



**ONE DAY FACULTY ORIENTATION PROGRAMME**  
on **Data Structures and Algorithms Lab (217532)** February 16,  
in Association with BoS, Computer Engineering, SPPU, Pune

Organized By Department of Artificial Intelligence and Data Science  
Dr. D.Y. Patil Institute of Engineering, Management and Research,  
Akurdi, Pune

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<b>Teaching Scheme</b> <b>Practical: 04 Hours/Week</b>	<b>Credit Scheme</b> <b>02</b>	<b>Examination Scheme and Marks</b> <b>Term Work: 25 Marks</b> <b>Practical: 25 Marks</b>
<b>Prerequisite Courses:</b> 110005: Programming and Problem Solving, 217522: Data Structures Laboratory		
<b>Companion Course :</b> 210252: Data Structures and Algorithms		
<b>Course Objectives:</b> <ul style="list-style-type: none"> <li>To <b>understand</b> practical implementation and usage of non linear data structures for solving problems of different domain.</li> <li>To strengthen the ability to identify and <b>apply</b> the suitable data structure for the given real world problems.</li> <li>To <b>analyze</b> advanced data structures including hash table, dictionary, trees, graphs, sorting algorithms and file organization.</li> </ul>		
<b>Course Outcomes:</b> On completion of the course, learner will be able to– <ul style="list-style-type: none"> <li><b>CO1: Understand</b> the ADT/libraries, hash tables and dictionary to design algorithms for a specific problem.</li> <li><b>CO2:</b> Choose most appropriate data structures and <b>apply</b> algorithms for graphical solutions of the problems.</li> <li><b>CO3: Apply</b> and <b>analyze</b> non linear data structures to solve real world complex problems.</li> <li><b>CO4: Apply</b> and <b>analyze</b> algorithm design techniques for indexing, sorting, multi-way searching, file organization and compression.</li> <li><b>CO5: Analyze</b> the efficiency of most appropriate data structure for creating efficient solutions for engineering design situations.</li> </ul>		

@The CO-PO Mapping Matrix

PO	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO11	PO12
CO1	1	2	2	-	-	-	-	-	-	-	-	-
CO2	-	2	2	-	-	-	-	-	-	-	-	-
CO3	-	2	2	1	-	-	-	-	-	-	-	-
CO4	1	2	1	1	-	-	-	-	-	-	-	-
CO5	1	1	2	2	-	-	-	-	-	-	-	-



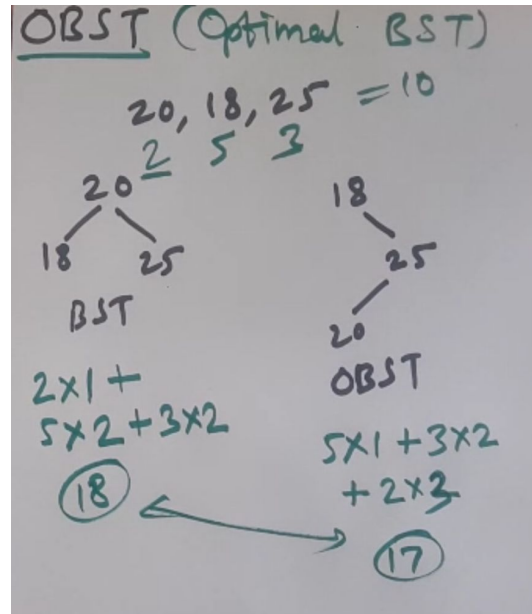
# Flipped Classroom



- A flipped classroom is an instructional strategy and a type of blended learning, which aims to increase student engagement and learning by having pupils complete readings at home and work on live problem-solving during class time.
- Prerequisite: Content Delivery Platform like YouTube, etc..

# D-18

Given sequence  $k = k_1 < k_2 < \dots < k_n$  of  $n$  sorted keys, with a search probability  $p_i$  for each key  $k_i$ . Build the Binary search tree that has the least search cost given the access probability for each key?





