

例 设某控制系统的开环传递函数为

$$G(s)H(s) = \frac{10}{(s+1)(s+2)(s+3)}$$

试用奈氏稳定判据判别闭环系统的稳定性。

$$1. G(j\omega) = \frac{10}{(j\omega+1)(j\omega+2)(j\omega+3)} = -\frac{60(\omega^2-1)}{(\omega^2+1)(\omega^2+4)(\omega^2+9)} - j\frac{10\omega(11-\omega^2)}{(\omega^2+1)(\omega^2+4)(\omega^2+9)}$$

$$\omega_x = \sqrt{11}$$

$$\text{Re}[G(j\omega_x)] = -0.17$$

$$P=0, n=0$$

$$\therefore Z=0, \text{稳定}$$

例 某单位反馈系统，开环传递函数为， $G_k(s) = \frac{2}{s-1}$

试用奈氏判据判别闭环系统稳定性。

$$2. G(j\omega) = \frac{2}{j\omega-1} = -\frac{2}{\omega^2+1} - j\frac{2\omega}{\omega^2+1} = \frac{2}{\sqrt{\omega^2+1}} e^{j\arctan \omega}$$

$$G(j\omega) = -2\angle 0^\circ \quad G(j\infty) = 0\angle -90^\circ$$

$$w \rightarrow +\infty$$

$$\arctan \omega \rightarrow +90^\circ ???$$

$$P=1$$

$$n=0.5$$

$$Z=P-2n=0$$

$$\therefore \text{稳定}$$

例 设某控制系统的开环传递函数为

$$G(s)H(s) = \frac{500}{(s+0.5)(s+1)(s+2)}$$

试用奈氏稳定判据判别闭环系统稳定性。

$$3. G(j\omega) = \frac{500}{(j\omega+0.5)(j\omega+1)(j\omega+2)} = -\frac{500[3.5\omega^2-1+j(3.5\omega-\omega^3)]}{6\omega^2+0.25(\omega^2+1)(\omega^2+4)}$$

$$G(j\omega) = 500\angle 0^\circ \quad G(j\infty) = 0\angle -270^\circ$$

$$\omega_x = 1.87 \text{ rad/s} \quad \text{Re}[G(j\omega_x)] = -44.44$$

$$P=0$$

$$n=-1$$

$$Z=2$$

$$\therefore \text{不稳定}$$

$$4. G(jw) = \frac{k(jw-1)}{jw(jw+1)} = \frac{2w^2 + jw(1-w^2)}{w^2(w^2+1)} \cdot k$$

$$G(j0) = \infty \angle -90^\circ \quad G(j\infty) = 0 \angle -90^\circ$$

