case 1:
$$P_u \succeq P^* \succeq P_l$$
 case 2: $P_u = P^* \succeq P_l$... P_u case 3: $P_u \succeq P^* = P_l$ case 4: $P_u = P^* = P_l$... P_l