Offset Curves along a parametric curve

- using Matplotlib, NumPy and scikit-vectors

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https://github.com/t-o-k/scikit-vectors (https://github.com/t-o-k/scikit-vectors)

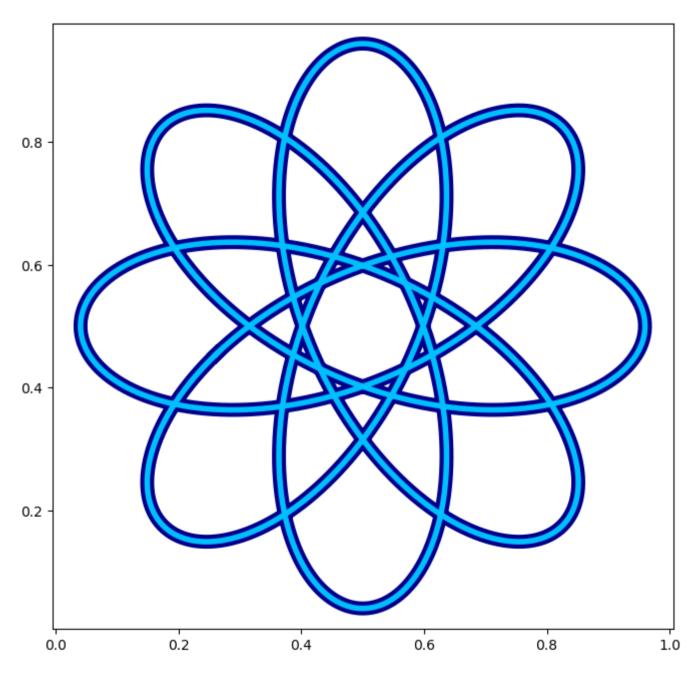
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```
In [1]:
            url = 'https://github.com/t-o-k/scikit-vectors examples/'
           # This example has been tested with NumPy v1.13.3, Matplotlib v2.1.1 and Jupyter v4.4.0.
In [2]:
In [3]:
            # Uncomment one of these to get a Matplotlib backend with interactive plots
            # %matplotlib auto
            # %matplotlib notebook
In [4]:
            import matplotlib.pyplot as plt
         2 from matplotlib.patches import Polygon
           from matplotlib.collections import PatchCollection
            import numpy as np
            from skvectors import create class Cartesian 2D Vector
In [5]:
            # Size and resolution for Matplotlib figures
            figure size = (8, 8)
           figure dpi = 100
```

```
In [6]:
            # The functions for a parametric "flower" curve
         3
            def f x(t):
                return 0.5 + 0.46 * (3 * np.cos(5 * t - np.pi / 6) + 2 * np.sin(3 * t)) / 5
         6
         7
         8
            def f_y(t):
         10
                return 0.5 + 0.46 * (3 * np.sin(5 * t - np.pi / 6) + 2 * np.cos(3 * t)) / 5
In [7]:
            # Numerical approximation of the first derivative of a univariate function
         2
            def first derivative(fn, h=1e-4):
         4
          5
                h2 = 2 * h
         6
         7
         8
                def d1 fn(t):
         9
         10
                    return (fn(t + h) - fn(t - h)) / h2
         11
         12
         13
                return d1_fn
In [8]:
            # Create derivative functions for the curve
            d1 f x = first derivative(f x)
            d1 f y = first derivative(f y)
In [9]:
            no of points along curve = 800
```

