### ADAPTIVE REFINEMENT RESULTS

Everywhere, we have  $1 \underline{\delta}$  layer,  $\theta = 0.7$ , mean-zero residual estimation unless specified otherwise.

### SMOOTH SOLUTION

 $u(t,x,y) = (1+t^2)x(1-x)y(1-y)$ . We see nice rate 0.5 of the error, rate 1.0 of the L2-error at t=0

### TIME-SINGULAR SOLUTION

 $u(t,x,y)=(1+t^{0.1})x(1-x)y(1-y)$ . Quadrature order 5 in time. We see *very* strong refinement towards the origin (with wavelets around  $t=10^{-10}$ ). Suspect it is due to quadrature error.

## MILDLY SINGULAR SOLUTION

 $u_0(x,y) := x(1-x)y(1-y)$  with g=1 forcing data. Nice rate 0.5 with rate 1.0 for L2-error at t=0.

Date: January 17, 2020.

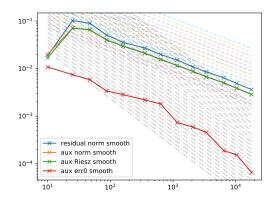
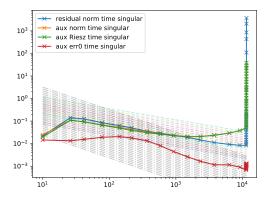


FIGURE 1. Smooth solution rate



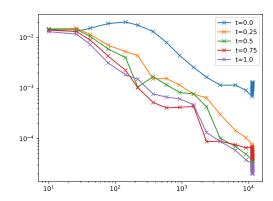


Figure 2. Time singular solution: left rate; right time-slice errors.

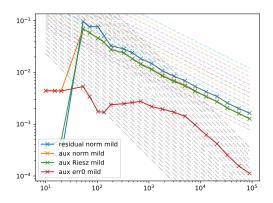


FIGURE 3. Mild singular solution rate.

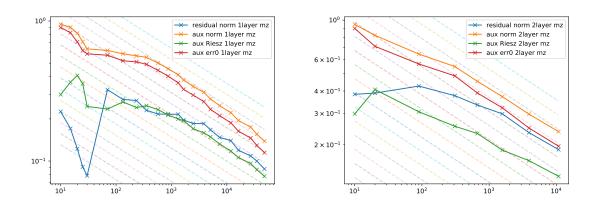


FIGURE 4. Strongly singular solution rates: left 1 layer, right 2 layers.

# STRONGLY SINGULAR SOLUTION

 $u_0(x,y) := 1$  with g = 0 forcing data. Clean rate 0.25 (where we had hoped 0.5).