematical Modelling

# User Workshop 1st April 2020

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## How to install

Instructions on the GitHub repo: <a href="https://github.com/pybamm-team/PyBaMM">https://github.com/pybamm-team/PyBaMM</a>

#### How can I obtain & install PyBaMM?

#### Linux

For instructions on installing PyBaMM on Debian-based distributions, please see here

#### Mac OS

For instructions on installing PyBaMM on Mac OS distributions, please see here

#### Windows

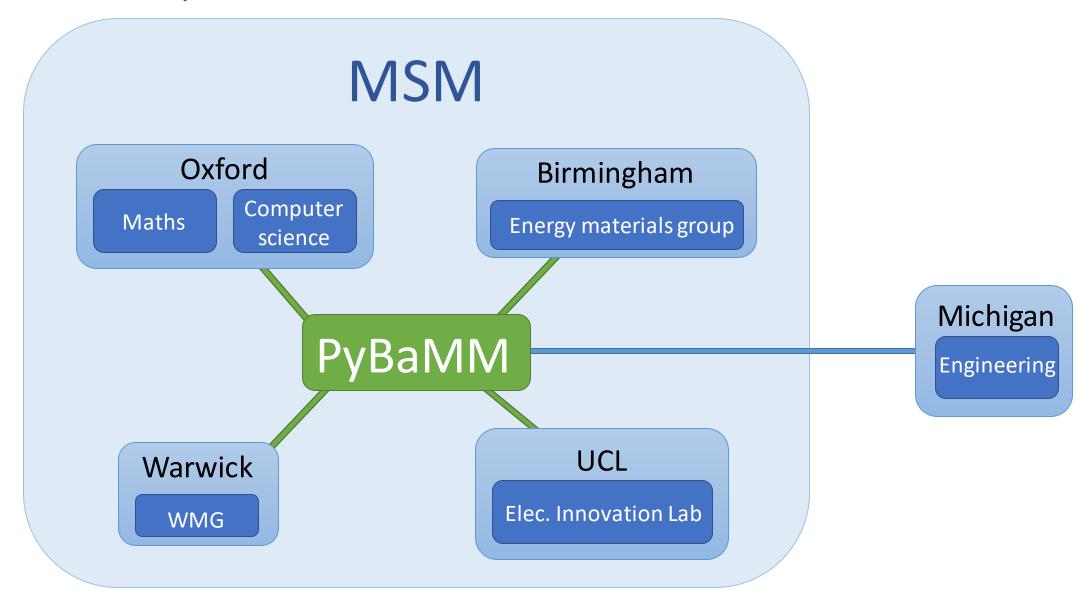
We recommend using Windows Subsystem for Linux to install PyBaMM on a Windows OS, for instructions please see here

We recommend that you install into a virtual environment. On Linux and Mac:

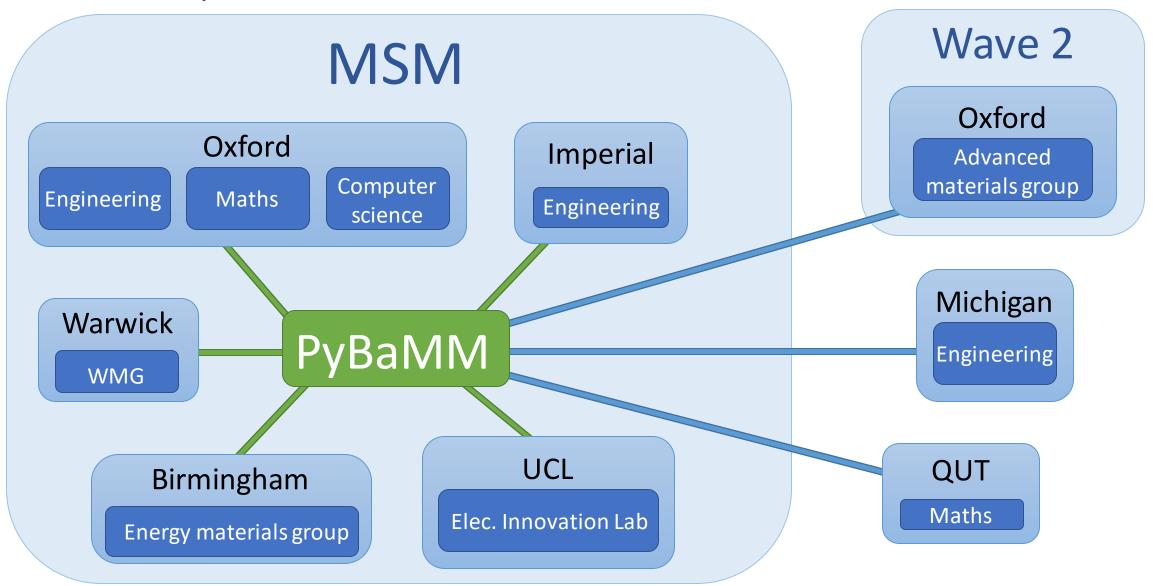
- 1. python3 -m venv env
- 2. source env/bin/activate
- 3. pip install pybamm