	1	2	3	4
keys	10	20	30	40
freq.	4	2	6	3

$n \rightarrow [n+1][n+1]$

$i \backslash j$	0	1	2	3	4
0	0				
1		0			
2			0		
3				0	
4					0

Step 1)  $l = 0 = j - i$

2)  $l = 1 = j - i$   
 $1 - 0 \quad (0, 1)$   
 $i \quad j$

$C_{ij} = C[0, 1]$   
 $= C_{01}$   
 exclude include

	1	2	3	4
keys	10	20	30	40
freq.	4	2	6	3

$n \rightarrow [n+1][n+1]$

$j \backslash i$	0	1	2	3	4
0	0	4			
1		0	2		
2			0		
3				0	
4					0

Cost max. with mfb

Step 1)  $l = 0 = j - i$

2)  $l = 1 = j - i$   
 $1 - 0 \quad (0, 1)$   
 $i \quad j$

$C_{ij} = C[0, 1]$   
 $= C_{0, 1}$   
 exclude include

(10)  
 $4 \times 1 = 4$

$j - i = 2, 1 = 1$

$C_{1, 2}$   
 ex. include

(20)  $2 \times 1 = 2$



# Filling the cost matrix repetitively without DP

Handwritten notes illustrating the calculation of the cost matrix for merging keys.

**Input Data:**

	1	2	3	4
key1	10	20	30	40
freq.	4	2	6	3

$n \rightarrow [n+1][n+1]$

**Cost Matrix (n x n):**

i \ j	0	1	2	3	4
0	0	4	8		
1		0	2		
2			0	6	
3				0	3
4					0

Cost mtr. with mtr

**Step 3)  $l = 2 = j - i$**

$Cost = \min\{r^1, r^2\}$

ex. in.  $\begin{pmatrix} 1 & 2 \\ 1 & 2 \end{pmatrix}$

$4 \times 1 + 2 \times 2 = 8$

$2 \times 1 + 4 \times 2 = 10$

# Filling the cost matrix with DP

Step 3)  $l = 2 = j - i$

$C_{02} = \min \{ r_1^1, r_2^2 \}$

$\uparrow \quad \uparrow$   
ex. in.  $\frac{1}{2}$   $\frac{10}{20}$   $4 \times 1 + 2 \times 2 = 8$

$2 \times 1 + 4 \times 2 = 10$

Weight =  $W_{02} = \text{sum of freq } [0, 2]$   
 $= 4 + 2 = 6$

$n \rightarrow [n+1][n+1]$

$j \backslash i$	0	1	2	3	4
0	0	4	8		
1		0	2		
2			0	6	
3				0	3
4					0

Cost max with mbr

# Cost of $C_{02}$ when key 10 is root

keys | 10 | 20 | 30 | 40  
freq. | 4 | 2 | 6 | 3

$n \rightarrow [n+1][n+1]$

i \ j	0	1	2	3	4
0	0	4	8		
1		0	2		
2			0	6	
3				0	3
4					0

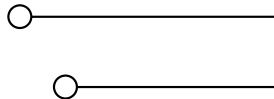

Cost max. with mfb

$C_{02} = \min\{r^1, r^2\}$   
or in  $\begin{matrix} 1 & 2 \\ 1 & 2 \end{matrix}$

$\begin{matrix} 10 & 20 \\ 4 \times 1 + 2 \times 2 = 8 \\ 2 \times 1 + 4 \times 2 = 10 \end{matrix}$

Weight =  $(w_{02}) = \text{sum of freq } [0, 2]$   
 $= 4 + 2 = 6$

$C_{02} = \underbrace{C_{00}}_{\text{left}} + \underbrace{C_{12}}_{\text{right}}$   
 $= 0 + 2$



We got  $C_{02}$  as 2, which is wrong

- That means something needs to be added
- There comes  $W_{02}$

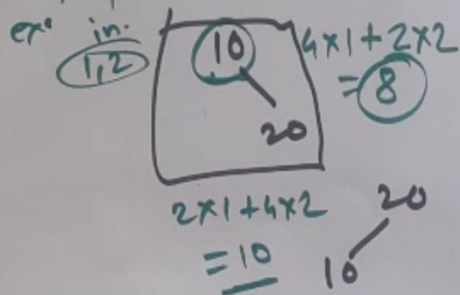
keys	10	20	30	40
freq.	4	2	6	3

$n \rightarrow [n+1][n+1]$

$i \backslash j$	0	1	2	3	4
0	0	4	8		
1		0	2		
2			0	6	
3				0	3
4					0

Cost msl. with mlt

$$C_{02} = \min\{r_1^1, r_2^2\} = 8$$



Weight =  $W_{02}$  = sum of freq  $[0,2]$

$$= 4 + 2 = 6$$

$$C_{02} = \underbrace{C_{00}}_{\text{left}} + \underbrace{C_{12}}_{\text{right}} + W_{02}$$

$$= 0 + 2 + 6 = 8$$



# Making Generic Formula

Step 3)  $l = 2 = j - i$

$C_{02} = \min \{ r_1^1, r_2^2 \} = 8$

Diagram illustrating the calculation of  $C_{02}$  using a square grid:

The grid is divided into four quadrants by a diagonal line from the top-left to the bottom-right. The top-left quadrant contains the value 10. The top-right quadrant contains the value 20. The bottom-left quadrant contains the value 20. The bottom-right quadrant contains the value 10. The value 8 is circled in the top-right quadrant.

Below the grid, the calculation is shown:

$$2 \times 1 + 4 \times 2 = 10$$

The value 10 is circled and marked with a checkmark.

Right =  $W_{02}$  = sum of freq  $[0, 2]$

$$= 4 + 2 = 6$$

The final calculation is shown:

$$C_{02} = \underbrace{C_{00}}_{\text{left}} + \underbrace{C_{12}}_{\text{right}} + W_{02}$$

The final result is 8.

Diagram illustrating the generic formula for  $C_{02}$ :

$$C_{02} = \min \{ r_1^1, r_2^2 \} + W_{02}$$

The diagram shows the calculation of  $C_{02}$  as the minimum of  $r_1^1$  and  $r_2^2$  plus  $W_{02}$ . The values  $C_{00} + C_{12}$  and  $C_{01} + C_{22}$  are shown as inputs to the minimum function. The value  $W_{02}$  is shown as the weight.



keys	10	20	30	40
freq.	4	2	6	3

$n \rightarrow [n+1][n+1]$

$i \backslash j$	0	1	2	3	4
0	0	4 <sup>1</sup>	8 <sup>1</sup>		
1		0	2 <sup>2</sup>	10 <sup>3</sup>	
2			0	6 <sup>3</sup>	
3				0	3 <sup>4</sup>
4					0

Cost max. with mkt

$$C_{02} = \min \{ r^1, r^2 \} + w_{02}$$

Diagram showing the calculation of  $C_{02}$  with arrows pointing to  $C_{00} + C_{12}$  and  $C_{01} + C_{22}$ . The value  $C_{02}$  is circled.

$$C_{13} = \min \{ r^2, r^3 \} + w_{13}$$

Diagram showing the calculation of  $C_{13}$  with arrows pointing to  $C_{11} + C_{23}$  and  $C_{12} + C_{33}$ . The value  $C_{13}$  is circled.

$$C_{11} + C_{23} = 0 + 6 = 6$$

$$C_{12} + C_{33} = 2 + 0 = 2$$

The value 2 is circled and underlined.

# Why DP is useful?

Handwritten notes illustrating the use of Dynamic Programming (DP) for finding the minimum cost of a Binary Search Tree (BST) given keys and their frequencies.

**Keys and Frequencies:**

	1	2	3	4
keys	10	20	30	40
freq.	4	2	6	3

**DP Table (Cost matrix):**

$n \rightarrow [n+1][n+1]$

i \ j	0	1	2	3	4
0	0	4	8		
1		0	2	10	
2			0	6	12
3				0	3
4					0

*Cost max. with min*

**Calculation for  $C_{03}$ :**

$C_{03} =$

For 'n' keys BST??

$$\frac{2n(n)}{n+1}$$
$$\frac{8(3)}{4} = \frac{6 \times 5 \times 4}{2 \times 2} = 5$$



keys	10	20	30	40
freq.	4	2	6	3

$n \rightarrow [n+1][n+1]$

$i \backslash j$	0	1	2	3	4
0	0	4 <sup>1</sup>	8 <sup>1</sup>	20 <sup>3</sup>	26 <sup>3</sup>
1		0	2 <sup>2</sup>	10 <sup>3</sup>	16 <sup>3</sup>
2			0	8 <sup>3</sup>	12 <sup>3</sup>
3				0	3 <sup>4</sup>
4					0

