Computing Fibonacci numbers on a Turing Machine

Alex Vinokur

Holon, Israel
alexvn@barak-online.net
alex.vinokur@gmail.com
Home Page: http://alexvn.freeservers.com/

 ${\bf Abstract.}\,$ A Turing machine that computes Fibonacci numbers is described.

1 Preface

The program computes a Fibonacci number.

A number n is represented by n 1-s. **Sample**:
5 is represented as 1 1 1 1 1
3 is represented as 1 1 1

Input: number nSample (n = 7):
1 1 1 1 1 1

Output: Fibonacci-nSample (Fibonacci-7):

2 Alphabets of States and Symbols

Here are alphabets of states and symbols.

```
\begin{array}{c} {\rm State\ alphabet} \\ {\rm Initial\ state:}\ q_0; \\ {\rm Halting\ state:}\ q_f; \\ {\rm Internal\ states:}\ q_{101},\ q_{102},\ q_{103},\ q_{104},\ q_{105},\ q_{106},\ q_{107},\ q_{108},\ q_{109},\ q_{201},\ q_{202}, \\ q_{203},\ q_{204},\ q_{301},\ q_{302},\ q_{303},\ q_{304},\ q_{305},\ q_{306},\ q_{307},\ q_{308},\ q_{309},\ q_{310},\ q_{311},\ q_{401},\ q_{402}, \\ q_{403},\ q_{404},\ q_{501},\ q_{502},\ q_{503},\ q_{601},\ q_{602},\ q_{603},\ q_{604},\ q_{701},\ q_{702},\ q_{703},\ q_{704},\ q_{801},\ q_{802}, \\ q_{803},\ q_{804},\ q_{805},\ q_{806},\ q_{807},\ q_{808},\ q_{809}. \end{array}
```

Symbol alphabet

Empty symbols alphabet: b;

Input alphabet: 1; Internal alphabet: x, *.

3 Transition Table

The table contains 100 rules.

$Rule_{No}$	$State_{cur}$	$Symbol_{cur}$	$State_{next}$	$Symbol_{next}$	$Head_{move}$
0	q_0	1	q_{101}	x	R
1	q_{101}	1	q_{101}	1	R
2	q_{101}	b	q_{102}	1	R
3	q_{102}	b	q_{103}	*	R
4	q_{103}	b	q_{104}	1	R
5	q_{104}	b	q_{601}	*	L
6	q_{105}	b	q_{106}	1	L
7	q_{106}	*	q_{701}	*	L
8	q_{107}	*	q_{108}	*	L
9	q_{107}	1	q_{107}	1	L
10	q_{108}	*	q_{109}	*	N
11	q_{108}	1	q_{108}	1	L
12	q_{109}	*	q_{109}	*	R
13	q_{109}	1	q_{109}	1	R
14	q_{109}	b	q_{201}	*	N
15	q_{201}	*	q_{202}	*	L
16	q_{201}	1	q_{201}	1	L
17	q_{202}	*	q_{203}	*	R
18	q_{202}	1	q_{202}	1	L
19	q_{202}	b	q_{203}	b	R
20	q_{203}	*	q_{301}	*	N
21	q_{203}	1	q_{204}	b	R
22	q_{204}	*	q_{204}	*	R
23	q_{204}	1	q_{204}	1	R
24	q_{204}	b	q_{201}	1	L
25	q_{301}	*	q_{302}	*	L
26	q_{302}	*	q_{303}	*	L
27	q_{302}	b	q_{302}	b	L
28	q_{303}	*	q_{304}	*	R
29	q_{303}	1	q_{303}	1	L
30	q_{303}	b	q_{304}	b	R
31	q_{304}	*	q_{308}	b	N
32	q_{304}	1	q_{305}	b	R
33	q_{305}	*	q_{306}	*	R
34	q_{305}	1	q_{305}	1	R
35	q_{306}	*	q_{307}	*	L
36	q_{306}	1	q_{307}	1	L
37	q_{306}	b	q_{306}	b	R
38	q_{307}	b	q_{302}	1	L
39	q_{308}	1	q_{309}	1	L

