# Modular Inverse Reinforcement Learning on Human Motion

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## **Abstract**

Human learning is modeled as reinforcement learning in the literature. However, human is able to learn complex tasks efficiently, while reinforcement learning is known for suffering from the curse of dimensionality. We observe that tasks that human handles can usually be decomposed into smaller tasks, and human can learn small tasks quickly, and then learn how to integrate them to solve the original task. In this paper, we find that modular reinforcement learning can be used to model human behavior. We report experiments of using modular inverse reinforcement learning to find the way that human combines sub-tasks, given samples of real human data. Our simulation demonstrates that human behavior can be well explained in this way.

Keywords: Reinforcement learning, human motion, inverse learning

#### 1 Introduction

A large body of evidence from human and other primate studies suggest that they use reinforcement signals to learn tasks and reinforcement learning has proved to be a good model for this process. However humans are able to learn and carry out very complex tasks involving many different objectives. How can they do this? The likelihood is that they use reinforcement in this context as well but most formal reinforcement learning models do not scale well with increasing complexity.

One promising possibility is that the complex task can be broken down into sub-tasks that are each learned separately [6, 5, 1]. For certain task venues, this decomposition allows the behavior in the complex task to be specified as a weighted sum of individual sub-task priorities. This paper explores the use of such a decomposition to characterize complex behavior of subjects in a virtual reality environment. The methodology of [5] allows the task priorities to be estimated using the subjects' behavioral data.

Our experimental analysis shows that the modular reinforcement can be a surprisingly good model of behavior, predicting individual subjects' sub-task priorities in a way that explains their behavioral choices.

This paper is organized as follows. Section 2 introduces the domain of the composite task that we collected human data. Section 3 describes the main algorithm, modular inverse reinforcement learning. We report our experiment results in Section 4, and conclude in Section 5.

# 2 Multi-objective Domain

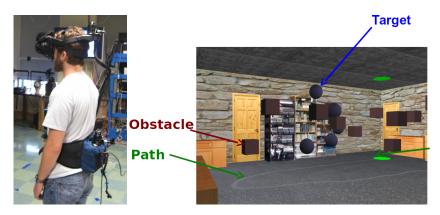


Figure 1: (Left) A human subject with head tracker, virtual reality displayer, and body tracker. (Right) The environment the human can see through the displayer. The red cubes represent obstacles. The blue balls represent targets. There is also a gray path on the ground that the human subject can follow.

Figure 1 shows the domain that we used for our experiment. The agent, which is a human subject in this case, is in a virtual reality domain. We ask the human subject to have trackers and a virtual reality displayer equipped. He can see the environment through the displayer in front of his eyes, and he can walk as if he is walking in the virtual domain. The agent would be punished if running into obstacles (red cubes), and rewarded if collecting targets (blue balls). There is a path on the ground that he can follow. Naturally, this domain has three sub-tasks, 1) following the path, 2) collecting targets, 3) avoiding obstacles. This is an experiment used in the literature to evaluate modular reinforcement learning [5] and understand human behavior [9].

We will evaluate four different tasks. **Task 1**, following the path only, and ignoring other objects. **Task 2**, following the path, while avoiding the obstacles. **Task 3**, following the path, while collecting targets when possible. **Task 4**, following the path, collecting the targets and avoiding obstacles simultaneously. We conducted experiments to ask human subjects to accomplish these tasks and recorded their trajectories. The human data are collected by the Center for Perceptual Systems at University of Texas at Austin.

If the agent observes the distance and angle to an object, he is expected to know the optimal action to avoid or pursue it. This decision is also Markov. Therefore, the question would be, if we have trained modules for these three sub-tasks, could they be integrated to match human's behavior?

# 3 Modular Inverse Reinforcement Learning

Recall that for a state, action pair, s and a, Q(s,a) evaluates the utility of taking action a from state s. The *policy* of a state is the action with the maximum Q value [7]. So how do we determine the global policy from the modules, or sub-tasks? In the literature, work has been done to integrate the decomposed value functions of the sub-tasks [2]. The sub-tasks can also propose their own policies, while the global policy is a weighted sum of those sub-task policies [8].