Ce max. with mft

$$C_{03} = \min\{r^1, r^2, r^3\} + \frac{w_{03}}{12}$$

$$C_{00} + C_{13} \quad C_{01} + C_{23}$$

$$\frac{0+10}{7} \quad \frac{4+6}{7} \quad C_{02} + C_{33} = 20$$

$$\frac{0+10}{7} \quad \frac{4+6}{7} \quad \frac{8+0}{7}$$

$$C_{14} = \min\{r^2, r^3, r^4\} + \frac{w_{14}}{11}$$

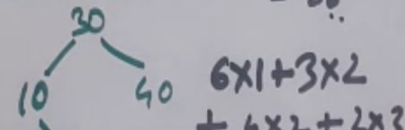
$$= C_{11} + C_{24} \quad C_{12} + C_{34} \quad C_{13} + C_{44}$$

$$0+12 \quad \frac{2+3}{4} \quad 10+0$$

$$45+11=16$$

$$C_{04} = \min\{r^1, r^2, r^3, r^4\} + w_{04}$$

$$= C_{02} + C_{34} + w_{04} = 8+3+15 = 26$$



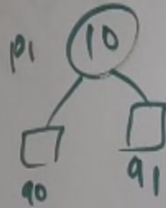
## Example

Q. Let  $n=4$  and  
 $(a_1, a_2, a_3, a_4) = (10, 15, 20, 25)$ .  
Let  $(p_1, p_2, p_3, p_4) = (3, 3, 1, 1)$  &  
 $(q_0, q_1, q_2, q_3, q_4) = (2, 3, 1, 1, 1)$ .  
The  $p$ 's &  $q$ 's have been  
multiplied by 16 for convenience.  
Find OBST.

$$(a_1, a_2, a_3, a_4) = (10, 15, 20, 25).$$

$$\text{let } (p_1, p_2, p_3, p_4) = (3, 3, 1, 1) \text{ \& } (q_1, q_2, q_3, q_4) = (2, 3, 1, 1, 1).$$

The  $p$ 's &  $q$ 's have been multiplied by 16 for convenience, and OBST.



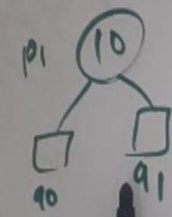
$w_{00} = q_0 = 2$ $c_{00} = 0$ $r_{00} = 0$	$w_{11} = q_1 = 3$ $c_{11} = 0$ $r_{11} = 0$	$w_{22} = q_2 = 1$ $c_{22} = 0$ $r_{22} = 0$	$w_{33} = 1$ $c_{33} = 0$ $r_{33} = 0$	$w_{44} = 1$ $c_{44} = 0$ $r_{44} = 0$
$w_{01} = p_1 + q_0 = 8$ $c_{01} =$ $r_{01} =$	$w_{12} =$ $c_{12} =$ $r_{12} =$	$w_{23} = 3$ $c_{23} = 3$ $r_{23} = 3$	$w_{34} = 3$ $c_{34} = 3$ $r_{34} = 4$	
2 $w_{02} =$ $c_{02} =$ $r_{02} =$	$w_{13} = 9$ $c_{13} = 12$ $r_{13} = 2$	$w_{24} = 5$ $c_{24} = 8$ $r_{24} = 3$		
3 $w_{03} = 14$ $c_{03} = 25$ $r_{03} = 2$	$w_{14} = 11$ $c_{14} = 19$ $r_{14} = 2$			
4 $w_{04} = 16$ $c_{04} = 32$ $r_{04} = 2$				

$(a_1, a_2, a_3, a_4) = (10, 15, 20, 25)$

let  $(p_1, p_2, p_3, p_4) = (3, 3, 1, 1)$

$(q_1, q_2, q_3, q_4) = (2, 3, 1, 1)$

The  $p$ 's &  $q$ 's have been multiplied by 16 for convenience and OBST.