For Windows we recommend the use of Windows Subsystem for Linux (instructions online)

# Who is PyBaMM? Current collaborators



# Who is PyBaMM? Future collaborators



# What is PyBaMM?

PyBaMM is a framework for building and solving battery models

**FAST** 

**FLEXIBLE** 

**MODULAR** 

Many standard models already implemented and easy to reuse

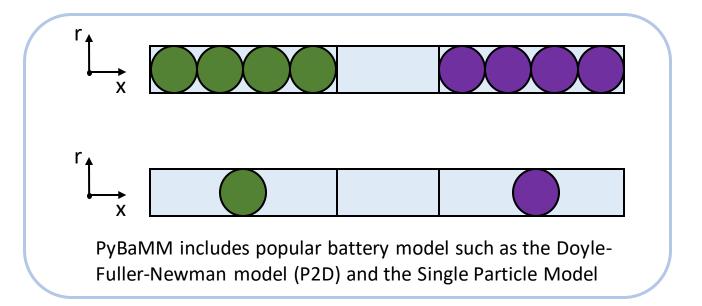
- Cell geometries: 1D, 2+1D single layer pouch cells
- Standard lithium-ion models: ODE, SPM, SPMe, DFN plus lead-acid models
- Chemistries: LCO, NCA, Graphite, LiPF6
- Fully coupled thermal models
- Experimental suite
  - Any voltage, current or power control (e.g. GITT, PITT, CCCV, drive cycle, etc.)
  - Easy interface to define new protocols
- Nonlinear parameters provided as functional form or as data
- Structured electrodes
- Interface with external software