```
# Necessary NumPy functions
In [10]:
           3
              np functions = \
           5
                      'not': np.logical not,
           6
                      'and': np.logical and,
           7
                      'or': np.logical or,
           8
                      'all': np.all,
           9
                      'any': np.any,
          10
                      'min': np.minimum,
          11
                      'max': np.maximum,
          12
                      'abs': np.absolute,
          13
                      'trunc': np.trunc,
          14
                      'ceil': np.ceil,
          15
                      'copysign': np.copysign,
                      'log10': np.log10,
          16
          17
                      'cos': np.cos,
          18
                      'sin': np.sin,
          19
                      'atan2': np.arctan2,
          20
                      'pi': np.pi
          21
                  }
```

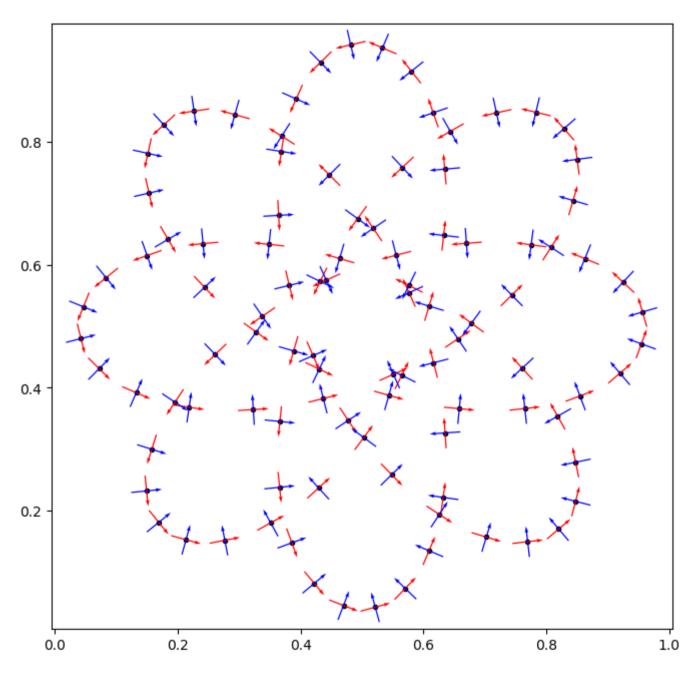
```
In [11]:
             # Create a vector class that can hold all the points along the curve
           2
           3
             NP2 = \
                 create_class_Cartesian_2D_Vector(
           4
           5
                     name = 'NP2',
           6
                     component names = 'xy',
           7
                     brackets = '<>',
           8
                     sep = ', ',
          9
                      cnull = np.zeros(no of points along curve),
                     cunit = np.ones(no of points along curve),
          10
                     functions = np functions
          11
         12
```



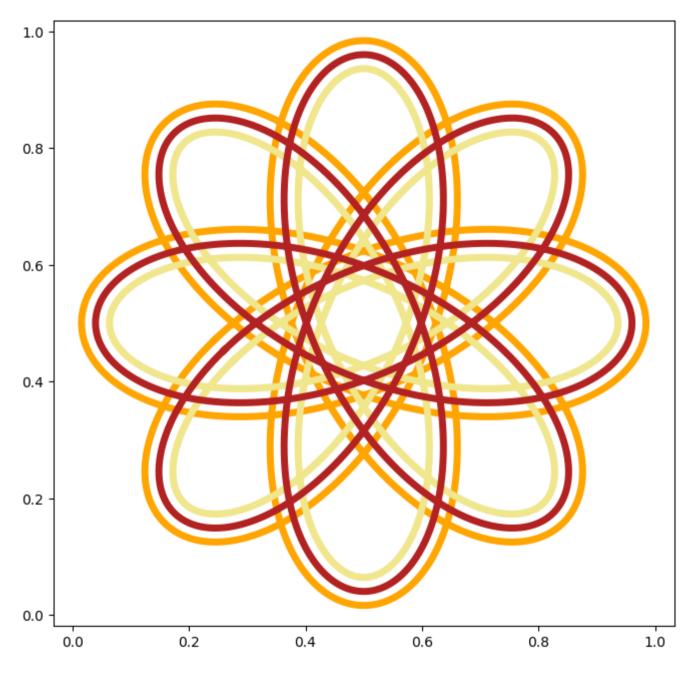
https://github.com/t-o-k/scikit-vectors_examples/

```
In [14]:
             # Calculate vectors from the first derivatives at the points along the curve
          3
             v_d1 = 
                 NP2(
          5
                     x = d1_f_x(angles_along_curve),
                     y = d1 f y(angles along curve)
          6
          7
In [15]:
          1 # Calculate tangent vectors at the points along the curve
          3 v_t = v_d1.normalize()
In [16]:
          1 # Calculate normal vectors at the points along the curve
          2
          3 | v_n = v_t.perp()
```

