

Basic Electronics Engineering (Spring 2024)

Resources of PPT:

- ❑ www.google.com
- ❑ Digital Design, 4th Edition
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Combinatorial Circuit



Digital Circuits are of two types:

- Combinatorial: The combinational circuit is time-independent. The output it generates does not depend on any of its previous inputs.
- Sequential: Sequential circuits are the ones that depend on clock cycles. They depend entirely on the past as well as the present inputs for generating output.

What is a Combinational Circuit?

- The output of a Combinational Circuit depends entirely on the present input.
- It exhibits a faster speed.
- It is comparatively easier to design.
- No feedback is present between the input and output.
- The combinational circuit depends on time.
- Logic gates form the building blocks of such circuits.
- One can make use of it for both boolean and arithmetic operations.
- They don't hold the capacity of storing any state.
- These circuits do not have a clock- thus, they don't require triggering.
- They do not possess any memory element.
- Users can feasibly use as well as handle them.
- Example – Demultiplexer, Multiplexer, Decoder, Encoder, etc.

What is a Sequential Circuit?

- The output of a Sequential Circuit depends on both- past as well as present inputs.
- It works at a comparatively slower speed.
- The design of these circuits is comparatively much tougher than the Combinational Circuit.
- A feedback path exists between the output and the input.
- The circuit is time-dependent.
- Flip-flops constitute the building blocks of such a circuit.
- People mainly use them for storing data and information.
- They possess the capability of storing any data state or retaining an earlier state at any given point.
- Because a Sequential circuit depends on a clock, it usually requires triggering.
- They always possess a memory element.
- A user may not be able to handle and use these circuits easily.
- For Example – Counters, Flip-flops, etc.

Combinatorial Circuit

Half Adder

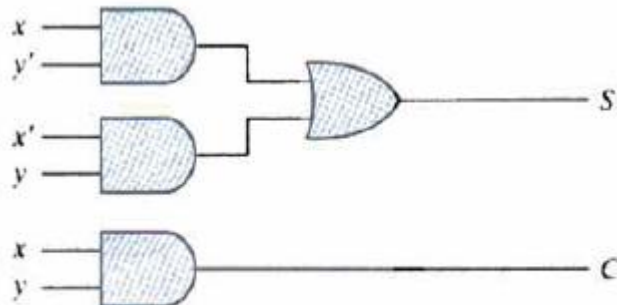
Half Adder

x	y	C	S
0	0	0	0
0	1	0	1
1	0	0	1
1	1	1	0

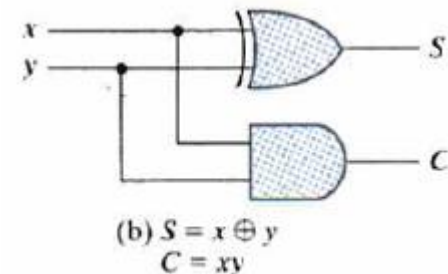
The simplified Boolean functions for the two outputs can be obtained directly from the truth table. The simplified sum-of-products expressions are

