

# MODPATH-RW: A RANDOM WALK PARTICLE TRACKING CODE FOR SOLUTE TRANSPORT IN HETEROGENEOUS AQUIFERS

DOCUMENTATION OF INPUT-OUTPUT

Version 1.0.0

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#### Chapter 1

## Introduction

This report provides the documentation of input and output for the Random Walk Particle Tracking (RWPT) program MODPATH-RW, implemented as an extension to the source code of MODPATH, released by the U.S. Geological Survey (USGS) (see Pollock, 2016; Pollock & Provost, 2017). Besides the base functionalities, the program implements: (i) new particles displacements based on the RWPT, (ii) Grid Projected Kernel Density Estimation (GPKDE) for smoothed concentration reconstruction, (iii) cell observations for resident and flux concentrations, (iv) and the new interpretation of MODPATH particles as individual solute mass elements with specific dispersion properties. In this sense, the RWPT method requires more computational effort in comparison to the base code, so in order to provide efficient runtimes, development also considered the implementation of parallel processing of particles with the OpenMP library (Pérez-Illanes & Fernàndez-Garcia, 2022). Additional functionalities and program characteristics supporting the previous features are addressed in more detail throughout this document.

Specific topics regarding the routines for reading values from MODFLOW simulation files, or the different grid files supported by MODPATH and their characteristics, are not addressed in much detail in this report, because essentially these remain the same as in the base code and users are referred to the MODPATH documentation for more details (Pollock, 2016).

The main motivation to extend MODPATH source code lies in the inherent interoperability with a variety of MODFLOW models, allowing the immediate integration of the solute transport functionalities with this suite of groundwater flow codes. Following the practices of the USGS, the program is delivered with complementary online repositories and tools to assist the process of writing input files. The program release considers the following repositories

- MODPATH-RW: Main Fortran source code for the program.
- gpkde: Fortran module for GPKDE reconstruction.
- flopyrw: python utilities for writing program input files extended from the flopy package (Bakker *et al.*, 2016).

In the following, specific changes to the main simulation file and the instructions for writing the input files for the new model packages are addressed.

#### Chapter 2

## Input

Input files for MODPATH-RW follow in general a similar logic than those from the base code. In this sense, users are encouraged to follow the documentation of MODPATH-v7 (Pollock, 2016) for the main simulation file and in this chapter only the main notable differences are remarked. Most of the main solute transport functionalities are grouped into packages, and the program will look for specific package files while interpreting the mpnam file (Section 2.2). Package files configure specific aspects of a RWPT simulation like for example the protocols for time step selection, dispersion parameters, just to name a few. This documentation is written considering that the program executable is mpathrw, and in general, considering a simulation file mpathsim.mprw.

A complementary project of this development are the python classes grouped in the repository flopyrw<sup>1</sup>, which contain automated utilities to write the necessary input files for MODPATH-RW. These are an extension from the classes currently available at the project flopy<sup>2</sup> (Bakker *et al.*, 2016) for particle tracking simulations based on MODPATH-v7. At the time of this documentation, python utilities are consistent with the structure of files discussed in the following sections.

### 2.1 Simulation file

This is the main entry point for a MODPATH-RW simulation. It configures the simulation kind and general model parameters. Is the input file required to execute the program

mpathrw mpathsim.mprw

The file parameters are illustrated in Figure (2.1). It should be considered that not all of the parameters are included simultaneously and the presence of some of them is dependent on the values assigned to other parameters. In this regard, for MODPATH-RW, this file has only minor differences and users are encouraged to follow the guidelines explained in Pollock (2016). The differences introduced into this file for the purposes of MODPATH-RW are outlined in the following.

The main simulation file is very dynamic, so an objective of the implementation was to intervene this file only on the strictly necessary parts. The variables that have been given new interpretations or modifications are summarized in Table (2.1). Besides the MODPATH SimulationTypes,

<sup>&</sup>lt;sup>1</sup>https://github.com/upc-ghs/flopyrw

<sup>&</sup>lt;sup>2</sup>https://github.com/modflowpy/flopy

```
0 :Optional comment line
                                     # MODPATH-RW configuration file
  :NameFileName
                                     mpathsim.mpnam
2 :ListingFileName
                                     mpathsim.mplst
3 :i.
         SimulationType
                                     5 1 2 1 0 0 0 1 1 1
         TrackingDirection
                                    mpathsim.mpend
                                                                        4:EndpointFileName
  ii.
         WeakSinkOption
                                     mpathsim.pathline
                                                                        5:PathlineFileName
   iii.
                                    mpathsim.timeseries
   iν.
         WeakSourceOption
                                                                        6:TimeseriesFileName
         BudgetOutputOption
                                    mpathsim.trace
                                                                        7:TraceFileName
   ν.
         TraceMode
                                                                      8: i. TraceParticleGroup ii. TraceParticleID
   vi.
                                     1 100
         TimeseriesOutputOption
                                                                      | 9:BudgetCellCount
   vii.
   viii. ParticlesMassOption
                                                                      | 10:BudgetCellNumbers[BudgetCellCount]
                                     10 20
  ix.
         SpeciesDispersionOption
                                     1
                                                                      |11:ReferenceTimeOption
                                     0.0
         EndpointOutputOption
                                                                      112:ReferenceTime
                                     1 1 0
                                                                      l13:i.
                                                                               StressPeriod
                                     3
                                                                               TimeStep
14:StopTimeOption
15:StopTime
                                     100.0
                                                                          iii. TimeStepFraction
16:TimePointOption
                                     50 2.0
17:i. TimePointCount
                                                                      | 18: TimePointCount
   ii. TimePointInterval
                                     3
                                                                      |19:TimePoints[TimePointCount]
                                     1.0 2.0 3.0
20:ZoneDataOption
21:StopZone
22:Zones[NCPL] or Zones[NROW, NCOL] |
                                     CONSTANT 1
23:DelayingFactorOption
24:DelayingFactor[NCPL] or
                                     CONSTANT 2.0
   DelayingFactor[NROW,NCOL]
                                                                      |25:ParticleGroupCount
                                     PG1
                                                                      |26:ParticleGroupName
                                                                      |27:ReleaseOption
                                     0
                                                                      |28:ReleaseTime
                                     10 0.0 1.0
                                                                      129:i.
                                                                               ReleaseTimeCount
30:ReleaseTimeCount
                                     2
                                                                          ii.
                                                                               InitialReleaseTime
31:ReleaseTimes[ReleaseTimeCount]
                                     0.0 1.0
                                                                          iii. ReleaseInterval
32:StartingLocationsFileOption
                                     EXTERNAL PG1.sloc
   (StartingLocationsFileName)
33:ParticlesMass
                                     0.1
34:SpeciesID
```

Figure 2.1: Illustrative MODPATH-RW simulation file. Example parameters are enclosed between vertical dividers and their names are given in left/right columns.

MODPATH-RW introduces additional interpretations for this parameter, that modify the function that track particles to a version considering Random Walk (RW) which performs the necessary operations for obtaining local quantities determining particles displacement. As in the case of MODPATH, all of the simulations write an endpoint file compiling the last position of particles.

