



Ultimatum Game in Complex Networks

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Network Science

Ultimatum Game

Proposer offers p

Responder accepts

Proposer receives $1-p$
Responder receives p



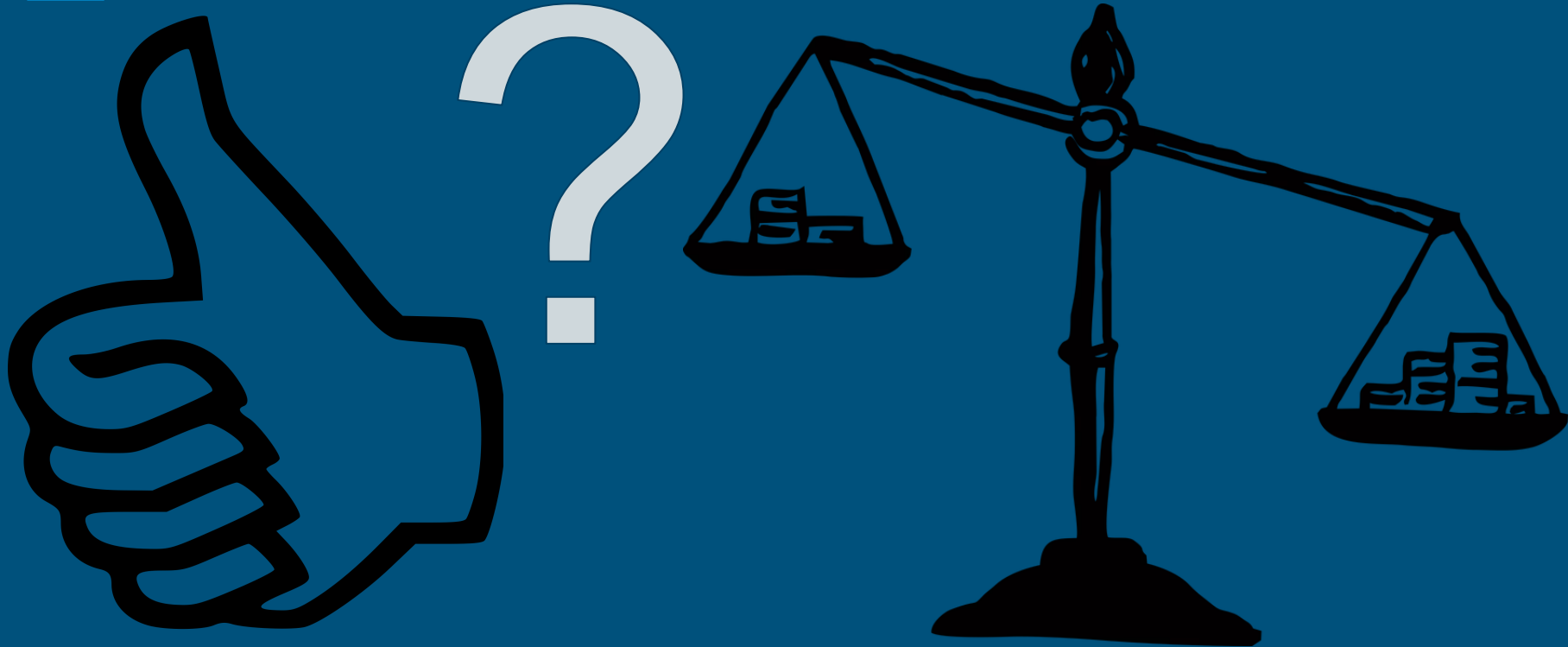
Responder rejects



Proposer receives 0
Responder receives 0



Ultimatum Game

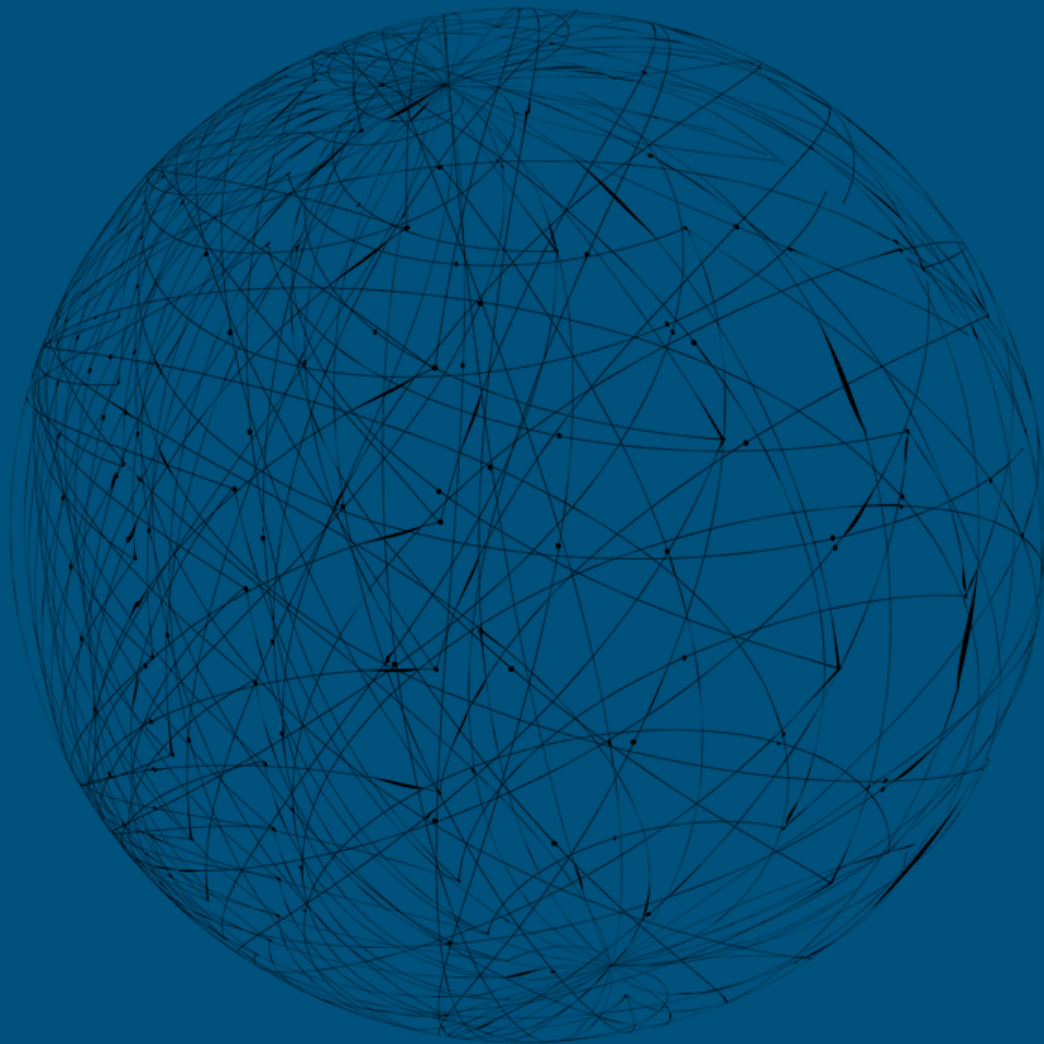


Method

- Erdős–Rényi graphs