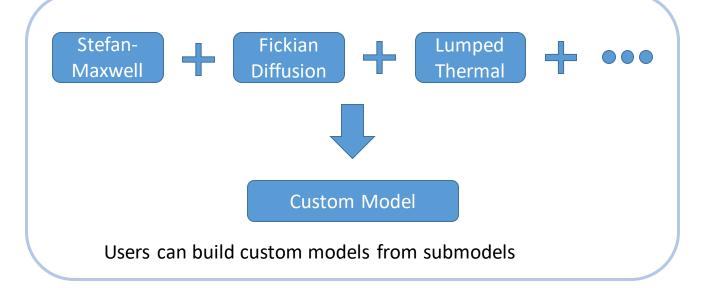
## Model structure

 Battery models are constructed from submodels

Use or adapt pre-built models

Create custom models



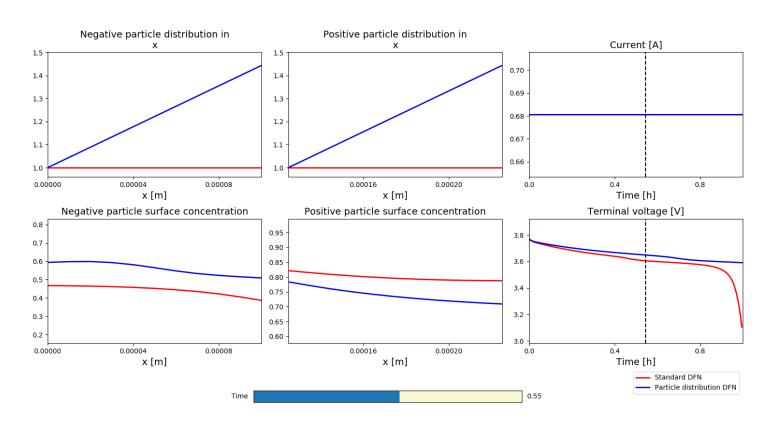


#### Model structure

 Structure allows for "plug and play" physics

 New physics can be quickly implemented in an independent fashion

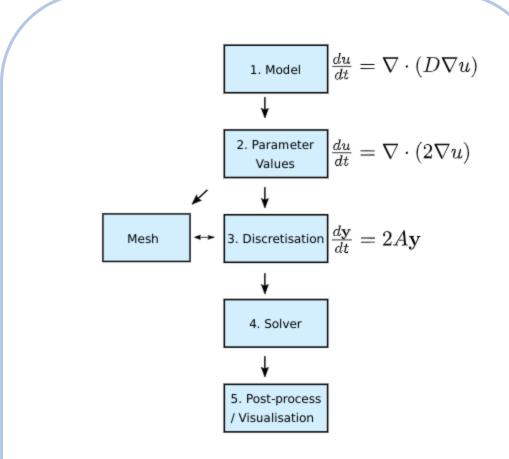
 Different physical mechanisms are readily included in both full and reduced-order models



Using PyBaMM it is easy to compare how different physics affects the model solution. Here we investigate the influence of graded electrodes (particle distribution in the through-cell direction x).

## Numerical methods

- Choice of spatial discretisation
  - Finite Volume Method (macroscopic and particles)
  - Finite Element Method in 2D direction (current collectors in pouch cell models)
- Calculation of the analytic Jacobian from expression tree via automatic differentiation (using CasAdi)
- Ability to set up, solve and perform forward and adjoint sensitivity analysis
- Multiple ODE and DAE solvers (e.g. scipy, sundials CVODE and IDA)

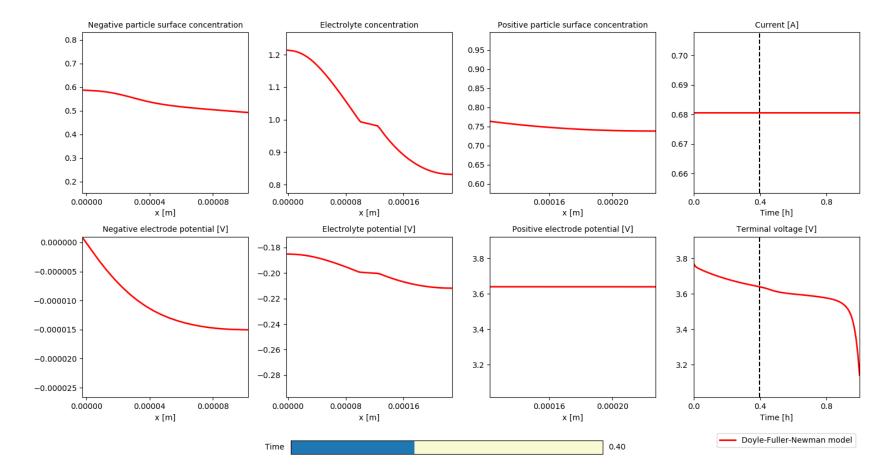


By employing a pipeline process, PyBaMM separates the statement of model equations, from the inputted parameters, choice of spatial discretization, and choice of time solver.