In the last public version of the base code (Pollock & Provost, 2017), an additional parameter was added to the simulation file, controlling the writing of timeseries records (TimeseriesOutputOption). This variable defines whether records are written only for active particles or for all particles. An additional interpretation introduced here is to skip the writing of records, which is useful for simulations pursuing aggregated metrics like concentrations at observation cells or spatial density reconstruction. These are generally based on timeseries simulations, and skipping the writing of records, removes the overhead of this operation and the sometimes very large output files for simulations with high particle resolution.

Two additional options allow the user to indicate further information for the particle groups provided in the main simulation file. Specifically, the parameter 3.viii ParticlesMassOption indicate whether a particle mass should be read for the particle groups, and further, the additional specification of a solute integer identifier for the particles. The latter is in general useful for organizing multiple particle groups into a single substance for the purposes of concentration monitoring.

The last new parameter in this file is the SpeciesDispersionOption which indicates whether mass particles are displaced with the same dispersion parameters or with species specific dispersion. Dispersion parameters are provided in the DSP package which is detailed in Section (2.5).

Table 2.1: New and modified parameters of the main simulation file introduced by MODPATH-RW, identified following the indexation shown in Figure (2.1). All SimulationTypes write an endpoint file.

Id	Parameter	Type	Values
3.i	SimulationType	int	<ol> <li>MODPATH endpoint</li> <li>MODPATH pathline</li> <li>MODPATH timeseries</li> <li>MODPATH pathline-timeseries</li> <li>MODPATH-RW timeseries</li> <li>MODPATH-RW pathline-timeseries</li> <li>MODPATH-RW endpoint</li> </ol>
3.vii	TimeseriesOutputOption	int	<ul><li>0: Write timeseries only for active particles</li><li>1: Write timeseries for all particles</li><li>2: Skip timeseries writer</li></ul>
3.viii	ParticlesMassOption	int	0: Particles groups follow classical specification 1: Request 33:ParticlesMass for particle groups 2: Request both mass and 34:SpeciesID. In this case, SpeciesID is also requested for other packages leading to the creation of particle groups (IC,SRC)
3.ix	SpeciesDispersionOption	int	<ul><li>0: All particles with the same dispersion parameters.</li><li>1: Specific dispersion related to SpeciesID.</li></ul>
3.x	EndpointOutputOption	int	<ul><li>0: Write the classical endpoint file.</li><li>1: Write the simplified endpoint file for mass particles.</li></ul>
33	ParticlesMass	float	Particles mass used for concentration postprocesses.
34	SpeciesID	int	Identifies the particle group as a specific species. In case ParticlesMassOption=2 and single dispersion, the SpeciesID is identificatory and organizes particle groups as a species for postprocess (OBS,GPKDE).

#### 2.2 Name file

The name file acts as coordination of the packages included on a simulation. In classical MOD-PATH, this file contains the link to the MODFLOW model files, and the basic package (MPBAS). For MODPATH-RW, this is the entry point for the new packages implemented in the program following a similar structure than the classical approach for MODFLOW-based software, where an identificatory package code is provided followed by the name of the file storing the specifications. The new packages are summarized in Table (2.2), and an example name file for a MODPATH-RW simulation considering a MODFLOW-6 flow model is shown in Figure (2.2). For a RW simulation, the DSP and RWOPTS packages are mandatory as they control the necessary parameters for computing particles displacements. Some packages are allowed to contain multiple instances of the parameters specification and begin with a number indicating how many instances are included in the file. As a remark, this does not mean that the package is given multiple times in the name file.

Table 2.2: Packages implemented for MODPATH-RW. The column "Multi" indicates whether the package accepts multiple specifications on a single file. The "Optional" column is in terms of a RW simulation. For classical MODPATH runs, none of these packages is required.

Code	Name	Explanation		Optional
RWOPTS	Random Walk options	Controls RW displacements, time step	No	No
DSP	Dispersion	Dispersion parameters	Yes	No
GPKDE	GPKDE	Smoothed density reconstruction	No	Yes
IC	Initial conditions	Initial distribution of concentrations	Yes	Yes
SPC	Species	Individualize species parameters	Yes	Yes
OBS	Observations	Monitor resident and flux concentrations	Yes	Yes
SRC	Sources	Mass injection cells	Yes	Yes
IMP	Impermeable cells	Specular reflection cells	No	Yes

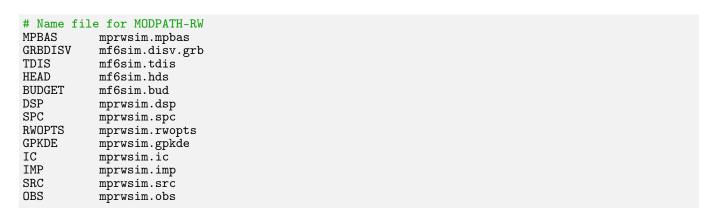


Figure 2.2: Example MODPATH-RW name file for MODFLOW-6 simulation with DISV grid.

#### 2.3 Basic file

This file store cell porosities and default IFACEs for stress packages not able to store this parameter as auxiliary variable. The structure and interpretation of this file remains exactly the same as in MODPATH-v7 so no additional comments are provided here (see Pollock, 2016).

## 2.4 Random walk options (RWOPTS)

This package is mandatory for a RW simulation. It specifies basic parameters for computing the displacement of particles like the time step selection criteria, the advection model and the dimension mask. An example specification file is shown in Figure (2.3) and the interpretation of parameter names is shown in Table (2.3).

The last parameter in this file allows to select the function for random number generation. The latter is optional and by default selected by compiler. While using the ifort compiler some parallel scalability issues where detected while obtaining random numbers based on the intrinsic random\_number. An external module generating random numbers with the Ziggurat method was included into the program, which is explicitly parallelized and solves the scalability issue.

Figure 2.3: Illustrative specification for Random Walk options package. Parentheses remark conditional parameters (see Table 2.3).

Table 2.3: Parameter details for RWOPTS file shown in Figure (2.3).

$\overline{\operatorname{Id}}$	Parameter	Type	Values
0	TimeStepSelection	string	ADV: selection of time step with advection criteria using CFL.  DISP: selection of time step with dispersion criteria using CTDisp.  MIN_ADV_DISP: selects the minimum, requires CFL and CTDisp.  FIXED: the same for all particles, given in TimeStep.
1	CFL	float	Include if TimeStepSelection is ADV or MIN_ADV_DISP.
2	CTDisp	float	Include if TimeStepSelection is DISP or MIN_ADV_DISP.
3	TimeStep	float	Include if TimeStepSelection is FIXED.
4	AdvectionKind	string	EULERIAN (default) or EXPONENTIAL.
5	DimensionMask	int	RW displacements in active (1) dimensions. 0 means inactive.
6	RandomGenerator	int	<ul><li>0: selected by compiler.</li><li>1: based on intrinsic random_number.</li><li>2: uses the Ziggurat method.</li></ul>

## 2.5 Dispersion (DSP)

Package groups dispersion parameters. Accepts multiple specifications following the simplified structure

```
0 :NDsp
[1]:DspSpecification
```

where NDsp is the number of dispersion specifications (DspSpecification) given in the file. Two different alternatives for specifying dispersion parameters are implemented on this release. The first is the classical dispersion model with linear isotropic dispersivities (Fig. 2.4), interpreting pore-diffusion plus the longitudinal and transverse values. The second alternative employs the axisymmetric formulation from Lichtner et al. (2002), considering the vertical axis for these purposes (Fig. 2.5). In this case, besides pore-diffusion, two longitudinal dispersivities plus two transverse dispersivities are specified. Following the notation of the axisymmetric formulation, the index H indicates that the value is perpendicular to the symmetrix axis (the vertical axis), and the index H indicates that the value is parallel to the symmetry axis. Regardless of the given dispersion model, parameters can be specified as domain constants or read with the free-format input of MODPATH for each model layer. More details are presented in Tables (2.4) and (2.5).

