```
from pattern_utilities import generate_n_random_patterns
    from hopfield import StochasticHopfieldNetwork
2
    import numpy as np
3
    def main():
6
        n_bits = 200
        n_patterns = 7
        noise\_parameter = 2
        T = int(2e5)
10
        n_{iterations} = 100
11
12
        patterns = generate_n_random_patterns(n_patterns=n_patterns, n_bits=n_bits)
13
14
        network = StochasticHopfieldNetwork()
15
        network.set_patterns(patterns)
16
        network.set_diagonal_weights_rule("zero")
17
        network.set_noise_parameter(noise_parameter)
18
        network.generate_weights()
19
20
        pattern1 = patterns[0, :]
21
        updated_pattern = pattern1.copy()
22
23
        m = np.zeros(n_iterations)
24
        for i in range(n_iterations):
25
            print(i)
26
            for t in range(T):
27
                updated_pattern = network.update_random_neuron(updated_pattern)
28
                m[i] += np.inner(updated_pattern, pattern1)
29
            m[i] /= n_bits
30
            m[i] /= T
31
32
        m_estimate = sum(m) / n_iterations
33
        print("{:.3f}".format(m_estimate))
34
35
36
    if __name__ == "__main__":
37
        main()
38
```

Listing 1: Main method for computing the order parameter.

```
import numpy as np
from scipy import stats
from abc import ABC, abstractmethod

class HopfieldNetwork(ABC):
```

```
def set_diagonal_weights_rule(self, diagonal_weights_rule):
7
            if diagonal_weights_rule == "zero":
8
                 self.diagonal_weights_equal_zero = True
            elif diagonal_weights_rule == "non-zero":
10
                 self.diagonal_weights_equal_zero = False
11
            else:
                raise KeyError(
13
                         diagonal_weights_rule
14
                         + " not a valid diagonal_weights_rule"
                         )
16
17
        def set_patterns(self, patterns):
18
            self.patterns = patterns
19
20
        def generate_weights(self):
21
            _, n_bits = self.patterns.shape
22
            self.weights = np.zeros((n_bits, n_bits))
23
            for pattern in self.patterns:
24
                 self.weights += np.outer(pattern, pattern)
25
            self.weights /= n_bits
26
27
            if self.diagonal_weights_equal_zero:
28
                np.fill_diagonal(self.weights, 0)
29
30
        def asynchronous_update(self, pattern, n_updates):
31
            updated_pattern = pattern.copy()
32
            for i in range(n_updates):
33
                updated_pattern = self.update_random_neuron(updated_pattern)
34
            return updated_pattern
35
36
        def update_random_neuron(self, pattern):
37
            n_bits = pattern.shape
38
            neuron_index = np.random.randint(n_bits)
39
            return self.update_neuron(pattern, neuron_index)
40
        def update_neuron(self, pattern, neuron_index):
42
            weights_i = self.weights[neuron_index, :]
43
            local_field = np.inner(weights_i, pattern)
            updated_bit = self.get_state_of_local_field(local_field)
45
            updated_pattern = pattern.copy()
46
            updated_pattern[neuron_index] = updated_bit
            return updated_pattern
48
49
        @abstractmethod
50
        def get_state_of_local_field(self, local_field):
51
            pass
52
53
    class DeterministicHopfieldNetwork(HopfieldNetwork):
55
```

```
def get_state_of_local_field(self, local_field):
56
            return sign_zero_returns_one(local_field)
57
59
    class StochasticHopfieldNetwork(HopfieldNetwork):
60
        def get_state_of_local_field(self, local_field):
            p = 1/(1 + np.exp(-2*self.noise_parameter*local_field))
62
            rand = stats.bernoulli.rvs(p)
63
            return 1 if rand else -1
65
        def set_noise_parameter(self, noise_parameter):
66
            self.noise_parameter = noise_parameter
67
68
69
    def sign_zero_returns_one(value):
70
        return 1 if value >= 0 else -1
71
```

Listing 2: Classes for creating Hopfield Networks.

```
import numpy as np
    from scipy import stats
2
    import matplotlib.pyplot as plt
    def generate_n_random_patterns(n_patterns, n_bits):
6
        random_0s_and_1s = stats.bernoulli.rvs(0.5, size=(n_patterns, n_bits))
        random_minus_1s_and_1s = 2*random_0s_and_1s - 1
        return random_minus_1s_and_1s
10
11
    def get_index_of_equal_pattern(pattern_to_match, patterns):
12
        for index, pattern in enumerate(patterns):
13
            n_different_bits = get_n_different_bits(pattern_to_match, pattern)
14
            if n_different_bits == 0:
15
                return index
16
        return -1
17
18
19
    def get_n_different_bits(pattern1, pattern2):
20
        return sum(pattern1 != pattern2)
21
22
23
    def vector_to_typewriter(vector, n_columns):
24
        return np.reshape(vector, (-1, n_columns))
25
26
27
    def print_typewriter_pattern(pattern, n_columns):
28
        print_pattern(vector_to_typewriter(pattern, n_columns))
29
30
```

```
31
    def print_pattern(pattern):
32
        np.set_printoptions(formatter={"float_kind": lambda x: "%.4f" % x})
33
        print(repr(pattern), sep=", ")
34
35
36
    def plot_pattern(pattern):
37
        plt.imshow(pattern, cmap="Greys")
38
        plt.tick_params(
39
                 axis="both",
40
                 which="both",
41
                 bottom=False,
42
                 top=False,
43
                 left=False,
44
                 labelbottom=False,
45
                 labelleft=False)
```

Listing 3: Help module for handling patterns.