# Simple interface: CC discharge

```
import pybamm
model = pybamm.lithium_ion.DFN()
sim = pybamm.Simulation(model)
sim.solve()
sim.plot()
```

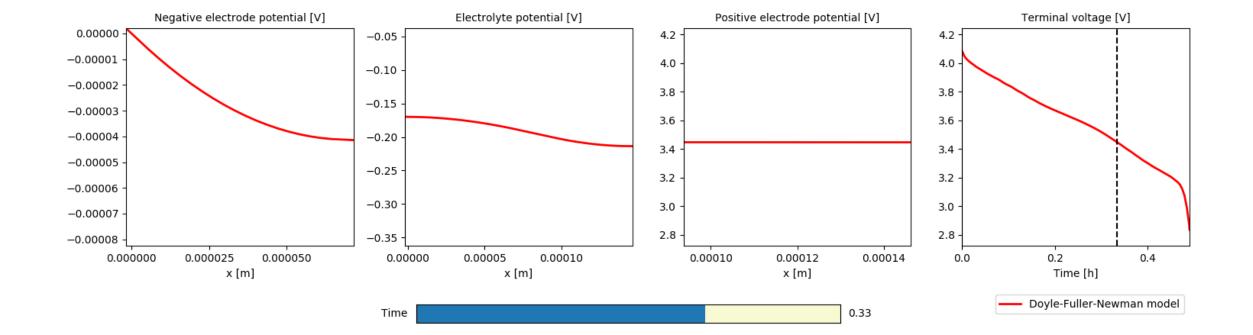
- Easy interface for running simulations
- Model, simulation and plots can be customised



# Simple interface: Change parameters

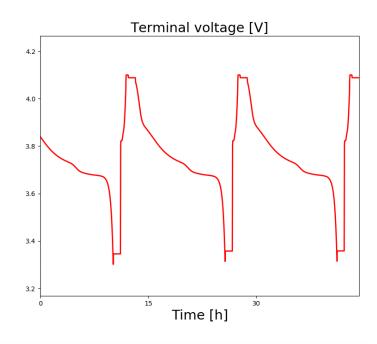
```
import pybamm
model = pybamm.lithium_ion.DFN()
chemistry = pybamm.parameter_sets.NCA_Kim2011
parameter_values = pybamm.ParameterValues(chemistry=chemistry)
sim = pybamm.Simulation(model, parameter_values=parameter_values, C_rate=2)
sim.solve()
sim.plot()
```

Easy to change parameters and model options



# Simple interface: Simulation of experimental protocols

PyBaMM allows users to specify experimental protocols using keyword strings



- Can easily define custom protocols
- Specify current, power or voltage
- Standard protocols developed by Emma Kendrick's group are also implemented but not public yet

## Solution times

## Doyle-Fuller-Newman Model – 1C CC Discharge

Grid points per domain	States	CasAdi ("fast" mode)	CasADi ("safe" mode)	IDA KLU	Scikits DAE
10	281	0.155s	0.793s	4.860s	2.102s
20	961	0.226s	1.571s	4.776s	10.120s
40	3521	0.566s	5.101s	6.992s	1m 47s
80	13441	1.977s	18.951 s	11.642s	-
160	52481	8.865s	1m 41s	34.289s	-

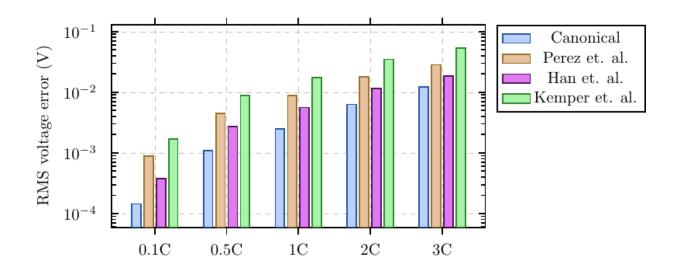
All simulation performed on a laptop computer (i5, 2.1 GHz, 16 Gb of RAM) using both absolute and relative tolerances of  $10^{-6}$ . The parameters were taken from the papers:

- 1) M. Ecker, T.K.D. Tran, P. Dechent, S. Kabitz, A. Warnecke, and D.U. Sauer. *Parameterization of a physico-chemical model of a lithium-ion battery. I. Determination of parameters.* Journal of The Electrochemical Society, 162 (2015), pp. A1836-A1848.
- 2) M. Ecker, S. Kabitz, I. Laresgoiti, and D.U. Sauer. *Parameterization of a physico-chemical model of a lithium-ion battery. II. Model validation.* Journal of The Electrochemical Society, 162 (2015), pp. A1849-A1857.