If multiple dispersion specifications are given, but SpeciesDispersionOption=0, then only the first specification will be read. In case the simulation is configured with species specific dispersion, then all specifications will be loaded. However, the assignment of the different dispersion models will be conditioned to the presence of the SPC package, as discussed in the following section. Each specification begins with an identificatory string name for the dispersion data, followed by the dispersion model and input format, which configures the reading of dispersion parameters.

```
0 :DspName
                              DSP1
1 :i.DspModel ii.InputFormat
                              10
                                      1
2 :DMEff
                              I CONSTANT
                                            0.00000E+00
                                                                #dmeff layer 1
                                            10.00000E+00
3 :AlphaL
                              CONSTANT
                                                                #alphal layer 1
4 :AlphaL
                              | CONSTANT
                                            10.00000E+00
                                                                #alphal layer 1
```

Figure 2.4: Illustrative structure for specification of dispersion parameters for a single layer model.

```
0 :DspName
                               IDSP1
1 :i.DspModel ii.InputFormat
2 :DMEff
                               | CONSTANT
                                             0.00000E+00
                                                                 #dmeff
                                                                           layer 1
3 :AlphaLH
                               | CONSTANT
                                             10.00000E+00
                                                                 #alphalh layer 1
4 :AlphaLV
                                             5.00000E+00
                                                                 #alphalv layer 1
                               | CONSTANT
5 : AlphaTH
                               | CONSTANT
                                             1.000000E+00
                                                                 #alphath layer 1
                               | CONSTANT
                                             1.00000E-01
 :AlphaTV
                                                                 #alphatv layer 1
```

Figure 2.5: Illustrative structure for specification axisymmetric dispersion model, for a single layer domain.

Table 2.4: Parameter details for dispersion specification shown in Figure (2.4).

Id	Parameter	Type	Values	
0	DspName	string	Less than 20 characters.	
1.i	DspModel	int	1: linear, isotropic. The only implemented.	
1.ii	InputFormat	int	<ul><li>0: Domain uniform parameters.</li><li>1: Distributed parameters, free-format input.</li></ul>	
2	DMEff	float	Effective molecular diffusion (corrected by tortuosity).	
3	AlphaL	float	Longitudinal dispersivity.	
4	AlphaT	float	Transverse dispersivity.	

Table 2.5: Dispersivities for specification shown in Figure (2.5).

$\overline{\operatorname{Id}}$	Parameter	Type	Values
3	AlphaLH	float	Longitudinal dispersivity perpendicular to the vertical axis.
4	AlphaLV	float	Longitudinal dispersivity parallel to the vertical axis.
5	AlphaTH	float	Transverse dispersivity perpendicular to the vertical axis.
6	AlphaTV	float	Transverse dispersivity parallel to the vertical axis.

## 2.6 Species (SPC)

This package organizes the different species instances. These serve as a link between different particle groups, also coordinating the dispersion parameters for simulations with species specific dispersion. The package accepts the specification of multiple species, following the simplied structure

```
0 :NSpecies
[1]:SpeciesSpecification
```

where NSpecies indicates how many specifications are given. For MODPATH-RW, this package is optional and different scenarios are possible depending on the values given to the simulation parameters SpeciesDispersionOption and ParticlesMassOption, and if the SPC package was specified or not.

In case the package is not specified and ParticlesMassOption=2, then different species will be internally created, using the SpeciesID given by the user. If ParticlesMassOption!=2 and the package is not given, a single placeholder species is created, to which all of the particle groups in the simulation are linked.

If the package is given the program will interpret the specifications. If ParticlesMassOption!=2, then the program will require that the user indicates the particle groups associated with the species (Fig. 2.6). In case ParticlesMassOption=2, the program will read the specifications and relate the SpeciesID given by users while defining particle groups. In this case, it is internally understood that the identifying numbers given to the particle groups have a minimum value of one and a maximum equal to NSpecies given in the SPC package.

For simulations with a single dispersion model for all particles, then the grouping provided by species will be only identificatory. Concentration related postprocesses will consider that species are different, but the transport model will employ the same dispersion parameters for all particles. If the simulation considers species specific dispersion, then this package becomes mandatory because is the only way for the program to know which dispersion model should be related to which species.

```
0 : SpcName | SRC1

1 : (NPGroups) | 2

2 : (ParticleGroups[NPGroups]) | 1 2

3 : (DspName) | DSP1
```

Figure 2.6: Illustrative structure for specification of species. Parentheses remark conditional parameters.

In case that the particle groups are specified by the user to the species in the SPC package, the group numbers should be considered carefully. Besides the classical particle groups, some packages will increase the number of groups (IC,SRC) and the user needs to keep track of their ids. In this sense, for simulations with complex specification of sources and initial conditions, it might be easier to provide the SpeciesID with ParticlesMassOption=2 and let the program interpret which particle group belongs to which species.

Table 2.6: Parameter details for dispersion specification shown in Figure (2.4).

$\overline{\operatorname{Id}}$	Parameter	Type	Values	
0	SpcName	string	Less than 20 characters.	
1	NPGroups	int	Read if ParticlesMassOption!=2. At least 1.	
2	ParticleGroups	int	Read if ParticlesMassOption!=2.	
3 DspName string Identifier of dispersion to which the species is a Read if SpeciesDispersionOption=1.		Identifier of dispersion to which the species is related. Read if SpeciesDispersionOption=1.		

## 2.7 Initial conditions (IC)

This package is intended to specify an initial distribution of concentrations which is internally transformed into a distribution of particles, for a given scale of particles mass. The expected values are explicitly interpreted as resident concentrations, in all cases interpreted with the free-format input of MODPATH. This information combined with porosities, cell volumes and delaying factors, allow to estimate the total mass inside model cells. An example specification is shown in Figure (2.7) illustrating only one concentration distribution, however, the program is able to interpret multiple specifications. Details of parameters are show in Table (2.7).

The program will enforce consistency of total mass by recalculating the value of particles mass with two different methodologies. The first integrates the solute plume at the domain level in order to obtain the total mass. Combined with the estimated total number of particles, recompute particles mass and assign this value to all particles. A second alternative allows to perform a similar procedure, but in this case at a cell level. This means that particles from different cells might have different characteristic mass. The user can specify a parameter for determining the placement of particles inside each cell. The latter can be equispaced, similar to a uniform distribution. A second alternative allows to perturbate the previous distribution by a random number proportional to half the particle spacing, known as quasi-random. A third alternative allows to place particles randomly inside each cell.