Here, we assume that the global Q function is a weighted sum of all  $Q_i$ , where  $Q_i$  is the Q function for i-th module.

$$Q(s,a) = \sum_{i} w_i Q_i(s_i, a)$$

where  $w_i$  is the weight of the i-th sub-MDP.  $w_i \ge 0, \sum_i w_i = 1$ .  $s_i$  denotes the decomposition of s in the i-th module.

Different weights can yield different performance. Let w be the vector of  $(w_1, w_2, w_3)$ , where  $w_1, w_2, w_3$  are weights for the sub-tasks of target collection, obstacle avoidance, and path following, respectively. An agent with w = (1, 0, 0) only collects targets, and one with w = (0, 0.5, 0.5) may avoid the obstacles and follow the path.

To obtain the weights given the samples, we need to use the inverse reinforcement learning technique. In reinforcement learning, we derive optimal policies given an MDP. In inverse reinforcement learning, however, we find out the underlying MDP by observing policies. In the literature, a common way is to use a maximum likelihood method to recover the transition function and the reward function [4]. Here, however, we only need to find out the weights. The transition function is known, and the reward function is trivially the weighted sum of that of modules. Concretely, we use the modular inverse reinforcement learning method [5] to maximize the function below.

$$\max_{w} \prod_{t} \frac{e^{\eta Q(s^{(t)}, a^{(t)})}}{\sum_{b} e^{\eta Q(s^{(t)}, b)}} \tag{1}$$

where  $s^{(t)}$  is the state at time t, and  $a^{(t)}$  is the action at time t, which are both from samples.  $Q(s,a) = \sum_i w_i Q_i(s_i,a)$ , as defined before.  $\eta$  is a hyperparameter that determines the consistency of human's behavior. The larger  $\eta$  is, the algorithm is more likely to overfit the data.

The intuition of Equation 1 is that if an action is observed from the sample, then the Q value of taking that action should be larger compared to Q values of taking other actions.

## 4 Experiments

We trained the modules first to obtain  $Q_i$  before running the inverse reinforcement learning algorithm. For each module, the agent only considers the closest target and the closest obstacle. For the path module, the path is defined as segments connected by waypoints, so the next waypoint is considered. The agent takes the distance and angle to the closest objects as the state representation.

To make our weights represent the significance of the modules, we normalize the sub-MDPs with the unit (positive or negative) reward. The reward is 1 for collecting a target, -1 for running into an obstacle, and 1 for collecting a waypoint of the path. In the implementation, we make the radius of waypoints larger than that of other objects, so that the agent will not cling too much to the path.

We make some constraints on our learning agent to make it walk like a human. We can find from the human trajectories that humans walk smoothly and do not turn sharply. Our agent is only allowed to do three actions — going straight ahead, turning left with a small step, and turning right with a small step.

We report the results in Figure 2. Same as Figure 1, the red circles are obstacles. The blue circles are targets. The gray lines are the path. The black lines are trajectories of human — each line represents one human trajectory. Using the weights derived from the algorithm, the trajectories of the agents are drawn in green color.

Although humans don't agree with each other on how to avoid obstacles or collect targets, the agent can figure out what the humans are doing, and perform a similar behavior. Figure 3 evaluates the performance by showing the number of targets hit and number of obstacles hit. The number of targets hit should be large, and the number of obstacles hit should be small, when the corresponding module is active. We can observe that humans still do better than the agent in these tasks. Nevertheless, the agent has a similar performance compared to human subjects.

In Figure 4, we show the log of values of Equation 1 for different weights. The white color represents higher probability. We can observe the centroids of white zones move for different tasks. It stays at the origin in Task 1, so none of the target module and obstacle module is active. It moves away from the origin when a module is active. From the heatmaps, we find the optimums exist for these tasks. The optimal weights are also consistent with the experiment context.

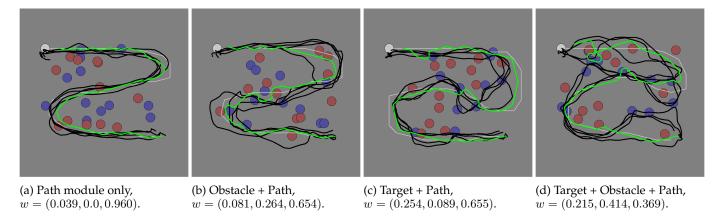


Figure 2: The trajectories of humans and the agent in the four tasks. The black lines are trajectories of human subjects, and the green lines are trajectories of the learning agent by using the optimum weights, w, derived from modular inverse reinforcement learning. Weights are shown in the target, obstacle, path order.