Table continued on next page

Continued

$\overline{Rule_{No}}$	$State_{cur}$	$Symbol_{cur}$	$State_{next}$	$Symbol_{next}$	$Head_{move}$
40	q_{308}	b	q_{308}	b	R
41	q_{309}	b	q_{310}	*	L
42	q_{310}	*	q_{311}	*	R
43	q_{310}	b	q_{310}	1	L
44	q_{311}	*	q_{501}	*	R
45	q_{311}	1	q_{311}	1	R
46	q_{401}	*	q_{402}	*	L
47	q_{401}	1	q_{401}	1	L
48	q_{402}	*	q_{403}	*	L
49	q_{402}	1	q_{402}	1	L
50	q_{403}	*	q_{403}	*	L
51	q_{403}	1	q_{404}	*	L
52	q_{404}	*	q_{404}	*	R
53	q_{404}	1	q_{404}	1	R
54	q_{404}	b	q_{201}	*	N
55	q_{404}	x	q_{801}	x	N
56	q_{501}	*	q_{502}	1	N
57	q_{501}	1	q_{501}	1	R
58	q_{502}	1	q_{502}	1	R
59	q_{502}	b	q_{503}	b	L
60	q_{503}	1	q_{401}	b	L
61	q_{601}	*	q_{602}	*	L
62	q_{601}	1	q_{601}	1	L
63	q_{602}	1	q_{603}	*	L
64	q_{603}	1	q_{604}	1	R
65	q_{603}	x	q_{801}	x	N
66	q_{604}	*	q_{604}	*	R
67	q_{604}	1	q_{604}	1	R
68	q_{604}	b	q_{105}	b	N
69	q_{701}	*	q_{702}	*	L
70	q_{701}	1	q_{701}	1	L
71	q_{702}	*	q_{702}	*	L
72	q_{702}	1	q_{703}	*	L
73	q_{703}	1	q_{704}	1	R
74	q_{703}	x	q_{801}	x	N
75	q_{704}	*	q_{704}	*	R
76	q_{704}	1	q_{704}	1	R
77	q_{704}	b	q_{107}	b	L
78	q_{801}	*	q_{801}	*	R
79	q_{801}	1	q_{801}	1	R

Table continued on next page

Continued

$Rule_{No}$	$State_{cur}$	$Symbol_{cur}$	$State_{next}$	$Symbol_{next}$	$Head_{move}$
80	q_{801}	b	q_{802}	b	L
81	q_{801}	x	q_{801}	x	R
82	q_{802}	*	q_{808}	b	L
83	q_{802}	1	q_{808}	1	L
84	q_{803}	*	q_{803}	*	L
85	q_{803}	1	q_{803}	*	L
86	q_{803}	x	q_{804}	x	R
87	q_{804}	*	q_{804}	*	R
88	q_{804}	1	q_{805}	*	L
89	q_{804}	b	q_{809}	b	N
90	q_{805}	*	q_{805}	*	L
91	q_{805}	1	q_{806}	1	R
92	q_{805}	x	q_{806}	*	N
93	q_{806}	*	q_{807}	1	R
94	q_{807}	*	q_{804}	*	R
95	q_{808}	*	q_{803}	*	L
96	q_{808}	1	q_{808}	1	L
97	q_{809}	*	q_{809}	b	L
98	q_{809}	1	q_f	1	N
99	q_{809}	b	q_{809}	b	L

4 Testing the Machine

C++ Simulator of a Turing machine has been used to compute several Fibonacci numbers. The simulator can be downloaded at

- http://sourceforge.net/projects/turing-machine
- http://alexvn.freeservers.com/s1/turing.html

 $Raw \ logs \ can \ be \ seen \ at \ \texttt{http://groups.google.com/groups?th=1e653c4ef60faa44}$