For each initial condition specification, MODPATH-RW will create a particle group whose name is given by InitialConditionName, which will be appended to the currently existing particle groups. An aspect to consider for the particles created with this method, is that their release time is zero by definition, for consistency with the idea of an initial condition.

```
0 :NInitialConditions
                            1
[1 :InitialConditionName
                            IIC1
2 : InitialConditionFormat
                           |1
 3 :i. ParticlesMass
                            1500.0
                                       0
    ii. ParticlesDistrib
                                                                             4 : (SpeciesID)
                            |1
                                          1 (3E15.6) -1 #ic1 layer 1
5 : ResidentConcentration
                            INTERNAL
                            |1.593200E+00
                                            3.470600E+00
                                                           4.769200E+00
/1]
                            |8.877000E+00
                                            1.032400E+01
                                                            1.181560E+01
                            1.661340E+01
                                            1.834760E+01
                                                           2.016920E+01
                            2.634600E+01
                                            2.872420E+01
                                                           3.131140E+01
                            INTERNAL
                                          1 (3E15.6) -1 #ic1 layer 2
                            0.00000E+00
                                            0.00000E+00
                                                           0.00000E+00
                            4.184800E+00
                                            6.062600E+00
                                                           7.428200E+00
                            |1.189620E+01
                                            1.346920E+01
                                                           1.506860E+01
                            11.996520E+01
                                            2.161440E+01
                                                            2.326660E+01
```

Figure 2.7: Example input for initial condition package, considering a structured model with  $(N_{lay}, N_{row}, N_{col}) = (2, 4, 3)$ . Square brackets in parameters column indicate a list of sub-specifications and parenthesis remarks conditional parameters.

Table 2.7: Parameter details for initial condition shown in Figure (2.7).

Id	Parameter	Type	Values
0	NInitialConditions	int	At least 1, determine how many are interpreted.
1	InitialConditionName	string	Less than 20 characters.
3	InitialConditionFormat	int	Read concentrations with free-format input.  0: Particles with unique mass, global mass consistency.  1: Particles with cell-specific mass, local consistency.
3.i	ParticlesMass	float	To tranform the total mass concentration into a number of particles. Determines particle resolution.
3.ii	ParticlesDistrib	int	Determines the placement of particles inside cells.  0: Particles are equispaced.  1: Particles are in quasi-random array.  2: Random locations.
4	SpeciesID	int	Read if ParticlesMassOption=2.
5	ResidentConcentration	float	The initial condition specified with free-format input.

## 2.8 Sources (SRC)

This package configures the source mass influx from a flow-model boundary condition, in cases where the flow-rate through the boundary is positive, entering the groundwater flow-model. The combination of flow-rates, concentrations and particles mass is transformed into a release of particles characterizing the boundary. Specifications for this package share some similarities with the Source and Sink Mixing (SSM) packages from MODFLOW (Langevin et al., 2017) and MT3DMS (Zheng & Wang, 1999). However, in case of negative flow-rates, the boundary will not release particles and the number of extracted particles is an output result that could be monitored, for example, with observation cells.

The package accepts multiple specifications on a single file, following the simplified structure:

0 :NSources

[1]:SourceSpecification

where the first parameter NSources is a positive integer indicating the length of the list of specifications (SourceSpecification) to be interpreted. Two specification formats are implemented:

- AUXILIARY (AUX): concentrations are extracted from auxiliary variables stored in the MOD-FLOW budget file. MODPATH-RW generates a timeseries of flow-rates from a given budget header.
- SPECIFIED (SPEC): concentrations, injection times and cells are given by the user for a determined budget header.

The package file can contain combined (multiple) specification formats. In the following, both specification formats are addressed with more details.

#### 2.8.1 AUXILIARY

Auxiliary variables have been progressively integrated into the different versions of MODFLOW. In MODFLOW-2005 only some packages were compatible with this approach accepting up to 20 auxiliary variables (see Harbaugh, 2005), whereas in MODFLOW-6 most of the stress packages write output files capable of storing an unlimited number of auxiliary variables (Table 36, p. 288 in Langevin et al., 2022). In MODPATH-v7, auxiliary variables are employed for interpretation of the IFACE parameter (Pollock, 2016). For practical purposes, auxiliary variables offer high flexibility to users allowing them to directly relate concentrations and flow-rates for a set of cells, at specific flow-model stress periods. This format will create a MODPATH particle group for each given auxiliary variable, under the assumption that these represent solute concentrations.

Figure (2.8) presents the variables structure and example values for a source specification with the AUXILIARY format, and the interpretation of parameters is shown in Table (2.8). In plain words, the specification begins with an identificatory name, after which the AUX format is indicated. The format allows for multiple budget names to be read, indicating the set of auxiliary variables to be extracted

```
0 :SourceName
                                   SRC1
 1 :SourceFormat
                                   AUX
2 :NBudgets
                                   1
  :i.BudgetName ii.IFaceOption
                                   WEL-1
  :NAuxVariables
                                   3
[5:i. AuxVarName
                                   CONCSPC1
                                                1.0
                                                     2 2 2
                                                             1
    ii. ParticlesMass
                                   CONCSPC2
                                                     4 2 2
                                                0.5
                                                             2
                                   CONCSPC3
                                                     4 4 1
    iii.Nx iv.Ny v.Nz
                                                0.1
/5] vi. (SpeciesID)
/3]
```

Figure 2.8: Example specification structure for source format AUXILIARY. Square brackets indicate a list of sub-specifications and parenthesis remarks optional parameters.

and parameters that allow to transform the concentration data into particles. The program detects automatically which flow-model cells are associated with the budget name, running over all the simulation stress periods. For each auxiliary variable, the user should specify the magnitude of particles mass and a template distribution (Nx,Ny,Nz) to be applied for each cell detected in the budget name, which determine the resolution with which the source is represented. This distribution of particles is modified according to the dimensions mask provided in the RWOPTS package, and for inactive dimensions a default value of 1 is assigned to the template. For each auxiliary variable, the program will look for an integer solute identifier in case that ParticlesMassOption=2. For each budget name, a flag indicates whether the IFACE auxiliary variable is read, and in such a case, the template of particles is applied on the face of cells. For consistent results, the value of IFACE should not change in time.

For simulations based on MODFLOW-6, multiple packages of the same kind can be specified, so the value of BudgetName should be the identificatory name given to each instance of a package (the value stored in TXT2ID2, see Langevin et al., 2022). For simulations based on MODFLOW-2005, only some packages allow to specify auxiliary variables. The user can specify BudgetName as the three character identifier of the budget or its full budget header (WEL or WELLS for the well package). For budget header names with white spaces, the value should be specified in between quotes. Packages currently supported are shown in Table (2.9).

Table 2.8: Parameter details for specification with AUXILIARY format shown in Figure (2.8).

Id	Parameter	Type	Values	
0	SourceName	string	Less than 20 characters.	
1	SourceFormat	string	Less than 20 characters.	
2	NBudgets	int	At least 1.	
3.i	BudgetName	string	Less than 20 characters.	
3.ii	IFaceOption	int	<ul><li>0: IFACE is not read from budget.</li><li>1: IFACE is read from budget.</li></ul>	
4	NAuxVariables	int	At least 1.	
5.i	AuxVarName	string	Less than 20 characters.	
5.ii	ParticlesMass	float	Greater than zero.	
5.iii	Nx	int	At least 1.	
5.iv	Ny	int	At least 1.	
5.v	Nz	int	At least 1.	
5.vi	SpeciesID	int	Read if ParticlesMassOption=2.	