```
1 # Show some of the tangent vectors and the normal vectors along the curve
In [17]:
          3
             s = 8 # stride
             fig, ax = plt.subplots(figsize=figure size, dpi=figure dpi)
             fig.text(0.30, 0.05, url)
             ax.scatter(
           8
                 p_o.x[::s], p_o.y[::s],
                 color = 'black',
           9
                 marker = '.'
          10
         11 )
          12
             ax.quiver(
         13
                 p o.x[::s], p_o.y[::s],
          14
                 v t.x[::s], v t.y[::s],
          15
                 \overline{\text{width}} = 0.002,
          16
                 color = 'red',
          17
                 scale = 20,
                 scale units = 'xy',
         18
          19
                 pivot = 'middle'
          20 )
          21
             ax.quiver(
          22
                 p_o.x[::s], p_o.y[::s],
          23
                 v_n.x[::s], v_n.y[::s],
          24
                 width = 0.002,
                 color = 'blue',
          26
                 scale = 20,
          27
                 scale units = 'xy',
                 pivot = 'middle'
          28
          29 )
         30 ax.axis('equal')
         31 plt.show()
```

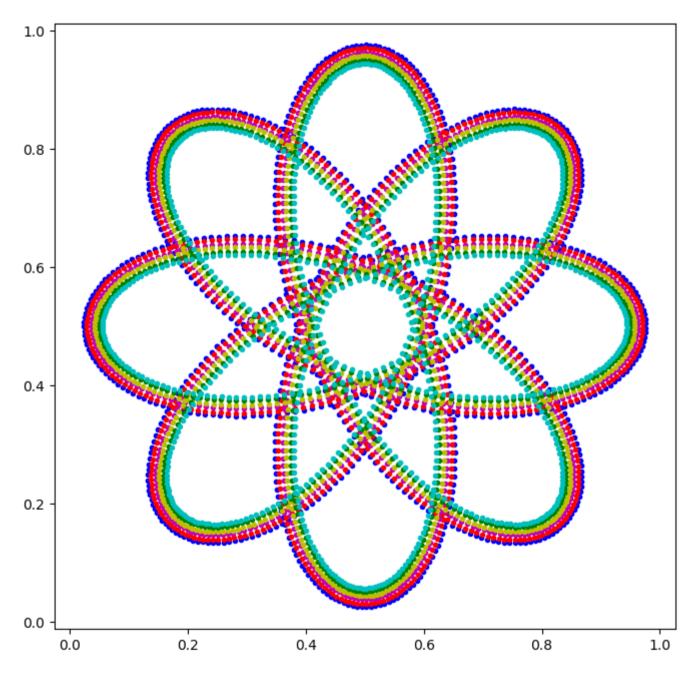


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4 | p_cm = p_o - c * v_n 5 | p_cp = p_o + c * v_n

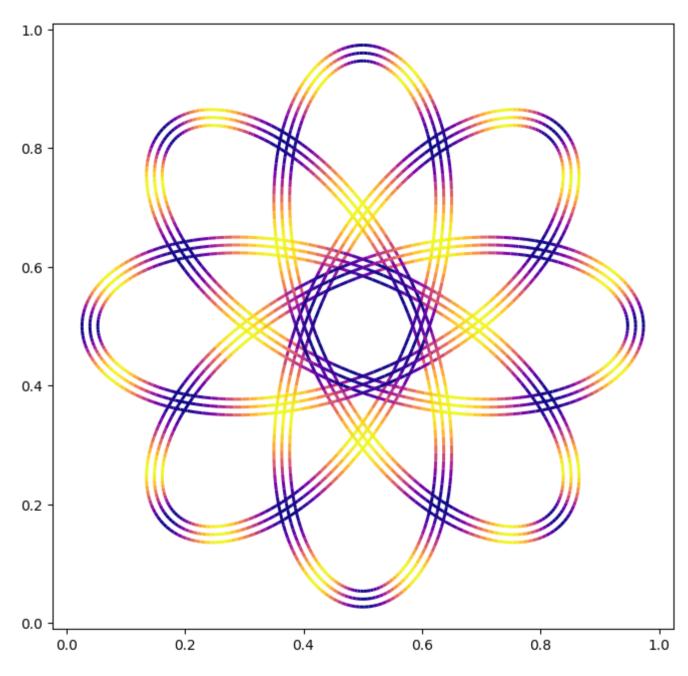


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```
# Prepare for plotting with quad patches (between pairs of offset curves) instead of lines
In [23]:
           3
             def Patches(p e, p f, color='grey'):
           5
                 no of points = len(p e.cnull)
           6
           7
                 return \
           8
           9
                          Polygon(
          10
          11
                                  [ p_e.x[j], p_e.y[j] ],
          12
                                  [ p_f.x[j], p_f.y[j] ],
          13
                                  [ p_f.x[k], p_f.y[k] ],
          14
                                  [ p_e.x[k], p_e.y[k] ]
          15
                              closed = True,
          16
          17
                              color = color
          18
          19
                          for j, k in zip(range(0, no of points-1), range(1, no of points))
          20
          21
             patches outer = Patches(p am, p bm)
             patches inner = Patches(p ap, p bp)
             patches center = Patches(p_cm, p_cp)
```