$$S = x'y + xy'$$

$$C = xy$$



(a) $S = xy' + x'y$
 $C = xy$



Combinatorial Circuit

Full Adder

Full Adder

x	y	z	C	S
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1

$x \backslash yz$		y			
		00	01	11	10
x	0	m_0	m_1	m_3	m_2
	1	m_4	m_5	m_7	m_6

Truth Table for Sum S

$$S = x'y'z + x'yz' + xy'z' + xyz$$

$x \backslash yz$		y			
		00	01	11	10
x	0	m_0	m_1	m_3	m_2
	1	m_4	m_5	m_7	m_6

Truth Table for Carry C

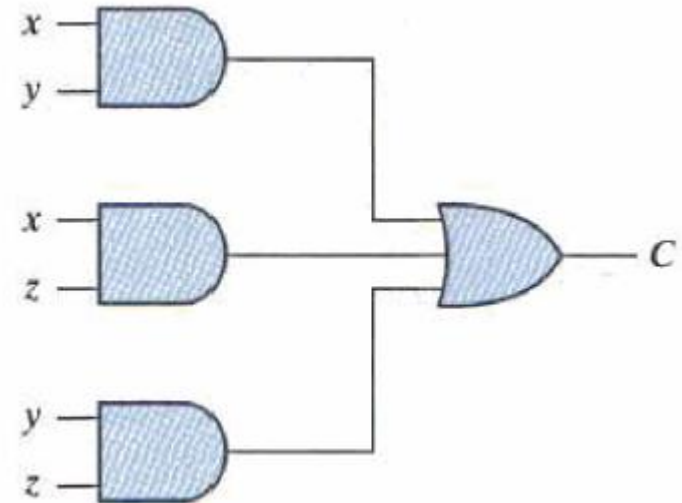
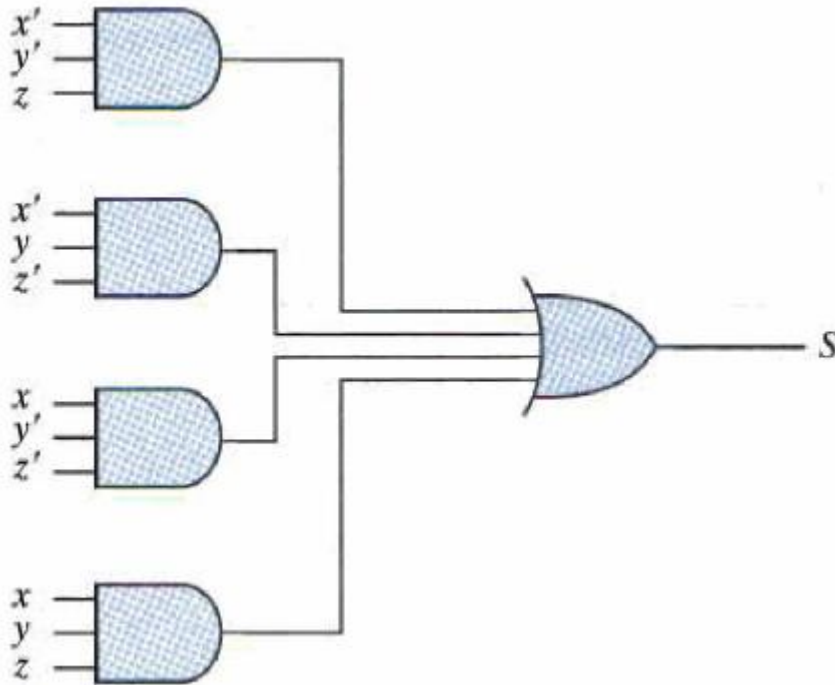
$$C = xy + xz + yz$$