Table 2.9: MODFLOW-2005 packages supported to be specified as sources with the AUXILIARY format.

Package id	Budget header
DRN	DRAINS
DRT	"DRAINS (DRT)"
GHB	"HEAD DEP BOUNDS"
RIV	"RIVER LEAKAGE"
WEL	WELLS

```
:SourceName
                                                             ISRC2
                                                             SPEC
    :SourceFormat
 1
 2
   :NBudgets
                                                             |1
   :i.BudgetName ii.IFaceOption iii.(DefaultIFace)
                                                            "CONSTANT HEAD"
[3
    :i.CellInput ii.NCells iii.CellFormat iv.ConcPerCell
                                                            1 2 0 1
[5
    :i.Cells ii.(IFace)
                                                            |1 1 5
\5] :
                                                            11 1 10 4
   :i.NSpecies ii.TemplateOption
                                                            |2 1
 6
[7
    :i.Nx ii.Ny iii.Nz
                                                            12 2 2
                                                            |4 4 2
/7]
[8] :ParticlesMass
                                                            11.0 5.0
[9] :(SpeciesID)
                                                             | 1
 10 :NTimeIntervals
                                                            14
[11 :i.TStart ii.TEnd iii.ConcSpeciesCell
                                                            10.0
                                                                    10.0
                                                                          55.5
                                                                                45.5
                                                                                       75.5
                                                                                             15.5
                                                                                             26.6
                                                             15.0
                                                                   17.5
                                                                          66.6
                                                                                56.6
                                                                                       26.6
                                                                   20
                                                                          87.7
                                                                                67.8
                                                                                       27.7
                                                             17.5
                                                                                             27.7
\11]
                                                            122.5
                                                                    30
                                                                          57.7
                                                                                37.1
                                                                                      17.7
                                                                                             27.7
\3]
```

Figure 2.9: Example specification structure for source format SPECIFIED. Square brackets indicate a list of sub-specifications and parenthesis remarks conditional parameters.

#### 2.8.2 SPECIFIED

This second input format offers an additional alternative for users to indicate mass sources. It may be useful for users not familiarized with auxiliary variables, or to configure mass sources for those packages from MODFLOW-2005 that do not support said variables. In this case, the format is called SPECIFIED because users need to explicitly specify the cells and concentration timeseries for a given budget. A prototype file structure is presented in Figure (2.9), and most of the variables share the same meaning than for the case with auxiliary variables. The variables with different interpration are shown in Table (2.10).

The format provides different alternatives for reading source cells. These can be interpreted from the budget file, specified as a list of cell ids or as a three dimensional array. Only in the case the cells are given as list the program offers the users to read different concentration values for each cell. Meaning that in the case the source cells are read from the budget file or as three dimensional array, then the same concentration is assumed for all cells. Format requires that the user indicates time intervals, where concentrations are interpreted as step-wise quantities. Start and end times are relative to the MODFLOW simulation time, and are made consistent with the MODPATH reference and stop times indicated in the simulation file. The only restriction for the intervals specified by the user is that the intervals are not overlapping, but the program allows discontinuous time. In this sense, MODPATH-RW will create a timeseries of flow-rates extracted from the budget file that is consistent with the MODFLOW simulation steps and the user given intervals. As before, this format will create a MODPATH particle group for each of the species indicated in the input file.

Table 2.10: Parameter details for specification with SPECIFIED format shown in Figure (2.9). Only parameters with different meaning than those from Table (2.9) are presented.

Id	Parameter	Type	Values
3.ii	IFaceOption	int	0: IFACE is not read 1: IFACE is read after cell id (if CellInput=1)
3.iii	DefaultIFace	int	Default if IFaceOption=1 and no value is given after cell id.  If CellInput=0 or 2 applies DefaultIFace to all cells.
4.i	CellInput	int	0: cells are read from budget 1: cells are given as a list of cell id's 2: cells are read with U3D reader
4.ii	NCells	int	Number of cells if CellOption=1
4.iii	CellFormat	int	0: Cells read as Lay Row Col 1: Cells read as nodes (CellNumber)
4.iv	ConcPerCell	int	0: Same species concentration(s) for all cells. 1: Different concentration(s) values for each cell.
5.i	Cells	int	Do not include if CellInput=0 Cell identifiers written according to CellFormat if CellInput=1 U3D array with 0 and 1 for active cells if CellInput=2
5.ii	IFace	int	IFace value for cell if IFaceOption=1 and CellInput=1
6.i	NSpecies	int	Number of concentrations to be specified. At least 1
6.ii	TemplateOption	int	0: Only one particle template read, same for all species. 1: Read NSpecies templates.
8	ParticlesMass	float	One column for each specie
9	SpeciesID	int	Read if ParticlesMassOption=2. One column per specie.
10	NTimeIntervals	int	At least 1. Referent to MODFLOW times.
11.i	TStart	float	Beginning of the time interval.
11.ii	TEnd	float	End of the time interval. Intervals should not overlap.
11.iii	- Read NSpecies columns if CellInput=1 and		Concentration values during the time interval.  Read NSpecies columns if CellInput=0 or CellInput=2. Read NSpecies columns if CellInput=1 and ConcPerCell=0. Read NSpecies for each Cell if CellInput=1 and ConcPerCell=1.

## 2.9 Grid projected kernel density estimation (GPKDE)

This package configures the parameters for the spatial concentration reconstruction. Is an optional specification and performs kernel density estimation over the set of particles considered to be of the same species. Spatial reconstruction is performed by default at the end of each timeseries step configured in the main simulation file. However, users can indicate in the package configuration file specific times where reconstruction should be performed, similar to the time point data indicated for the timeseries.

Reconstruction is performed on a regular grid, which is independent of the flow-model grid, considering reference axes aligned with the MODPATH interpretation of coordinates. The module receives the three-dimensional global particle coordinates as input data, with their respective particle mass.

Based on the grid specifications, the GPKDE module will determine whether reconstruction should be performed with 1, 2 or 3-dimensional kernels. The latter is decided based on the relation between the domain and bin sizes. In case the bin size on a given direction equals to the domain size, then reconstruction will consider that said dimension is compressed. The same is not true while computing the histogram. In this case, if the user wants to ignore a coordinate of the particles while calculating the histogram, then the bin size should be specified to be zero in said dimension. Additional set of parameters allow the user to perform reconstruction on a sliced manner. The latter is useful, for example, for three-dimensional problems where the horizontal extent is significantly larger than the vertical. In said case, a two-dimensional reconstruction can be performed for each model layer and in general this is the recommended approach for quasi two-dimensional problems, avoiding issues due to the reflection correction for kernels when intersecting domain boundaries.

```
0: i.
         OutputFile
                                  mprwsim.gpkdeout
                                                  0.0
                                                                      1: DomainOrigin [x y z]
    ii.
         (ColumnFormat)
                                     0.0
                                            0.0
    iii. (FileFormat)
                                                               0.05
                                                                               DomainSize [x y z]
                                  100.0
                                           50.0
                                                  5.0
                                                                      2: i.
 3: BinSize [x y z]
                                                                               (GridAllocFormat)
                                     2.0
                                            2.0
                                                  2.5
                                                                          ii.
   i. SlicedReconstruction
                                          3
                                  1
                                                                          iii. (BorderFraction)
    ii. (SlicedDimension)
                                  10
                                                                      5: NOptLoops
                                  0
 6: i. SkipErrorConvergence
                                         0.02
    ii. (RelativeConvergence)
                                               0
                                         0
                                                                               KernelDatabase
                                  1
                                                                      7: i.
 8: KDB (MinHL DeltaHL MaxHL)
                                  0.5
                                         0.1
                                               10.0
                                                                          ii.
                                                                               (BoundKernelSize)
   i. InitialSmoothingFormat
                                         2.0
                                                                          iii. (IsotropicKernels)
                                  0
    ii. (BinSizeFactor)
                                                                     10: AsResidentConcentration
11: EffectiveWeightFormat
                                  0
12: i. (TimePointOption)
                                         0
                                  1
    ii. (SkipInitialCondition)
                                | 3
                                         2.0
                                                                    |13: i.
                                                                             TimePointCount
14: TimePoints[TimePointCount]
                                               3.0
                                                                          ii. TimePointInterval
```