# Case study: Single Particle model with electrolyte (SPMe)

Marquis, Timms (Oxford, Maths); Sulzer (Michigan)

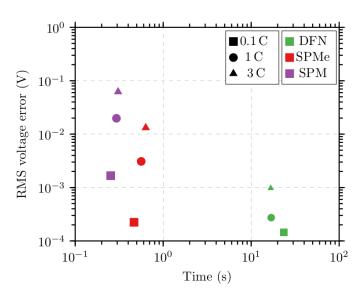
- Systematic derivation of SPMe using asymptotic methods
   Electrolyte diffusion time << discharge time</li>
   Large electrode and electrolyte conductivity
- Outperforms other (ad hoc) models in literature of similar complexity
- Achieves order of magnitude reduction in computation cost at small loss of accuracy
- Extends the validity of SPM to higher C-rates.



```
models = [
    pybamm.lithium_ion.SPM(),
    pybamm.lithium_ion.SPMe(),
    pybamm.lithium_ion.DFN(),
]
solutions = [None] * 3

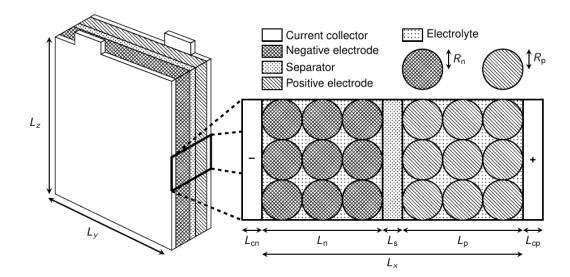
for i, model in enumerate(models):
    sim = pybamm.Simulation(model)
    sim.solve()
    solutions[i] = sim.solution

plot = pybamm.QuickPlot(solutions)
plot.dynamic_plot()
```



# Case study: 2+1D Pouch Cell Model

- Larger batteries exhibit non-uniform behaviour which may adversely affect battery performance and lifetime
- Exploit the geometry to systematically derive 2+1D model
- Combine with other limits to derive a hierarchy of reducedorder models
- Influence of cell geometry can be investigated efficiently



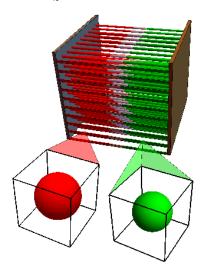
Timms, Marquis (Oxford, Maths); Sulzer (Michigan)

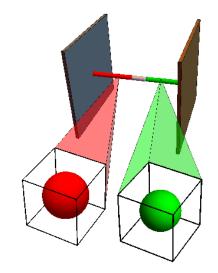
High conductivity

$$rac{\sigma L_x}{\sigma_c L_c} \sim rac{L_x^2}{L_z^2} \quad \Rightarrow \quad ext{2+1D model} \qquad rac{\sigma L_x}{\sigma_c L_c} \sim rac{L_x^3}{L_z^3}$$

Very high conductivity

$$rac{\sigma L_x}{\sigma_c L_c} \sim rac{L_x^3}{L_z^3} \quad \Rightarrow \quad 2 + ar{1} {\sf D} \,\, {\sf model}$$