Combinatorial Circuit

Full Adder

$$S = x'y'z + x'yz' + xy'z' + xyz$$

$$C = xy + xz + yz$$

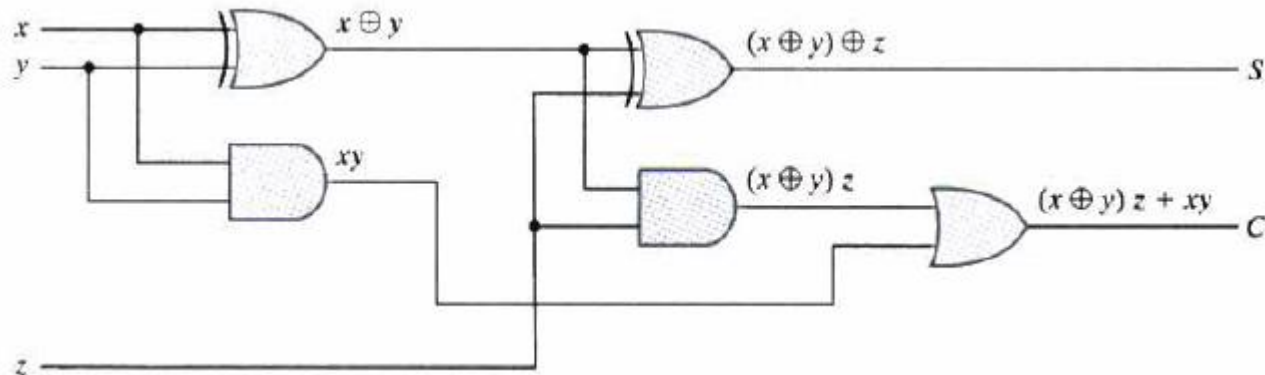


Combinatorial Circuit

Full Adder

$$\begin{aligned} S &= x'y'z + x'yz' + xy'z' + xyz \\ &= z'(xy' + x'y) + z(xy + x'y') \\ &= z'(xy' + x'y) + z(xy' + x'y)' \\ &= z \oplus (x \oplus y) \end{aligned}$$

$$\begin{aligned} C &= xy + xz + yz \\ &= xy + z(x + y) \\ &= xy + z(x[y + y'] + y[x + x']) \\ &= xy + z(xy + xy' + xy + x'y) \\ &= xy + xyz + z(xy' + x'y) \\ &= xy(1 + z) + z(xy' + x'y) \\ &= xy + z(x \oplus y) \end{aligned}$$



Combinatorial Circuit : Half Subtractor



Half Subtractors

Half Subtractors are a type of digital circuit that calculates the arithmetic binary subtraction between two single-bit numbers. It is a circuit with two inputs and two outputs.

For two single-bit binary numbers A and B, a half subtractor produces two outputs.

- **A** is known as the Minuend Bit
- **B** is called Subtrahend Bit.
- **Output D** is the difference between the two input bits (A-B).
- **Output P** is the previous borrow between the two input bits (A-B).

The previous borrow is for the most significant bit (MSB).

Combinatorial Circuit : Half Subtractor



Case 1: $A = 0, B = 0$;

According to Binary subtraction, the difference of these numbers is 0 with no previous borrow.

0

– 0

0

Hence, **$D = 0, P = 0$**

Case 2: $A = 0, B = 1$;

According to Binary subtraction, the difference between these two numbers is 1 with a previous borrow of 1.

0

– 1

–1 (Previous Borrow)

1

Hence, **$D = 1, P = 1$**

Combinatorial Circuit : Half Subtractor



Case 3: A= 1, B= 0;

As per Binary subtraction, the difference between these two numbers is 1 with no previous borrow.

1

– 0

1

Hence, **D= 1, P= 0**

Case 4: A= 1, B= 1;

According to Binary subtraction, the difference between these two numbers is 1 with no previous borrow.