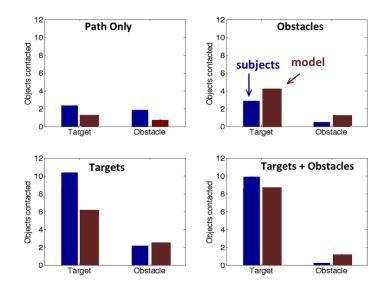


Figure 3: Number of targets hit and number of obstacles hit of the human subjects and the agent.

#### 5 Conclusion and Future Work

We interpreted human behavior using inverse module reinforcement learning in this paper. The experimental results show that modular reinforcement learning can well explain human behavior, even though the performance of the agent is inferior to human subjects'.

There are also some observations potential for the future work. First, weighted sum of Q functions is one way to combine multiple sub-MDPs. We also propose other ways including, for example, scheduling between different modules, with only one active at one time. This is also called *skill* in the literature [3]. However, we adopt the weighted sum approach because this is more reasonable for human behavior. When a human tries to collect targets while avoiding obstacles, these two modules are expected to be both active. A scheduling approach may yield frequent oscillation between these two modules.

Second, we also assume independency between modules. Correlation between modules doesn't impair our analysis in this paper. In Figure 4, we can tell that the target module and obstacle module tend to be negatively correlated from the shape of the white zones.

Lastly, weights may be dynamic and different from state to state. However, with such assumption, we need to learn a mapping from state to weights. In this case, the curse of dimensionality still exists, and inverse learning would be difficult.

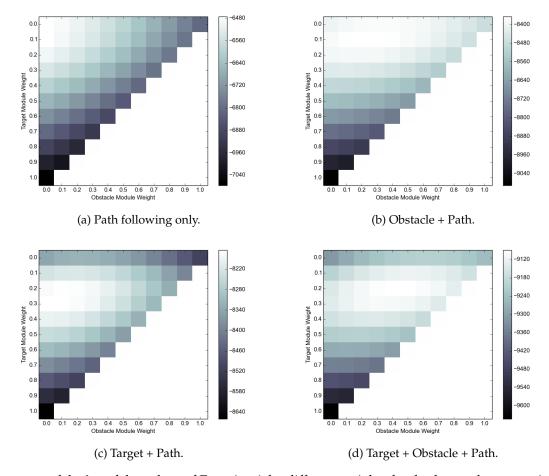


Figure 4: Heatmaps of the log of the values of Equation 1 for different weights for the four tasks, respectively. The white zones indicate higher probabilities. The weights of all three modules sum to 1, so we only show the weights on the target and the obstacle modules.

#### References

- [1] Thomas G Dietterich. Hierarchical reinforcement learning with the maxq value function decomposition. *J. Artif. Intell. Res.(JAIR)*, 13:227–303, 2000.
- [2] Daphne Koller and Ronald Parr. Computing factored value functions for policies in structured mdps. In *IJCAI*, volume 99, pages 1332–1339, 1999.
- [3] George Konidaris and Andre S Barreto. Skill discovery in continuous reinforcement learning domains using skill chaining. In *Advances in Neural Information Processing Systems*, pages 1015–1023, 2009.
- [4] Andrew Y Ng, Stuart J Russell, et al. Algorithms for inverse reinforcement learning. In *Icml*, pages 663–670, 2000.
- [5] Constantin A Rothkopf and Dana H Ballard. Modular inverse reinforcement learning for visuomotor behavior. *Biological cybernetics*, 107(4):477–490, 2013.
- [6] Nathan Sprague and Dana Ballard. Multiple-goal reinforcement learning with modular sarsa (0). In *IJCAI*, pages 1445–1447. Citeseer, 2003.
- [7] Richard S Sutton and Andrew G Barto. Reinforcement learning: An introduction, volume 1. Cambridge Univ Press, 1998.
- [8] Philip S Thomas and Andrew G Barto. Motor primitive discovery. In ICDL-EPIROB, pages 1–8, 2012.
- [9] M. H. Tong and M. M. Hayhoe. Modeling uncertainty and intrinsic reward in a virtual walking task. *Journal of Vision*, 14(10):5, August 2014.