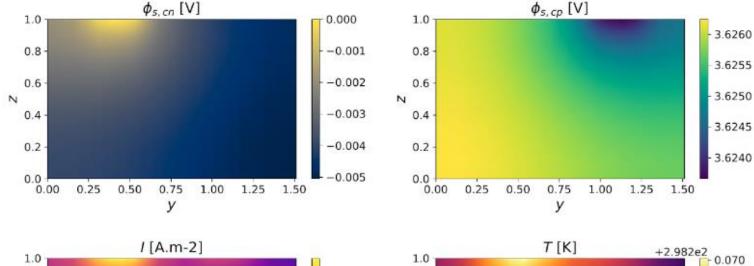




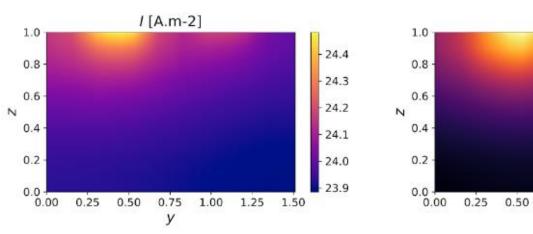
The full 3D model is reduced to a collection of 1D models, coupled via 2D current collectors

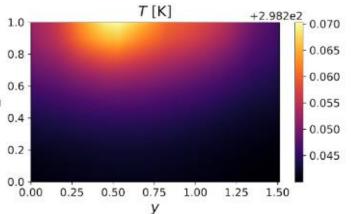
# Case study: 2+1D Pouch Cell Model

Timms, Marquis (Oxford, Maths); Sulzer (Michigan)



Example result: 100 local Single Particle Models with temperature, solution time approx. 22s for 1C discharge





```
options = {
    "current collector": "potential pair",
    "dimensionality": 2,
}
model = pybamm.lithium_ion.SPMe(options)

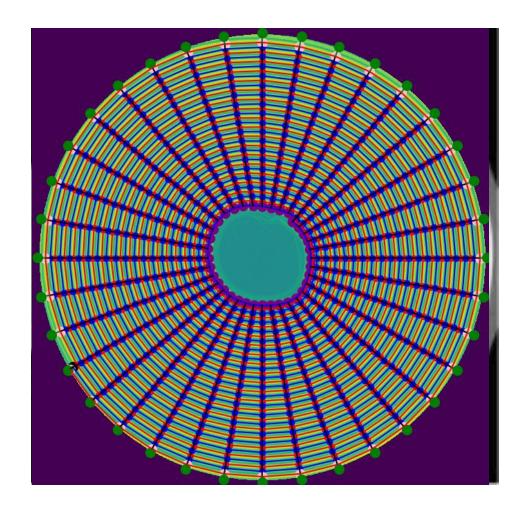
sim = pybamm.Simulation(model)
sim.solve()
```

# Case study:

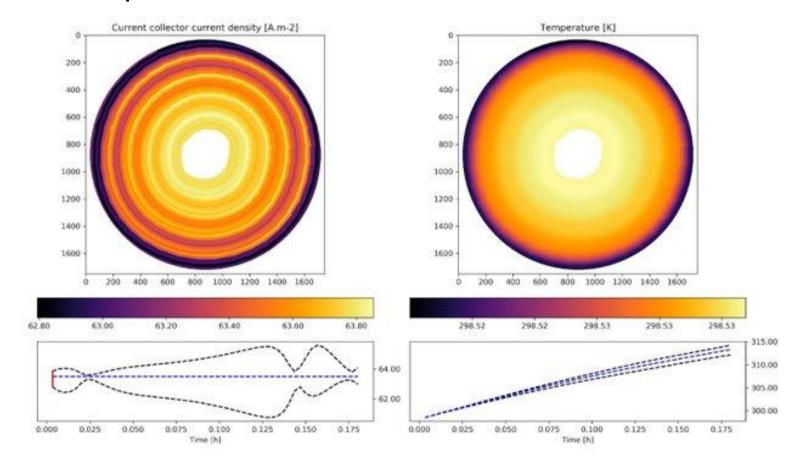
Tranter (UCL); Timms (Oxford, Maths)

# A coupled multiscale model of electrochemistry and thermal transport for Li-ion cells

- Internal temperature differences lead to non-uniformities in current flow, state of charge, particle stress and levels of degradation
- Li-ion battery heat generation and transport problem coupling:
  - particle scale electrochemical modelling (PyBaMM)
  - cell level electrical and thermal modelling (*OpenPNM*)
- Example: a 2D heat-transfer problem for spirally rolled cylindrical batteries using tomography data