1

– 1

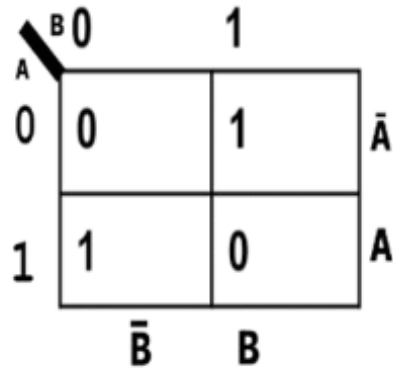
0

Hence, **D= 0, P= 0**

Combinatorial Circuit: Half Subtractor

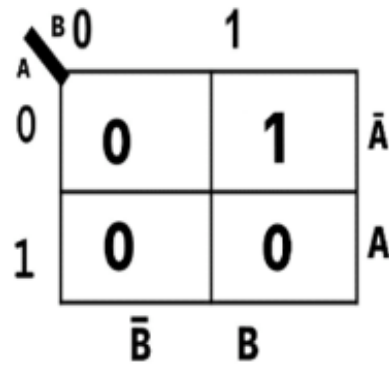


A	B	Difference (S)	Previous Borrow (P)
0	0	0	0
0	1	1	1
1	0	1	0
1	1	0	0



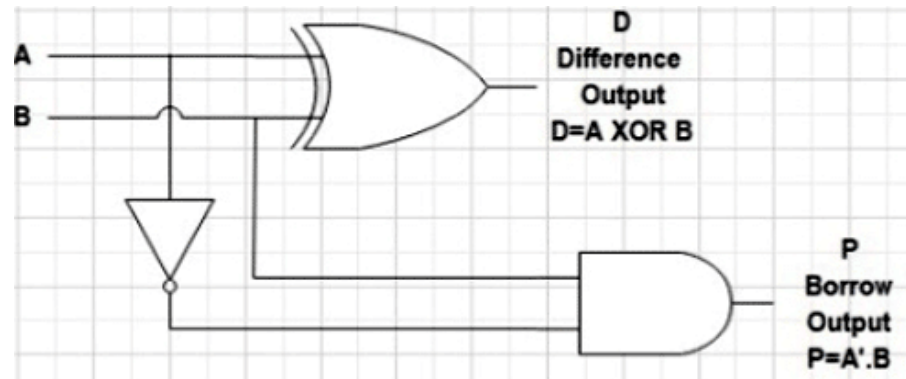
Half Subtractor Karnaugh Map for Difference

$$D = A'B + AB'$$

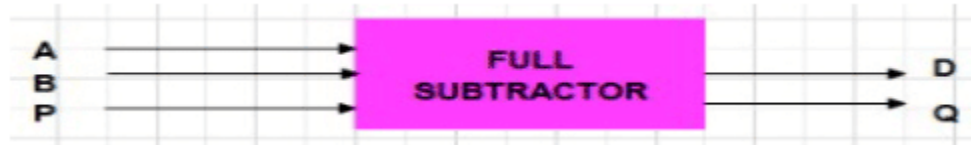


Half Subtractor K-Map for Borrow

$$P = A' \bullet B$$



Combinatorial Circuit: Full Subtractor



For three single-bit binary numbers A, B, and P, the full subtractor circuit generates two single-bit binary outputs D (Difference), and Q (Borrow Output).

- **A** is the Minuend.
- **B** is the Subtrahend.
- **P** is the Previous Borrow Bit.
- **D** is the Difference between A, B, and P.
- **Q** is the Borrow Output.

Combinatorial Circuit: Full Subtractor



Case 1: $A = 0$, $B = 0$, and $P = 0$;

The difference of the three binary numbers 0, 0, and 0 produces a difference of 0 and generates no borrow output.

0

-0

-0

0

Hence, **$D = 0$, $Q = 0$**

Case 2: $A = 0$, $B = 0$, and $P = 1$;

The difference of the three binary numbers 0, 0, and 1 produces a difference of 1 and generates a borrow output bit.

0

-0

-1

→1

1

Hence, **$D = 1$, $Q = 1$**

Combinatorial Circuit: Full Subtractor



Case 3: A= 0, B= 1, and P= 0;

The difference of the three binary numbers 0, 1, and 0 produces a difference of 1 and generates a borrow output bit.

0

-1

→1

-0

1

Hence, **D= 1, Q= 0**

Case 4: A= 0, B= 1, and P= 1;

The difference of the three binary numbers 0, 1, and 1 produces a difference of 0 and generates a borrow output bit.

0

-1

→1

-1

0

Hence, **D= 0, Q= 1**

Combinatorial Circuit: Full Subtractor



Case 5: A= 1, B= 0, and P= 0;

The difference of the three binary numbers 1, 0, and 0 produces a difference of 1 and generates no borrow output.

1
-0
-0

0

Hence, **D= 1, Q= 0**

Case 6: A= 1, B= 0, and P= 1;

The difference of the three binary numbers 1, 0, and 1 produces a difference of 0 and generates no borrow output.