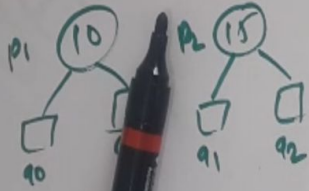


1	$w_{00} = q_0 = 2$ $c_{00} = 0$ $r_{00} = 0$	$w_{11} = q_1 = 3$ $c_{11} = 0$ $r_{11} = 0$	$w_{22} = q_2 = 1$ $c_{22} = 0$ $r_{22} = 0$	$w_{33} = 1$ $c_{33} = 0$ $r_{33} = 0$	$w_{44} = 1$ $c_{44} = 0$ $r_{44} = 0$
2	$w_{01} = p_1 + q_0 = 8$ $c_{01} = 8$ $r_{01} = 1$	$w_{12} =$ $c_{12} =$ $r_{12} =$	$w_{23} = 3$ $c_{23} = 3$ $r_{23} = 3$	$w_{34} = 3$ $c_{34} = 3$ $r_{34} = 4$	
3	$w_{02} =$ $c_{02} =$ $r_{02} =$	$w_{13} = 9$ $c_{13} = 12$ $r_{13} = 2$	$w_{24} = 5$ $c_{24} = 8$ $r_{24} = 3$		
4	$w_{03} = 14$ $c_{03} = 25$ $r_{03} = 2$	$w_{14} = 11$ $c_{14} = 19$ $r_{14} = 2$			
	$w_{04} = 16$ $c_{04} = 32$ $r_{04} = 2$				

$$c_{01} = \underline{c_{00}} + \underline{c_{11}} + \underline{w_{01}} = 8$$

# Using DP for $W_{ij}$ too

$(p_1, p_2, p_3, p_4) = (3, 3, 1, 1)$  &  
 $(q_1, q_2, q_3, q_4) = (2, 3, 1, 1)$ .  
 &  $p$ 's &  $q$ 's have been  
 multiplied by 16 for convenience,  
 and OBST.



$W_{00} = q_0 = 2$ $C_{00} = 0$ $r_{00} = 0$	$W_{11} = q_1 = 3$ $C_{11} = 0$ $r_{11} = 0$	$W_{22} = q_2 = 1$ $C_{22} = 0$ $r_{22} = 0$	$W_{33} = 1$ $C_{33} = 0$ $r_{33} = 0$	$W_{44} = 1$ $C_{44} = 0$ $r_{44} = 0$
$W_{01} = p_1 + q_0 + 1 = 8$ $C_{01} = 8$ $r_{01} = 1$	$W_{12} = 3 + 2 + 1 = 7$ $C_{12} = 7$ $r_{12} = 2$	$W_{23} = 3$ $C_{23} = 3$ $r_{23} = 3$	$W_{34} = 3$ $C_{34} = 3$ $r_{34} = 4$	
$W_{02} = 12$ $C_{02} =$ $r_{02} =$	$W_{13} = 9$ $C_{13} = 12$ $r_{13} = 2$	$W_{24} = 5$ $C_{24} = 8$ $r_{24} = 3$		
$W_{03} = 14$ $C_{03} = 25$ $r_{03} = 2$	$W_{14} = 11$ $C_{14} = 19$ $r_{14} = 2$			
$W_{04} = 16$ $C_{04} = 32$ $r_{04} = 2$				

$C_{01} = C_{00} + C_{11} + W_{01} = 8$   
 $C_{12} = C_{11} + C_{22} + W_{12} = 7$   
 $W_{ij} = W_{ij-1} + q_j + p_i$   
 $W_{02} = W_{01} + q_2 + p_0 = 8 + 1 + 3 = 12$



# Observations

- 2nd key is considered as root though 1st key is also having same success frequency. Because, failure frequencies attached with 1st key are 2,3 while failure frequencies attached with 2nd key are 3,1. So here also algorithm prefers optimization.
- Dynamic Programming for NP-class Problems.

# Time complexity

- $O(n^3)$  where  $n$  = keys

```
for (m = 2; m <= n; m++) /* calculate the weight and cost matrices */
{
    for (i = 0; i <= n - m; i++) {
        j = i + m;
        w[i][j] = w[i][j - 1] + p[j] + q[j];
        k = knuthmin(i, j); /* find minimum value in the range r[i-1][j] to
        c[i][j] = w[i][j] + c[i][k - 1] + c[k][j];
        cout << "c[" << i << "][" << j << " ]:" << c[i][j] << endl;
        r[i][j] = k;
    }
}
```

# Knuth reduced TC

- $O(n^2)$

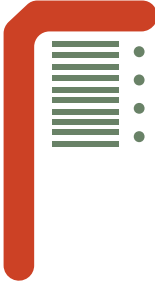
```
int obst::knuthmin(int i, int j) {  
    int min = 999, k, z;  
    for (k = r[i][j - 1]; k <= r[i + 1][j]; k++) { //k=i+1 to k<=j ==>O(n cube)  
        if (min > c[i][k - 1] + c[k][j]) {  
            min = c[i][k - 1] + c[k][j];  
            z = k;  
        }  
    }  
    return (z);  
}
```