Figure 2.10: Illustrative specification for spatial reconstruction module. Parentheses remark optional parameters

Table 2.11: Parameter details for specification GPKDE package shown in Figure (2.10).

$\overline{\operatorname{Id}}$	Parameter	Type	Values
0.i	OutputFile	string	Less than 200 characters.
0.ii	ColumnFormat	int	<ul><li>0: Output bin ids and densities.</li><li>1: Output bin ids, cell coordinates and densities.</li><li>2: Output cell coordinates and densities.</li></ul>
0.iii	FileFormat	int	<ul><li>0: Output file as text-plain.</li><li>1: Output file as binary.</li></ul>
1	DomainOrigin	float	Coordinates of the origin for the GPKDE grid.
2.i	DomainSize	float	Extent of the domain for the GPKDE grid.
2.ii	GridAllocFormat	int	<ul><li>0: Grid allocated according to domain.</li><li>1: Grid adapts to the particle coordinates.</li></ul>
2.iii	BorderFraction	int	Read if GridAllocFormat=1. Defines buffer distance for grid allocation, added to the extext of the particle distribution.
3	BinSize	float	Size of the reconstruction cells, regular.
4.i	SlicedReconstruction	int	For models with $d>1$ dimensions, performs reconstruction with $d-1$ dimensional kernels on each slice of SlicedDimension.  0: Disabled.  1: Enabled.
4.ii	SlicedDimension	int	The dimension to be considered compressed for kernels functions.
5	NOptLoops	int	Maximum number of bandwidth optimization loops.
6.i	SkipErrorConvergence	int	<ul><li>0: Break bandwidth optimization by error checks.</li><li>1: Skip error checks and do NOptLoops.</li></ul>
6.ii	RelativeConvergence	int	Threshold to determine reconstruction convergence.  Not read if SkipErrorConvergence=1.
7.i	KernelDatabase	int	<ul><li>0: Kernels calculated in real time for a given bandwidth.</li><li>1: Pre compute a kernel database for a set of bandwidths.</li></ul>
7.ii	BoundKernelSize	int	<ol> <li>Bound kernel size based on domain restrictions.</li> <li>Bound kernel size based on MinHL, MaxHL</li> <li>Unbounded kernel sizes.</li> </ol>
7.iii	IsotropicKernels	int	<ul><li>0: Kernels are anisotropic in multidimensional problems.</li><li>1: Kernels are isotropic.</li></ul>
8	KDB	float	If KernelDatabase=1, define a range of non-dimensional bandwidths for precomputing the kernel database.  If BoundKernelSize=1 will read MinHL and MaxHL.
9.i	InitialSmoothingFormat	int	<ul><li>0: Automatic initial kernel selection (Silverman, 1986).</li><li>1: Initial kernel as a factor amplifying cell size.</li></ul>
9.ii	BinSizeFactor	float	Amplifies cell size for initial bandwidth selection. Only read if InitialSmoothingFormat=1.
10	AsResidentConcentration	int	<ul><li>0: Report reconstruction as total mass density.</li><li>1: Report as resident concentration (aqueous), if possible.</li></ul>

Table 2.12: Parameter details for specification GPKDE package shown in Figure (2.10), continued.

Id	Parameter	Type	Values
11	EffectiveWeightFormat	int	Defines the protocol for processing mass particles.  0: Global effective mass to obtain histogram (Kish, 1965, 1992)  1: Average mass to obtain equivalent histogram.  2: Bandwidth selection based on real histogram.  3: Local effective histogram for bandwidth selection.
12.i	TimePointOption	int	<ul><li>0: Reconstruction performed at timeseries time points.</li><li>1: Read TimePointCount and TimePointInterval.</li><li>2: Read TimePointCount and TimePoints,</li></ul>
12.ii	SkipInitialCondition	int	<ul><li>0: Reconstruction performed for initial particle positions.</li><li>1: Skip reconstruction of tracking time zero.</li></ul>
13.i	TimePointCount	unt int The number of reconstruction time points. Read if TimePointOption=1 or TimePointOption=2.	
13.ii	TimeInterval	float	The interval for equispaced reconstruction stages if TimePointOption=1.
14	TimePoints	float	The array of times if TimePointOption=2.

## 2.10 Impermeable cells (IMP)

This is an optional package for MODPATH-RW, which determine which cells are impermeable for mass particles. Similarly, the first parameter of this package (DefaultBoundary) indicates the default behavior when reaching a flow-model boundary face. By default, if the package is not given, flow-model boundaries are considered to be impermeable (DefaultBoundary=1) meaning that particles will rebound specularly. A value of zero (0) indicates that boundaries are open.

The second parameter (ImpFormat) indicates the method in which the impermeable cells are specified. Impermeable cells can be linked to the flow-model IBOUND, which is static in time. Similarly, these could be linked to the IBOUNDTS variable, which is introduced by MODPATH to monitor those flow-model cells that get dry during the simulation. The latter changes in time and is offered to users as an alternative to specify impermeable cells. The final format will read a layered array of integers from the variable (ImpCells) using the free-format input, where the value of zero (0) indicates that the cell is permeable and a value of 1 that the cell is impermeable. The main restriction for the latter is that not all cells can be marked as impermeable. In case the package is not specified all the interior cells are marked as permeable.

<pre>0 : DefaultBoundary 1 : ImpFormat 2 : ImpCells</pre>		0 2 INTE	RNAL		1	(614)	-1 #impcells layer 1
•		0	0	0	0	0	0
	İ	0	0	0	0	0	0
	İ	0	0	1	1	0	0
	İ	0	0	1	1	0	0
	1	0	0	0	0	0	0
	I	0	0	0	0	0	0

Figure 2.11: Illustrative specification of a flow-model with  $(N_{lay}, N_{row}, N_{col}) = (1, 6, 6)$  cells with an interior region of mass impermeable cells.