1
-0
-1

0

Hence, **D= 0, Q= 0**

Combinatorial Circuit: Full Subtractor



Case 7: A= 1, B= 1, and P= 0;

The difference between the three binary numbers 1, 1, and 0 produces a difference of 0 and generates no borrow output.

1

-0

-0

0

Hence, **D= 0, Q= 0**

Case 8: A= 1, B= 1, and P= 1;

The difference between the three binary numbers 1, 1, and 1 produces a difference of 1 and generates a borrow output bit.

The difference between A=1 and B=1 is 0. P=1 gets subtracted from this 0 to produce an output of 1 by generating a borrowed output bit.

1

-1

-1

→1

1

Hence, **D= 1, Q= 1**

Combinatorial Circuit: Full Subtractor



A	B	P	Difference (D) $D = A - B - P$	Borrow Output (Q)
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	0	1
1	0	0	1	0
1	0	1	0	0
1	1	0	0	0
1	1	1	1	1

	$\bar{B}\bar{P}$	$\bar{B}P$	BP	$B\bar{P}$	
A	0	1	0	1	0
\bar{A}	1	0	1	0	1
	00	01	10	11	

Full Subtractor karnaugh Map for Difference

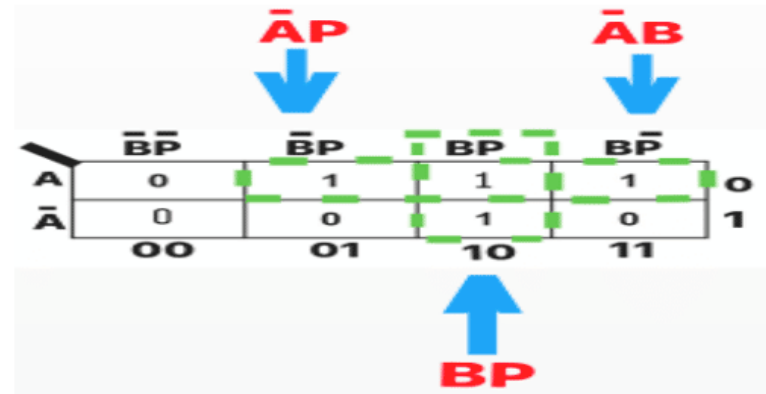
$$D = (\bar{A}\bar{B}P) + (\bar{A}B\bar{P}) + (A\bar{B}\bar{P}) + (ABP)$$