- Scale-free networks
- 3 types of players
- 2 update Rules



NetworkX
Network Analysis in Python



Types of Players

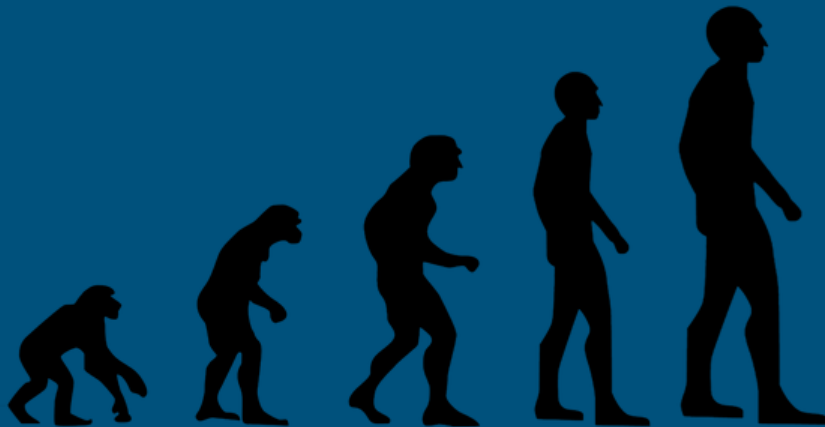
- Empathetic
- Pragmatic
- Independent



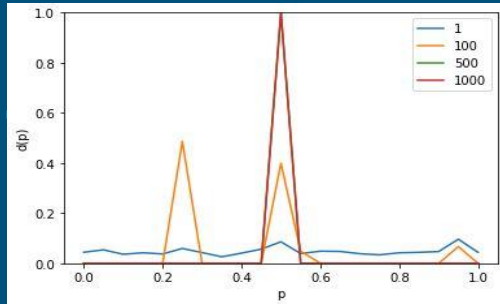
Update Rules

- Natural Selection
- Social Penalty

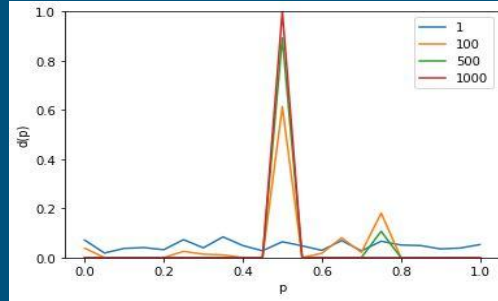
$$P_{ij} = \frac{\Pi_j - \Pi_i}{2 \max\{k_i, k_j\}}$$



