

Coordinates

$$q_1 = \left(\mathbf{x}_{\mathrm{G}}^1\right) \tag{1}$$

Configuration

$$\Pi_0 = \left(\begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}, \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \right)$$
(2)

$$\Pi_{1} = \left(\begin{bmatrix} x_{G}^{1} \\ 0 \\ 0 \end{bmatrix}, \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \right)$$
(3)

Energy

$$L = \frac{1}{2}m_1 \left(\frac{d}{dt} \,\mathrm{x}_{\mathrm{G}}^1\right)^2 \tag{4}$$

Kinetic Energy Metric

$$G = [m_1] \tag{5}$$

1

Forces and Torques

$$F_1 = \begin{pmatrix} \begin{bmatrix} F_x^1 \\ 0 \\ 0 \end{bmatrix}, \begin{bmatrix} \mathbf{x}_{\mathbf{G}}^1 \\ 0 \\ 0 \end{bmatrix} \end{pmatrix} \tag{6}$$

Equations of Motion

$$\begin{bmatrix} I & 0 \\ 0 & G \end{bmatrix} \begin{bmatrix} \frac{d}{dt} \mathbf{x}_{G}^{1} \\ \frac{d^{2}}{dt^{2}} \mathbf{x}_{G}^{1} \end{bmatrix} = \begin{bmatrix} \frac{d}{dt} \mathbf{x}_{G}^{1} \\ F_{x}^{1} \end{bmatrix}$$
 (7)