$$D = P(\bar{A}\bar{B} + AB) + \bar{P}(\bar{A}B + A\bar{B})$$

$$D = P(\overline{AB + A\bar{B}}) + \bar{P}(\bar{A}B + A\bar{B})$$

$$D = P \oplus (\bar{A}B + A\bar{B})$$

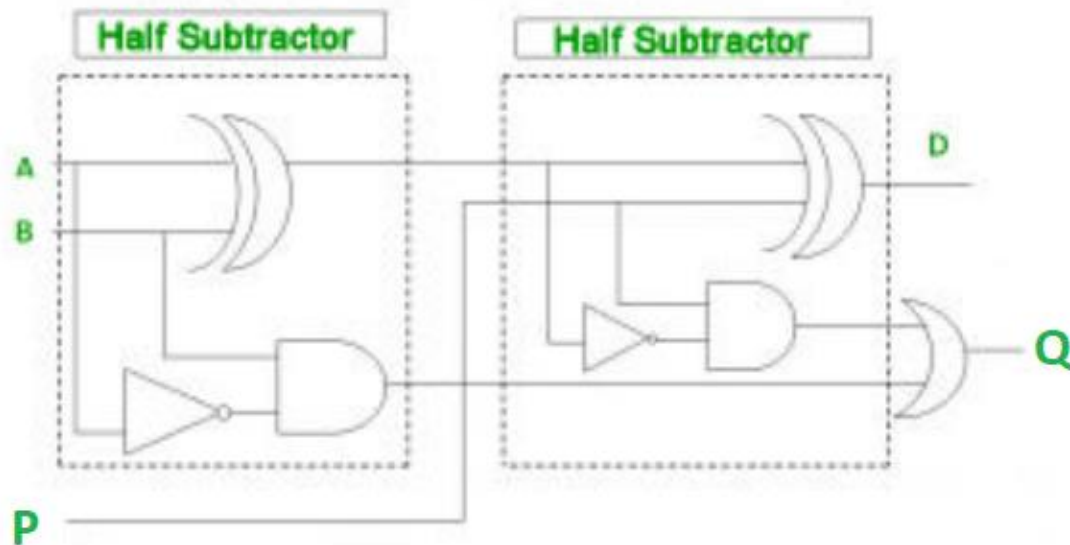
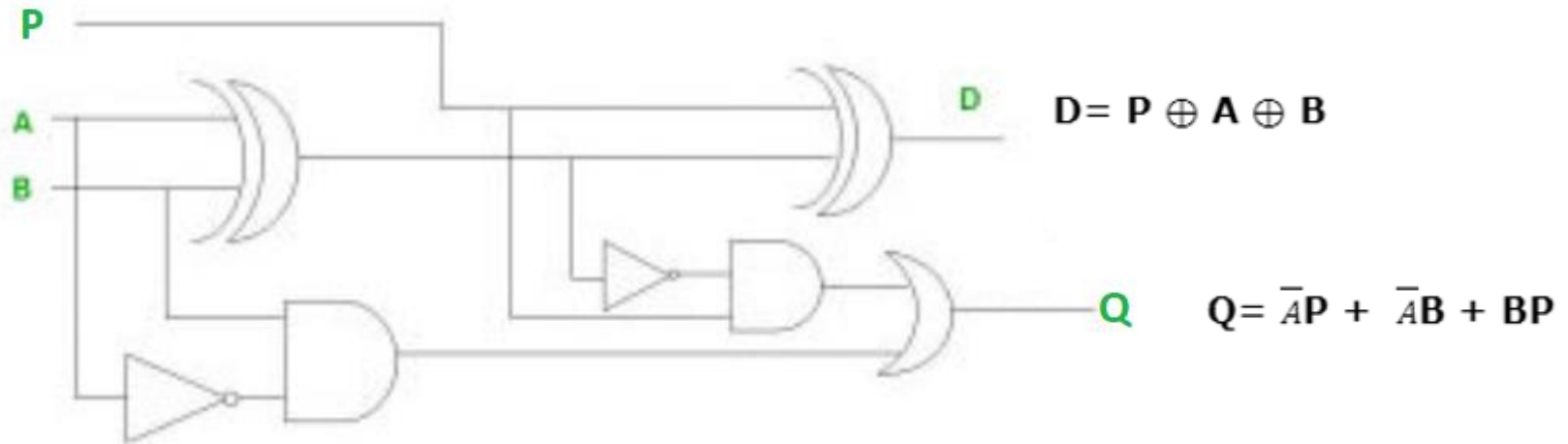
$$D = P \oplus A \oplus B$$