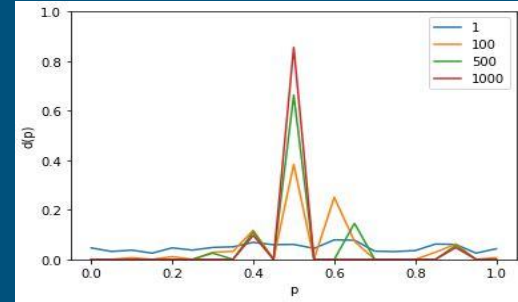
Natural Selection Scale Free



Empathetic

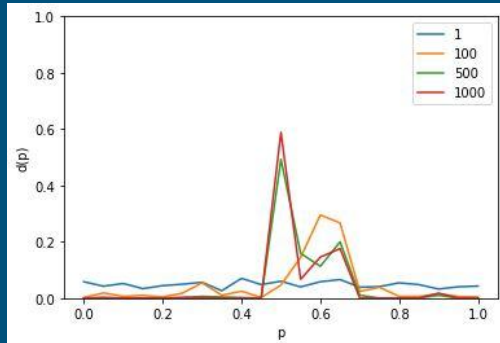


Pragmatic

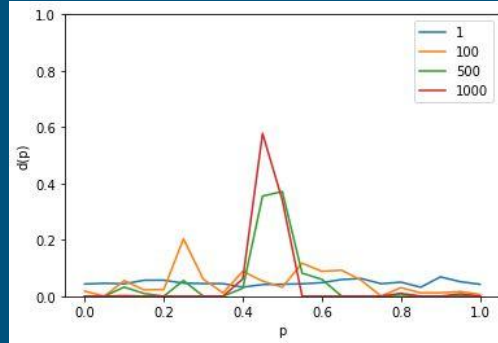


Independent

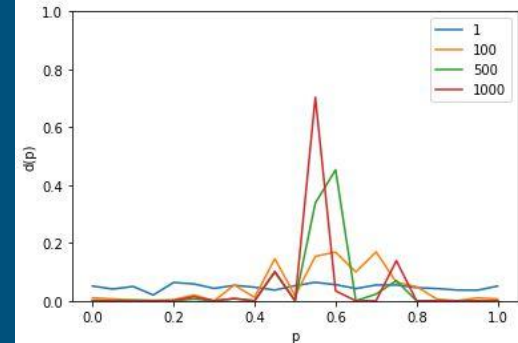
Erdős–Rényi



Empathetic

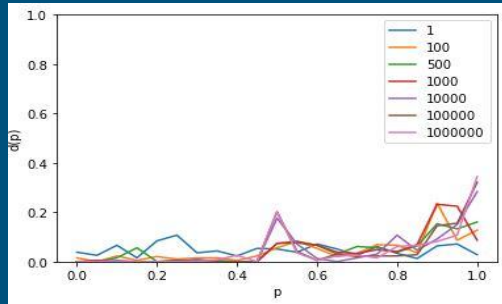


Pragmatic



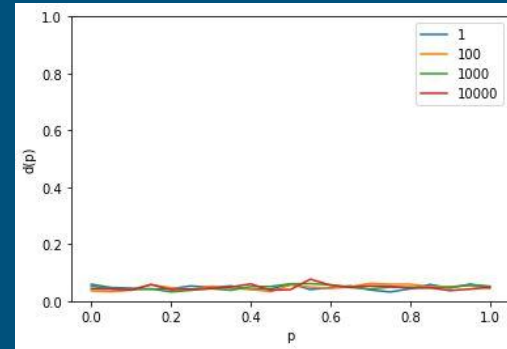
Independent

Social Penalty



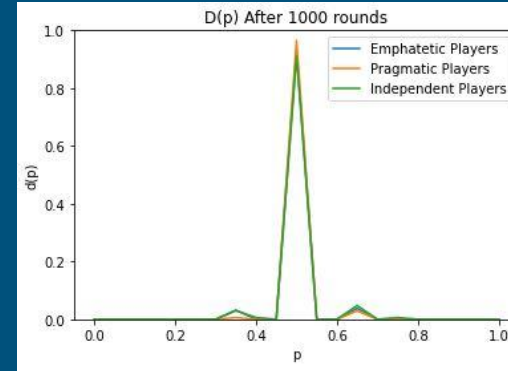
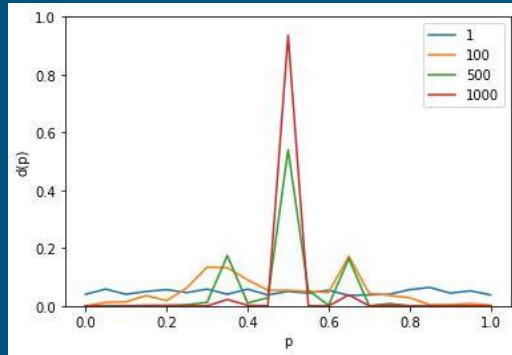