# Benefits of DP

- DP vs Recursion

```
int factorial(unsigned int n) {  
    if (n == 0)  
        return 1;  
    return n * factorial(n - 1);  
}  
  
int fact(int n) {  
    if (n >= 0) {  
        result[0] = 1;  
        for (int i = 1; i <= n; ++i) {  
            result[i] = i * result[i - 1];  
        }  
        return result[n];  
    }  
}
```



## D-19

A Dictionary stores keywords and its meanings. Provide facility for adding new keywords, deleting keywords, updating values of any entry. Provide facility to display whole data sorted in ascending/ Descending order. Also find how many maximum comparisons may require for finding any keyword. Use Height balance tree and find the complexity for finding a keyword





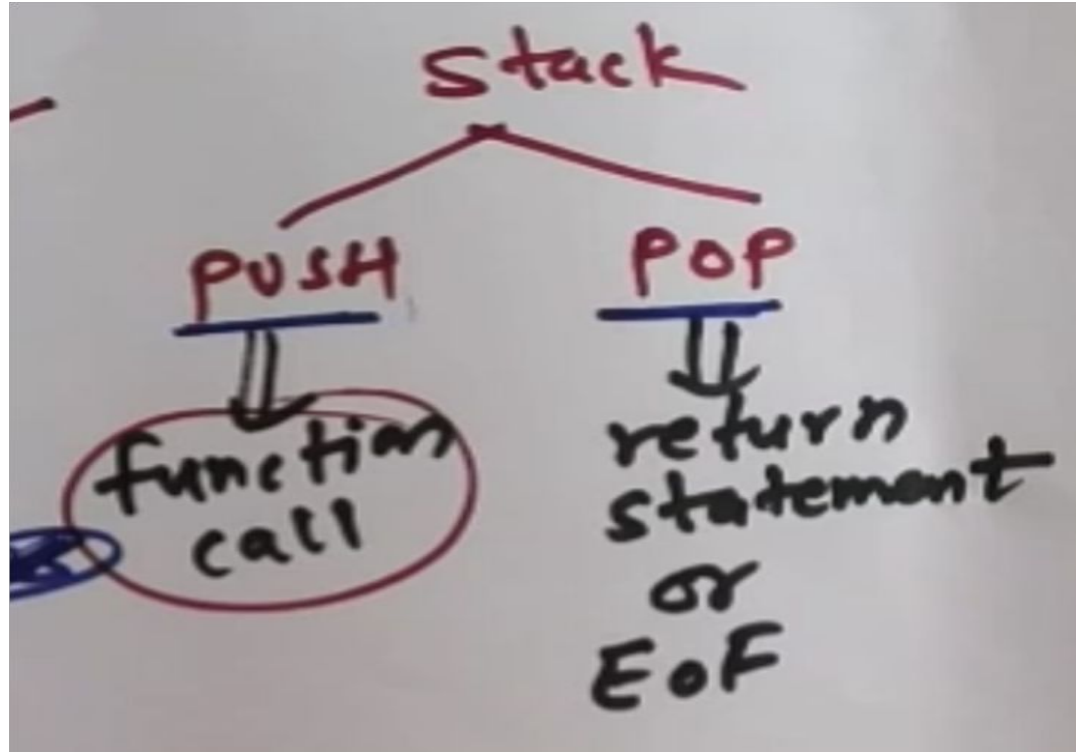
# AVL Tree with Recursion

Challenge – How to teach?

