Backward Propagation

$\mathbf{R}^{(3)}$

$$r^{(3)} = \frac{\partial E(w)}{\partial a^{(3)}} = \frac{-t}{e^{ta^{(3)}} + 1}$$

$\mathbf{R}^{(2)}$

$$r_q^{(2)} = \frac{\partial E(w)}{\partial a_q^{(2)}} = \frac{\partial E(w)}{\partial a^{(3)}} \frac{\partial a^{(3)}}{\partial a_q^{(2)}}$$

L

$$r_L^{(2)} = r^{(3)} \frac{(w^{(3)})^T \cdot a_{LR}^{(2)} \cdot e^{a_R^{(2)} + a_L^{(2)}}}{(e^{a_R^{(2)}} + 1)(e^{a_L^{(2)}} + 1)^2}$$

R

$$r_R^{(2)} = r^{(3)} \frac{(w^{(3)})^T \cdot a_{LR}^{(2)} \cdot e^{a_R^{(2)} + a_L^{(2)}}}{(e^{a_L^{(2)}} + 1)(e^{a_R^{(2)}} + 1)^2}$$

LR

$$r_{LR}^{(2)} = r^{(3)} \frac{(w^{(3)})^T}{(e^{-a_L^{(2)}} + 1)(e^{-a_R^{(2)}} + 1)}$$

$\mathbf{R}^{(1)}$

$$r_q^{(1)} = \frac{\partial E(w)}{\partial a_q^{(1)}} = \sum_{p \in \{L,R,LR\}} \frac{\partial E(w)}{\partial a_p^{(2)}} \frac{\partial a_p^{(2)}}{\partial a_q^{(1)}}$$

L

$$r_L^{(1)} = \sum_{i=1}^{H2} r^{(2)}((w_L^{(2)})^T \cdot sech(a_{L,i}^{(1)}) + (w_{LR,i}^{(2)})^T \cdot sech(a_L^{(1)}))$$

R

$$r_R^{(1)} = \sum_{i=1}^{H2} r^{(2)}((w_R^{(2)})^T \cdot sech(a_{R,i}^{(1)}) + (w_{LR,i}^{(2)})^T \cdot sech(a_R^{(1)}))$$