Full Subtractor karnaugh Map for Borrow

$$Q = \bar{A}P + \bar{A}B + BP$$

Combinatorial Circuit: Full Subtractor



Combinatorial Circuit



DECODERS

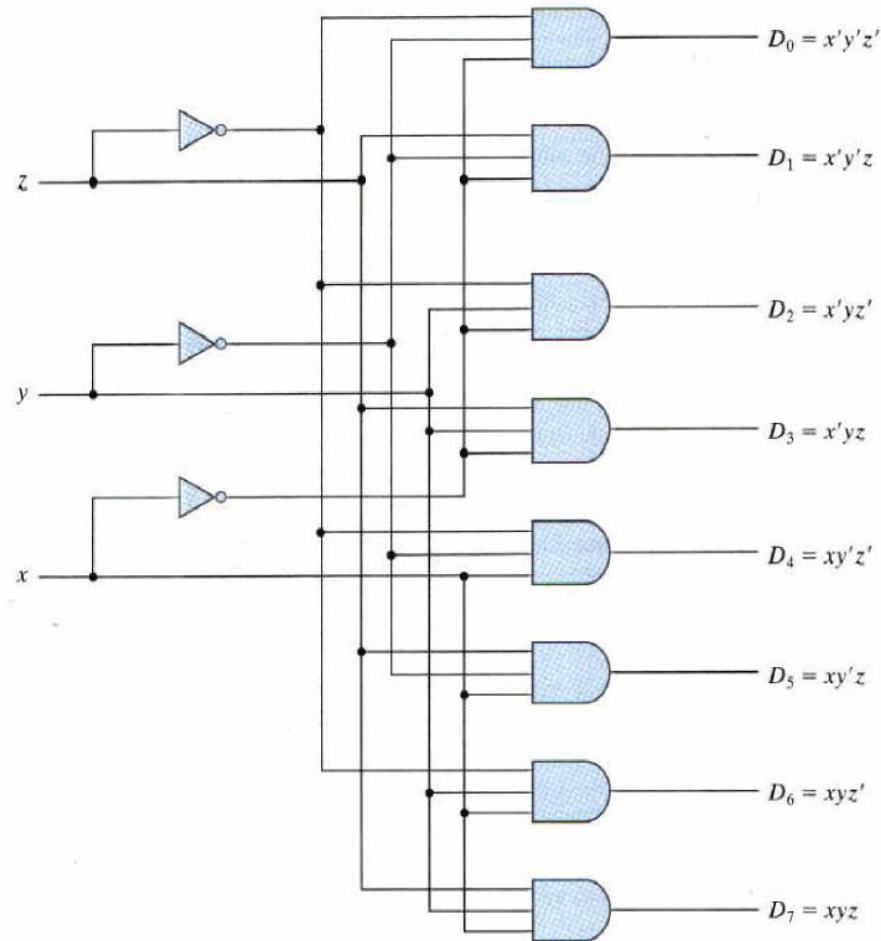
Discrete quantities of information are represented in digital systems by binary codes. A binary code of n bits is capable of representing up to 2^n distinct elements of coded information. A *decoder* is a combinational circuit that converts binary information from n input lines to a maximum of 2^n unique output lines. If the n -bit coded information has unused combinations, the decoder may have fewer than 2^n outputs.

Truth Table of a Three-to-Eight-Line Decoder

Inputs			Outputs							
x	y	z	D_0	D_1	D_2	D_3	D_4	D_5	D_6	D_7
0	0	0	1	0	0	0	0	0	0	0
0	0	1	0	1	0	0	0	0	0	0
0	1	0	0	0	1	0	0	0	0	0
0	1	1	0	0	0	1	0	0	0	0
1	0	0	0	0	0	0	1	0	0	0
1	0	1	0	0	0	0	0	1	0	0
1	1	0	0	0	0	0	0	0	1	0
1	1	1	0	0	0	0	0	0	0	1

Combinatorial Circuit

DECODERS



Combinatorial Circuit



ENCODERS

Truth Table of an Octal-to-Binary Encoder

Inputs								Outputs		
D_0	D_1	D_2	D_3	D_4	D_5	D_6	D_7	x	y	z
1	0	0	0	0	0	0	0	0	0	0
0	1	0	0	0	0	0	0	0	0	1
0	0	1	0	0	0	0	0	0	1	0
0	0	0	1	0	0	0	0	0	1	1
0	0	0	0	1	0	0	0	1	0	0
0	0	0	0	0	1	0	0	1	0	1
0	0	0	0	0	0	1	0	1	1	0
0	0	0	0	0	0	0	1	1	1	1

$$z = D_1 + D_3 + D_5 + D_7$$

$$y = D_2 + D_3 + D_6 + D_7$$

$$x = D_4 + D_5 + D_6 + D_7$$