Table 2.13: Parameter	details f	for imperm	neable cells	s specifi	cation s	hown in	Figure (	(2.11)	١.
rabic 2:10: I aramicul	accurry 1	or minporm	ICCOCIO CCII	J DPCCIII.	COULT D	110 11 111	- 15 are (		, •

Id	Parameter	Type	Values
0	DefaultBoundary	int	<ul><li>0: If no cell connection, open boundary.</li><li>1: If no cell connection, rebound boundary.</li></ul>
1	ImpFormat	int	<ul><li>0: Follow flow-model IBound.</li><li>1: Follow flow-model IBoundTS which also includes dry cells.</li><li>2: Read layered array of impermeable cells.</li></ul>
2	ImpCells	int	Layered array, read with free-format input.

## 2.11 Observations (OBS)

This package configures the monitoring of concentration with observation cells. The package allows the interpretation of multiple specifications on a single file following the simplified structure

```
0 :NObs
[1]:ObsSpecification
```

where NObs is the number of specifications (ObsSpecification) included in the file. The program will interpret as many specifications as indicated by the parameter NObs. Two kind of observations have been implemented into MODPATH-RW: observation of resident concentrations, which is obtained by monitoring the dissolved mass inside a cell (or group of cells) and dividing by a cumulative water volume; and observation of flux-concentrations, which require a sink flow rate and the simulation configured as strong-sinks in order to remove the particles from the system. A more detailed description on the conceptual differences between resident and flux concentrations can be found in Parker & van Genuchten (1984) and Kreft & Zuber (1986). Both these observations can be configured for a group of cells and a concentration timeseries can be obtained as postprocess of time dependent records.

#### 2.11.1 RESIDENT

Observations of RESIDENT kind are tightly connected to the timeseries specification of the simulation. This is because resident concentrations have to be computed for pre-established times, where dissolved mass within a cell is aggregated. In this sense, users should configure the timeseries simulation with regular (uniform) timesteps. For the timeseries reconstruction stage, in scenarios where the observation considers postprocessing, the program will automatically compute the size of the histogram bin as the step given for TimePoints. Users may provide some additional parameters for the reconstruction process. In case of smoothed reconstruction, these are a simplified set of the options given for the spatial reconstruction package.

An example specification is shown in Figure (2.12) with parameter details indicated in Table (2.14).

```
0: ObsName
                               IOBS1
                               RESIDENT
1: ObsFormat
2: ObsOutputFile
                               |obscells1.obs
3: i. OutputOption
                               11
                                    1
                                          1
                                                      4: i. NOptLoops ii. RelativeConvergence
   ii. PostprocessOption
                                   0.01
                               110
   iii.ReconstructionOptions
                                    3.0
                                                      5: i. InitialSmoothingFormat
                               11
6: EffectiveWeightFormat
                               13
                                                         ii. BinSizeFactor
7: i. CellInputOption
                               |1
                                    2
                                        1
   ii. NCells
                               1145
                                                     |[8 : Cells
   iii.CellFormat
                                                     [8/|
```

Figure 2.12: Example observation specification employing the format RESIDENT.

Table 2.14: Parameter details for specification of RESIDENT observation shown in Figure (2.12).

$\operatorname{Id}$	Parameter	Type	Values
0	ObsName	string	Less than 20 characters.
1	ObsFormat	string	RESIDENT or RES.
2	ObsOutputFile	string	Less than 200 characters.
3.i	OutputOption	int	0: ObsOutputFile with observation records. 1: Postprocesses in ObsOutputFile, second file with records. 2: ObsOutputFile with postprocessed records.
3.ii	PostprocessOption	int	<ul><li>0: Histogram timeseries reconstruction of records.</li><li>1: Histogram and smoothed timeseries reconstruction of records.</li></ul>
3.iii	ReconstructionOptions	int	<ul><li>0: Do not interpret reconstruction options [4-6].</li><li>1: Interpret reconstruction options.</li></ul>
4.i	NOptLoops	int	The limit number of bandwidth optimization loops for reconstruction
4.ii	RelativeConvergence	float	Tolerance for determining reconstruction convergence.
5.i	InitialSmoothingFormat	int	Determines the procotol for initial bandwidth selection.  0: Automatic based on Gaussian distribution (Silverman, 1986).  1: Initial bandwidth as a factor amplifying timeseries timestep.
5.ii	BinSizeFactor	float	Read if InitialSmoothingFormat=1.
6	EffectiveWeightFormat	int	Processing protocol for the particles with non-uniform mass.  0: Global effective mass to obtain histogram (Kish, 1965, 1992)  1: Average mass to obtain equivalent histogram.  2: Bandwidth selection based on real histogram.  3: Local effective histogram for bandwidth selection.
7.i	CellInputOption	int	<ul><li>0: Cells are given as a list of cell ids.</li><li>1: Cells read with free-format input.</li></ul>
7.ii	NCells	int	Number of cells if CellInputOption=0. At least 1.
7.iii	CellFormat	int	0: Cells read as Lay Row Col. 1: Cells read as nodes (CellNumber).

#### 2.11.2 FLUX

The second kind of observations monitors flux concentrations. Based on the number of particles (and their total mass) exiting through a strong-sink, the program estimates the mass flux leaving the system. In combination with the extraction flow-rate, a timeseries of flux concentrations can be obtained. Specification for this observation is similar to the previous case, being the only difference the ObsFormat parameter which can adopt the values FLUX or SINK. An aspect to remark of this observation is that it requires the cells to have a sink flow-rate. In case a cell with no extraction flow-rate is given, no records will be generated and hence the observation will remain empty. An example specification is seen in Figure (2.13). Until this implementation of MODPATH-RW, the postprocessing of this observation is also linked to the timeseries points provided by the user, but not the writing of records, which is performed only once per particle when arriving to an extraction

cell.

```
0: ObsName
                                IOBS2
1: ObsFormat
                                | FLUX
2: ObsOutputFile
                                |obscells2.obs
3: i. OutputOption ii. PostprocessOption
                                |1
                                      1
                                    0.01
                                10
                                                        4: i. NOptLoops ii. RelativeConvergence
   iii.ReconstructionOptions
                                     3.0
                                                        5: i. InitialSmoothingFormat
                                |1
6: EffectiveWeightFormat
                                                            ii. BinSizeFactor
                                13
7: i. CellInputOption
                                     2
                                11
   ii. NCells
                                                       |[8 : Cells
                                |1
                                     10 4
   iii.CellFormat
                                1
                                     8
                                         3
                                                       [8/|
```

Figure 2.13: Example observation specification employing the format FLUX.

Both observation formats can be combined on the same input file, as many times as the user require (see for example Fig. 2.14). It is recommended that users verify that a cell is being specified only once in observations to avoid inconsistencies. In case a cell appears in more than one specification, the program will consider that the cell belongs to the last interpreted specification.

```
2
OBS1
RESIDENT
obscells1.obs
1 1 0
1 2 1
145
146
OBS2
FLUX
obscells2.obs
2 1 0
1 2 0
1 10 4
1 8 3
```

Figure 2.14: Example observation file with two specifications of different kind.

#### Chapter 3

## Output

The base output files from MODPATH remain as they are configured in the original program. The structure of endpoint, pathline and timeseries files can be considered to be the same as the one shown in Pollock (2016). However, a new alternative for endpoint files is implemented, including solute related data as discussed later in this chapter.

In the following, new output files and some modifications done to existing output files are detailed.