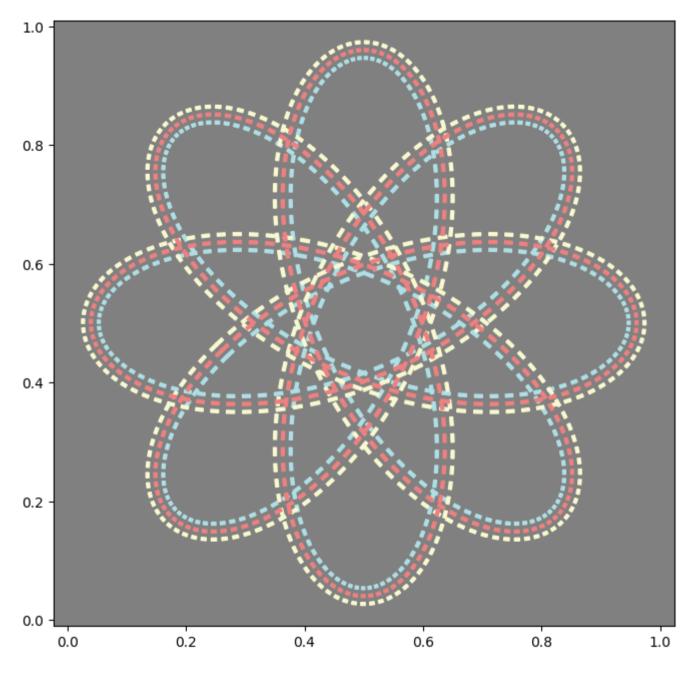
```
In [24]:
             # Prepare colors that cycle along the curves
          2
             c = 2 * np.pi / (no of points along curve / 32)
             d = 2 * np.pi * (1 / 2 + 1 / 16)
          6
             color value = \
          7
                 np.array(
          8
          9
                          (np.sin(i * c - d) + 1) / 2
          10
                         for i in range(no of points along curve)
          11
         12
```

```
# Show the curves with colors cycling
In [25]:
             fig = plt.figure(figsize=figure size, dpi=figure dpi)
             fig.text(0.30, 0.05, url)
             ax = fig.add subplot(1, 1, 1)
             ax.add collection(
                 PatchCollection(
           8
                     patches inner,
                     # match original = True,
          10
                     array = color value,
          11
                     cmap = plt.cm.plasma
          12
          13
          14
             ax.add collection(
                 PatchCollection(
          15
          16
                     patches outer,
          17
                     # match original = True,
                     array = color value,
          18
          19
                     cmap = plt.cm.plasma
          20
          21
          22
             ax.add collection(
          23
                 PatchCollection(
          24
                     patches center,
          25
                     # match original = True,
          26
                     array = color value,
                      cmap = plt.cm.plasma
          27
          28
          29
             ax.axis('equal')
          31
             plt.show()
```

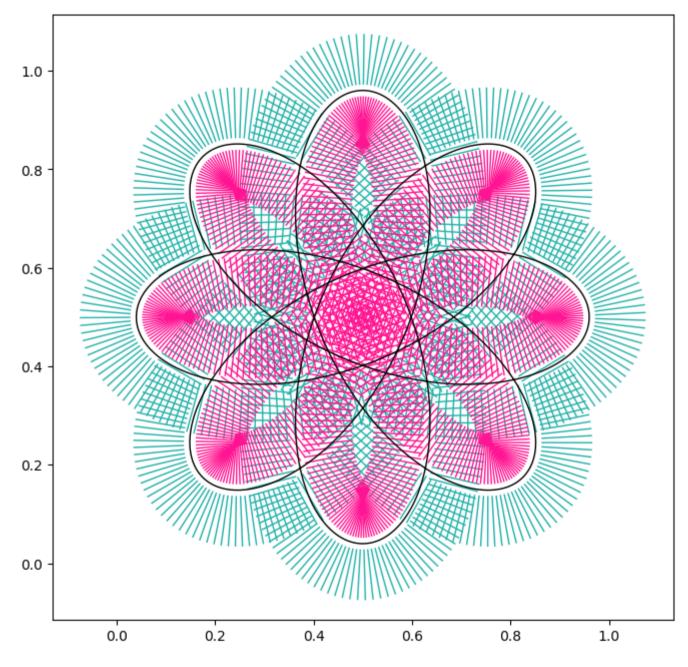


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```
# Show every other patch along the curves
In [26]:
          3
             s = 2 # stride
             fig, ax = plt.subplots(figsize=figure size, dpi=figure dpi)
             fig.text(0.30, 0.05, url)
             ax.add collection(
                 PatchCollection(
          8
          9
                     patches inner[::s],
         10
                     facecolor='powderblue',
                     edgecolor='powderblue'
         11
         12
         13 )
         14
             ax.add collection(
                 PatchCollection(
         15
         16
                     patches_outer[::s],
                     facecolor='lightgoldenrodyellow',
         17
                     edgecolor='lightgoldenrodyellow'
         18
         19
         20 )
         21
             ax.add collection(
         22
                 PatchCollection(
         23
                     patches_center[::s],
         24
                     facecolor='lightcoral',
         25
                     edgecolor='lightcoral'
         26
         27
         28
             ax.set facecolor('gray')
             ax.axis('equal')
         30
             plt.show()
```



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