Teach AVL tree 1st with all operations  
RR, LL, RL, LR



# Teach basic of recursions

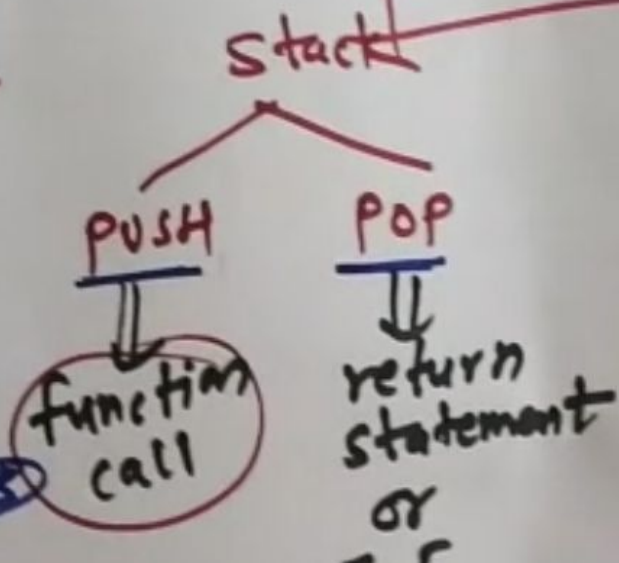


```

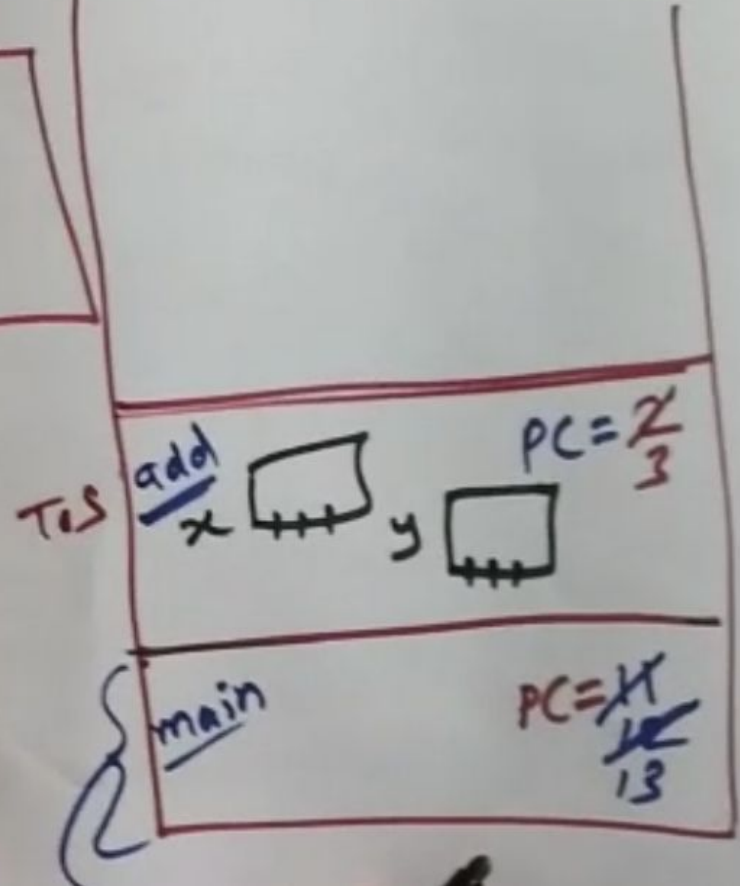
10 int main() {
11     printf("Hello world\n");
12     add();
13     printf("Exited");
14     return 0;
15 }

```

syntax ✓  
object



PC = is next line to be executed



④

```
if (lheight > rheight)
    return lheight;
else
    return rheight;
```

}

```
struct node *avldictionary::insertkeyword(struct node *r,
char ik[15],
```

```
char im[15]) {
```

```
if (r == NULL) {
```

```
    r = new struct node;
```

```
    strcpy(r->keyword, ik); //r's keyword and meaning
```

```
    strcpy(r->meaning, im); //updated with values given
```

```
//by user
```

```
    r->left = r->right = NULL; //r's both links are
```

```
//set to NULL
```

```
    } else if (strcmp(ik, r->keyword) > 0) {
```

```
        r->right = insertkeyword(r->right, ik, im);
```

```
        if (balanceFactor(r) == -2) //BF is -2 then
```