#### 3.1 List file

It is typical in MODFLOW-based programs to write a file that registers some of the configuration parameters and decisions performed by the program based on the user input. MODPATH also generate said file and for the purposes of MODPATH-RW it has been extended to report information specific to each package. This file might be useful as a summary of the simulation for successful terminations, and a source of information in case the simulation terminated unexpectedly or by some of the errors handled by the program.

The interpretation of packages is preceded by a header indicating which package is being read. For example, for the DSP package

```
"MODPATH-RW DSP file data"
"----"
```

Although the list file still contains some of the original messages implemented in MODPATH, most of the structure of this file has been modified to report aspects related to the MODPATH-RW simulations and users are encouraged to familiarize with it.

#### 3.2 Observations

Observations generate different output files depending on their type, providing the necessary information for users to obtain a timeseries of concentrations. In this regard, both observation types may generate up to two output files, depending on the configuration of the observation. These output files are identified in the following as ObsRecords, which contains the source information for postprocessing and ObsPostprocess, containing the concentration timeseries.

#### 3.2.1 RESIDENT

#### ObsRecords

File is written in text-plain format when users indicate OutputOption=0 or 1. In the first case, the records file adopts the name OutputFileName. In the second, the records file name is a modified version of OutputFileName with prepended substring rec\_. For clarity, a observation with OutputFileName=obscells1.obs and OutputOption=1, will generate a file called rec\_obscells1.obs. File columns are:

```
1 : TimePointIndex (int)
                                  8 : CellNumber
                                                       (int)
2 : CummTimeStep
                    (float)
                                  9 : Layer
                                                       (int)
3 : TrackingTime
                    (float)
                                  10: DelayingFactor (float)
                                  11: WaterVolume
                                                       (float)
4 : ParticleID
                    (int)
5 : ParticleMass
                    (float)
                                  12: GlobalX
                                                       (float)
6 : ParticleGroup
                                  13: GlobalY
                    (int)
                                                       (float)
                                  14: GlobalZ
                                                       (float)
7 : SpeciesID
                    (int)
```

#### ObsPostprocess

This file is provided in cases where the user specify OutputOption=1 or 2. The number of file columns are dependent on the number of species and PostprocessOption.

#### For PostprocessOption=0:

```
1 : TimePointIndex (int)
2 : TimePoint (float)
3 : CummWaterVolume (float)
4 : ConcHistogram[NSpecies] (float)
```

#### For PostprocessOption=1:

```
1 : TimePointIndex (int)
2 : TimePoint (float)
3 : CummWaterVolume (float)
4 : ConcHistogram[NSpecies] (float)
5 : ConcGPKDE[NSpecies] (float)
```

#### 3.2.2 FLUX

#### ObsRecords

This kind of observation follow the same OutputOption behavior than the discussed for resident concentrations.

#### File columns are

```
1 : TimePointIndex (int)
                                     6 : ParticleGroup
                                                         (int)
2 : CummTimeStep
                                     7 : SpeciesID
                    (float)
                                                         (int)
3 : TrackingTime
                    (float)
                                     8 : CellNumber
                                                         (int)
4 : ParticleID
                    (int)
                                     9 : Layer
                                                         (int)
                                     10: SinkFlowRate
5 : ParticleMass
                    (float)
                                                         (float)
```

#### ObsPostprocess

The only difference of this file with the one presented for resident concentrations is the meaning of the third column, which in this case is the cumulative flow-rate of the observation.

#### For PostprocessOption=0:

```
1 : TimePointIndex (int)
2 : TimePoint (float)
3 : CummSinkFlowRate (float)
4 : ConcHistogram[NSpecies] (float)
```

#### For PostprocessOption=1:

```
1 : TimePointIndex (int)
2 : TimePoint (float)
3 : CummSinkFlowRate (float)
4 : ConcHistogram[NSpecies] (float)
5 : ConcGPKDE[NSpecies] (float)
```

## 3.3 Spatial GPKDE

Writing of this file is controlled by the GPKDE library. As indicated previously, GPKDE considers an independent grid with respect to the flow-model grid and bin indexes are with respect to the given domain origin. Similarly, the reported values by the module are interpreted as resident concentration (dissolved) in the case that both porosity and delaying factor were uniform in space. In case any of these is not uniform, then the reported values should be considered as total mass density (aqueous plus sorbed). In any case, both Density and Histogram columns are considered to have the same units/dimensions. Users need to consider that the time reported in these output files corresponds to the time points selected for reconstruction, that is, it could be coincident with the timeseries points array or following the independent time points defined for the reconstruction package.

Depending on the value of the parameter ColumnFormat (0.ii in Table 2.11), the output can have different structures.

ColumnFormat=0: Time and species id's, bin id's and densities.

```
1 : TimePointIndex
                        (int)
2 : TimePoint
                        (float)
3 : SpeciesID
                        (int)
4 : idBinX
                        (int)
5 : idBinY
                        (int)
6 : idBinZ
                        (int)
7 : Density
                        (float)
8 : Histogram
                        (float)
```

ColumnFormat=1: Time and species id's, bin id's, center cell coordinates and densities.

```
: TimePointIndex
                      (int)
                                        7
                                            : X
                                                                  (float)
: TimePoint
                      (float)
                                           : Y
                                                                  (float)
                                           : Z
: SpeciesID
                      (int)
                                         9
                                                                  (float)
: idBinX
                                         10 : Density
                                                                  (float)
                      (int)
: idBinY
                      (int)
                                         11 : Histogram
                                                                  (float)
: idBinZ
                      (int)
```

ColumnFormat=2: Time and species id's, center cell coordinates and densities.

```
1 : TimePointIndex
                        (int)
2 : TimePoint
                        (float)
3 : SpeciesID
                        (int)
4 : X
                        (float)
5 : Y
                        (float)
6:Z
                        (float)
7 : Density
                        (float)
8 : Histogram
                        (float)
```

## 3.4 Endpoint for mass particles

This file is a modified version from the original endpoint file in MODPATH, without the local cell coordinates and face information, and including parameters like the particle mass and the corresponding solute identification. The columns of this file follow the structure:

```
(int)
(int)
                                       9 : InitialCellNumber
                                                                            17: FinalGlobalX
1 : SequenceNumber
                                                               (int)
                                                                                                    (float)
2 : ParticleGroup
                                       10: InitialLayer
                                                                (int)
                                                                            18: FinalGlobalY
                                                                                                    (float)
3 : SpeciesID
                                       11: InitialGlobalX
                           (int)
                                                                (float)
                                                                                                    (float)
                                                                            19: FinalGlobalZ
4 : ParticleID
                                       12: InitialGlobalY
                                                                (float)
                                                                            20: FinalZone
                                                                                                    (int)
                           (int)
5
  : Status
                           (int)
                                       13: InitialGlobalZ
                                                                (float)
6 : ParticleMass
                                       14: InitialZone
                           (float)
                                                                (int)
7 : InitialTrackingTime
                           (float)
                                       15: FinalCellNumber
                                                                (int)
8 : TrackingTime
                           (float)
                                       16: FinalLayer
                                                                (int)
```

As in MODPATH, records for unreleased particles are not written to the endpoint file. Notice that the information in this file can be used for mass balance purposes. For example, users may make use of the Status column to detect particles removed at sink cells, eventually grouping by cells and aggregating the particle mass.

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