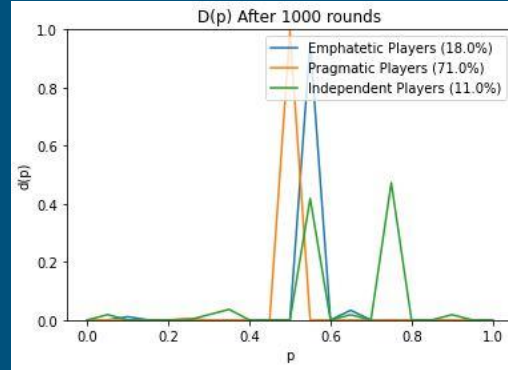
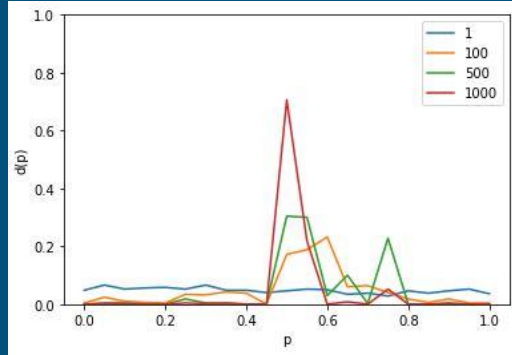
Scale Free Empathetic

Social Penalty & Natural Selection



Erdős-Rényi Empathetic

Social Penalty on Networks with multiple types of Players



Results and Conclusion

- Heterogeneity
- Convergence to 0.5
- Nash Equilibrium

Nash Equilibrium

		Player 2	
Player 1		(1,1)	(0,5)
		(5,0)	(3,3)

Pareto
Optimal



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Questions?