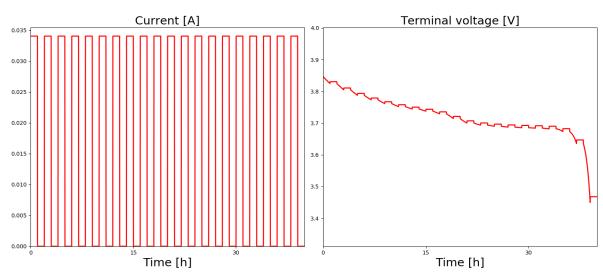


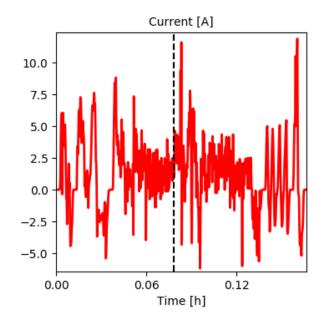
A coupled multiscale model of electrochemistry and thermal transport for Li-ion cells

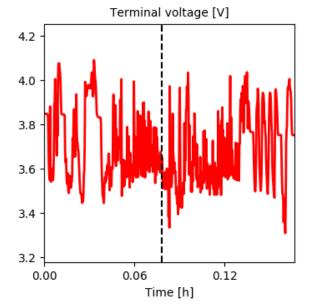


HTC = 5 [W.m-2],  $\sigma$  = 3e7 [S.m-1], #tabs = 5, Current = 5 [A]

# Case study: Simulation of experimental protocols



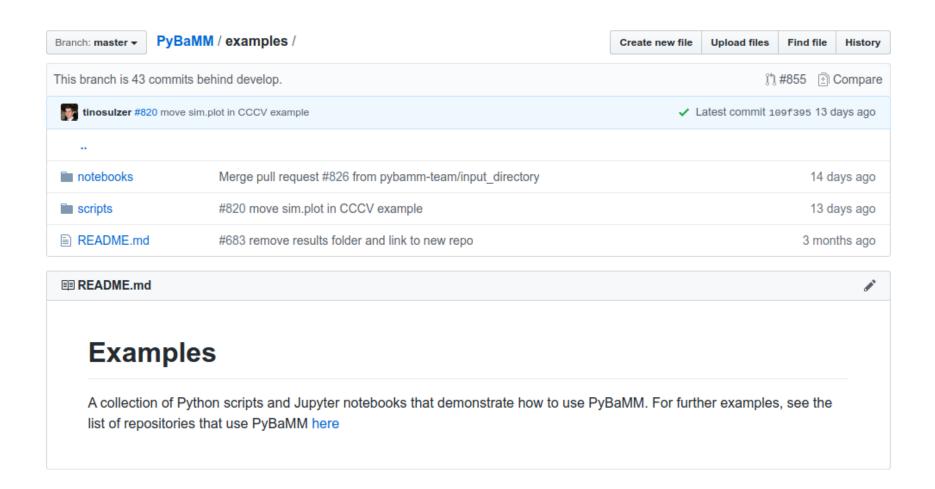




```
model = pybamm.lithium_ion.DFN()
param = model.default_parameter_values
param["Current function [A]"] = "[current data]US06"
sim = pybamm.Simulation(model, parameter_values=param)
sim.solve()
sim.plot()
```

# More examples online

https://github.com/pybamm-team/PyBaMM/tree/master/examples



## And documentation

https://pybamm.readthedocs.io/en/latest/

#### API docs:

## Welcome to PyBaMM's documentation!

Python Battery Mathematical Modelling (**PyBAMM**) solves continuum models for batteries, using both numerical methods and asymptotic analysis.

PyBaMM is hosted on GitHub. This page provides the API, or developer documentation for pybamm.

- Index
- Module Index
- Search Page

#### **Tutorials:**

#### Contributing

There are many ways to contribute to PyBaMM:

- Adding Parameter Values
- Adding a Model
- Adding a Spatial Method
- Adding a Solver

Before contributing, please read the Contribution Guidelines.