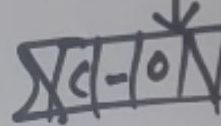
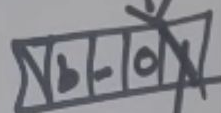
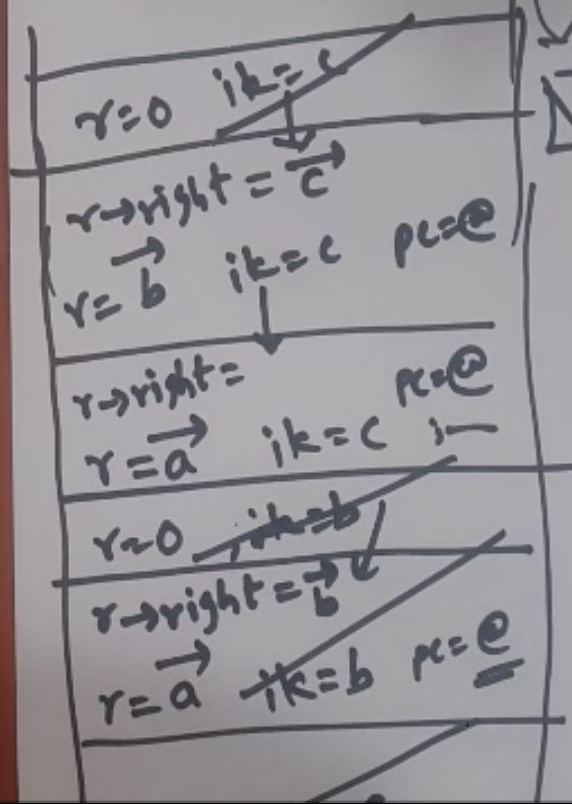
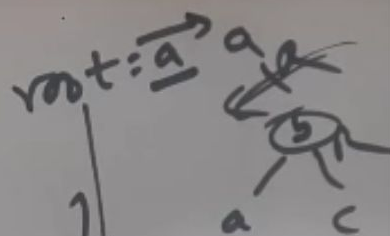
```
//insertion in RightSubTree
```

```
{
```

```
    if (strcmp(r->right->keyword) > 0) {
```

⑥

a, b, c

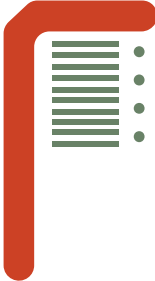




# Time & Space complexity of Recursive functions

<https://stackoverflow.com/questions/13467674/determining-complexity-for-recursive-functions-big-o-notation>





## F-23

Department maintains a student information. The file contains roll number, name, division and address. Allow user to add, delete information of student. Display information of particular employee. If record of student does not exist an appropriate message is displayed. If it is, then the system displays the student details. Use sequential file to main the data.







ofstream, ifstream, seekp, seekg

Useful for FIFO operations and cheaper device storages

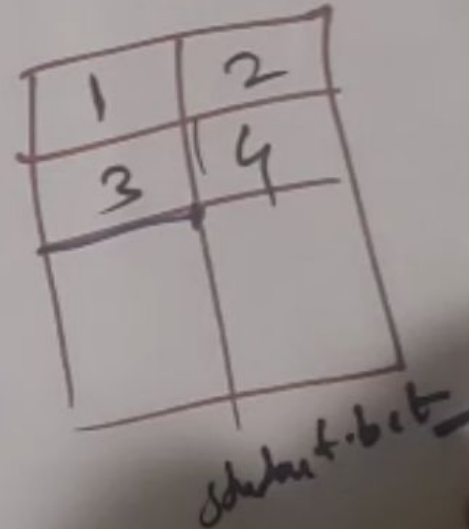
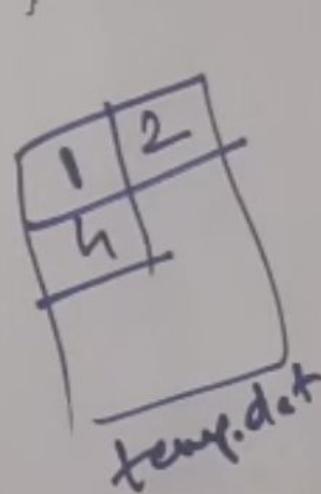




# Deletion is costly operation

```
}  
  
void delete_record(int n) {  
    Student obj;  
    ifstream inFile;  
    inFile.open("student.dat", ios::binary);  
    ofstream outFile;  
    outFile.open("temp.dat", ios::out |  
ios::binary);  
    while (inFile.read((char*) &obj,  
sizeof(obj))) {  
        if (obj.retAdmno() != n) {  
            outFile.write((char*) &obj,  
sizeof(obj));  
        }  
    }  
  
    inFile.close();  
    outFile.close();  
    remove("student.dat");  
}
```

```
case 6:  
    return 0;  
}  
} while (ch != 6);  
}
```





THANK YOU!!

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