This session is devoted to two ways of reusing the implementation, one of the greatest advantages provided by object-oriented programming: composition and inheritance. Composition regards the creation of objects of an existing class inside a new class, delegating to those objects the implementation of some methods, or part of it. For example, we see a class Car which has an object of type Engine, to which it delegates the implementation of the method start: with composition, you reuse the functionality of the code. On the other hand, with inheritance you create classes which extend existing classes, adding some fields or methods or, maybe even more importantly, changing the implementation of existing methods: this last feature is known as method overriding.

It's not always easy to recognise if you need inheritance or composition for the solution of a specific problem. We can say that inheritance involves a relation of type *is-a* (for example, a Circle is a Shape, and then the class Circle inherits from the class Shape) whereas composition involves a *has-a* relation (a Car has an Engine).

However, the borders are not always that clear. Generally speaking, composition may be preferred over inheritance because it is often simpler and more flexible: for example, the member objects of your new class are typically private, making them inaccessible to the client programmers who are using the class. Just to give a first intuition about the differences between the two approaches and their functionalities, we will see some examples of problems where the use of inheritance is the best solution and some others where composition comes into play.

One of the most striking features of inheritance is *polymorphism*: suppose you have three derived classes which extend (= inherit from) a base class, and suppose they all override a method of the base class, implementing it in different ways (one different way for derived class). So you want that objects of the derived class execute the method in a different way depending on their type. However, say you write a method somewhere that involves objects of the base class, making them call the overridden method. You don't want to change this last code depending on the derived type of objects, i.e., here you want to treat an object not as the specific type that it is, but instead as its base type. On the other hand, you want to treat it as its specific type when it calls the overridden method. This problem can be solved by treating an object as its base type at compilation time, and as its specific type at run type. This behaviour is known as *late binding* and allows for *polymorphism*: a method involving another, overridden method in its implementation can be written exactly in the same way for all the derived types, returning however different outputs depending on the specific type. We will see some examples of this use.

Inheritance introduces a further access modifier, i.e., protected: as we see in some examples, protected gives the second less restrictive access to methods and fields: protected methods and fields have package access, and can moreover been accessed and called in methods of classes which extend the class where they are defined.

In order for you to be able to have a look at the code also after the class, this is a list of the classes we see, in the order we look at them and with reference to the topic they are supposed to cover.

- com.andreamazzon.session4.usefulmatrices.UsefulMethodsMatricesVectors: this class is not about reusing of implementation, but it contains useful methods that deal with arrays and matrices (arrays of arrays). It will be used in com.andreamazzon.session4.composition.binomialmodel.
- Code in com.andreamazzon.session4.inheritanceandconstructors.basicexample: the code in this package gives a very simple example of the syntax of inheritance and of the way the default constructors of the derived and of the base class are called. In particular, you can note that the default constructor of the base class is implicitly called when an object of the derived class is created.
- Code in com.andreamazzon.session4.inheritanceandconstructors.sportsmans: here we see how things work when the base class have only constructors with arguments. We have seen that in this case the default constructor cannot be called. For this reason, inside the constructor of the derived class we have to call the constructor of the base class. This is done with the keyword super.

- Code in com.andreamazzon.session4.testingprotection: in this package we illustrate how the protected access modifier works: the methods of the class DerivedClass have access to the protected methods and fields of the parent class ProtectedOtherPackage in com.andreamazzon.session4.protectedotherpackage even if they are not in the same package. On the other hand, in the main method of TestClass we can access protected fields and method of the class ProtectedSamePackage, because protected also gives package access.
- Code in com.andreamazzon.session4, goalkeepers: the code here gives a simple example of how an object of a derived class is able to call methods and to access fields of the base class, plus possibly some more methods which are defined in the derived class.
- Code in com.andreamazzon.session4.overridingandoverloading.videogame: the classes here illustrate the difference between overriding (give another implementation of a method of the base class) and overloading (defining and implementing a method with same name of an existing one but with different argument lists). We see that the derived class can both override and overload a method of the base class. Note the note the @Override annotation above the overridden method. Here we also see what happens if we construct an object with the constructor of the derived class, but giving it a reference to the base class. That is, when we attach an object of the derived class to a reference of the base class.
- Code in com.andreamazzon.session4.polymorphism.amphibians: this is an example of polymorphism: you can see how the method behavior(Amphibian amphibian) of the class Amphibian accepts as an argument a reference of type Amphibian, making it call three methods which are overridden from the derived classes Frog and Toad. Running the example, you can see that you can also pass it objects of type Frog and Toad, which then execute the methods in their specific way. Here late binding comes into play: the point is that at compilation time Java looks at the reference of the objects (the first name of the class you write when you construct the object) and at running time it looks at the specific type of the object which is attached to that reference. At compilation time, when we call the method behavior(Amphibian amphibian) passing it an object of type we have constructed as Frog frog = new Frog(), it accepts it because:
 - Due to late binding, behavior(Amphibian amphibian) accepts any object which has a reference of type Amphibian;
 - Because of that, Java is able to recognize that it should *upcast* frog to Amphibian, i.e., give it an Amphibian reference: this is what it does. It's like we had written Amphibian frog = new Frog().

In this way, the objects are treated as their base type at compilation time, and as their derived type at running time.

- com.andreamazzon.session4.polymorphism.shapes; this is another example of polymorphism, and here you also have to work a little bit. We have a class Shape with a method computeArea(), that we are not able to implement in a good way for a general Shape object (we will see next time how such methods should be handled). We then have three classes extending Shape, i.e., Triangle, Circle and Square. Override computeArea() for the three classes, giving an implementation according to the type of the shape. You have to add specific sub-class fields (for example, height and base for the triangle), also implementing the constructors setting those fields. Note then how polymorphism appears in the main method of ShapeAreaTest: the method computeArea() can be called by any object of type Triangle, Circle and Square returned by the RandomShapeGenerator.
- com.andreamazzon.session4.composition.car: first example of composition. The class Car has an object of type Engine, to which it *delegates* the implementation of the method start.
- com.andreamazzon.session4.composition.binomialmodel and

com.andreamazzon.session4.inheritance.modifiedgenerator:

here we see two examples, both involving

in order to see the different uses of composition and inheritance. In the first example we use the code of LinearCongruentialGenerator in the class BinomialModelSimulator in order to simulate a binomial model: we delegate to the methods of the object of type LinearCongruentialGenerator the generation of random natural numbers on which we base to simulate our process. We can say that our simulator has a LinearCongruentialGenerator. The class BinomialModelSimulator is used itself in BinomialModelUser to simulate the process and return some paths or the average at a given time. This is another example of composition and delegation.

On the other hand, the second example is another linear congruential generator, in which we also want to get negative numbers. Here inheritance is maybe simpler, and we have more a kind of *is-a* relation: we then extend the class LinearCongruentialGenerator, just by overriding one method.