

NEURAL NETWORKS AND DEEP LEARNING

➤ Why Neural network needs non-linear activation function?

The purpose of the **activation function** is to introduce **non-linearity** into the output of a **neuron**.

... **Neuron** cannot learn with just a **linear function** attached to it, it **requires** a **non-linear activation function** to learn as per the difference w.r.t error.

Handwritten derivation on lined paper showing the composition of two linear functions:

$$\begin{aligned} a^{[1]} &= z^{[1]} = w^{[1]}x + b^{[1]} \\ a^{[2]} &= z^{[2]} = w^{[2]}a^{[1]} + b^{[2]} \\ &= w^{[2]}(w^{[1]}x + b^{[1]}) + b^{[2]} \\ &= \underbrace{w^{[2]}w^{[1]}}_{w'}x + \underbrace{w^{[2]}b^{[1]} + b^{[2]}}_{b'} \\ a^{[2]} &= w'x + b' \end{aligned}$$

The final result shows that the composition of two linear functions is itself a linear function, with the combined weights w' and combined bias b' .

- Neural Network is an outputting a linear function.
- If the input is linear the output is also linear.
- LINEAR + LINEAR = LINEAR
- Linear activation function to be used in Output Layer .

- It is advised to not use Linear Activation Function for Hidden Layers!

FORWARD AND BACKWARD PROPAGATION

Summary of gradient descent

$$dz^{[2]} = a^{[2]} - y$$

$$dW^{[2]} = dz^{[2]} a^{[1]T}$$

$$db^{[2]} = dz^{[2]}$$

$$dz^{[1]} = W^{[2]T} dz^{[2]} * g^{[1]'}(z^{[1]})$$

$$dW^{[1]} = dz^{[1]} x^T$$

$$db^{[1]} = dz^{[1]}$$

$$dZ^{[2]} = A^{[2]} - Y$$

$$dW^{[2]} = \frac{1}{m} dZ^{[2]} A^{[1]T}$$

$$db^{[2]} = \frac{1}{m} \text{np.sum}(dZ^{[2]}, \text{axis} = 1, \text{keepdims} = \text{True})$$

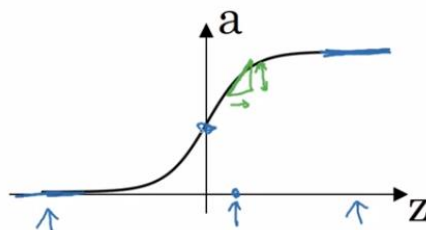
$$dZ^{[1]} = W^{[2]T} dZ^{[2]} * g^{[1]'}(Z^{[1]})$$

$$dW^{[1]} = \frac{1}{m} dZ^{[1]} X^T$$

$$db^{[1]} = \frac{1}{m} \text{np.sum}(dZ^{[1]}, \text{axis} = 1, \text{keepdims} = \text{True})$$

- $G(z)$ is a sigmoid function, then the slope of the function is

Sigmoid activation function



$$g(z) = \frac{1}{1 + e^{-z}}$$

$$\begin{aligned} \frac{d}{dz} g(z) &= \text{slope of } g(z) \text{ at } z \\ &= \frac{1}{1 + e^{-z}} \left(1 - \frac{1}{1 + e^{-z}} \right) \\ &= g(z) (1 - g(z)) \leftarrow \end{aligned}$$

$$z = 10, \quad g(z) \approx 1$$

$$\frac{d}{dz} g(z) \approx 1 \cdot (1 - 1) \approx 0$$

$$z = -10, \quad g(z) \approx 0$$

$$\frac{d}{dz} g(z) \approx 0 \cdot (1 - 0) \approx 0$$

$$z = 0, \quad g(z) = \frac{1}{2}$$

16 $\rightarrow g(z) = \max(0, z)$

17 $g'(z) = \frac{d}{dz} (g(z))$

18 $g'(z) = \begin{cases} 0 & z < 0 \\ 1 & z > 0 \\ \times \text{undefined} & z = 0 \end{cases}$

STEPS TO BUILD A NEURAL NETWORK

11 To build a Neural Network:-

12 1) Define Neural Network structure
14 (No. of input, hidden units)

15 2) Initialize model param.

16 3) Loop

- 17 \rightarrow Implement forward propagation
- \rightarrow Compute Loss
- 18 \rightarrow Implement backward propagation to get gradients
- \rightarrow Update param.

Notes

* build helper func to compute 1-3. and merge them into 1 func = nn-model, after