A tutorial for Discriminant Analysis of Principal Components (DAPC) using adequet 1.3-6

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Abstract

This vignette provides a tutorial for applying the Discriminant Analysis of Principal Components (DAPC [1]) using the *adegenet* package [2] for the R software [3]. This methods aims to identify and describe genetic clusters, although it can in fact be applied to any quantitative data. We illustrate how to use find.clusters to identify clusters, and dapc to describe the relationships between these clusters. More advanced topics are then introduced, such as advanced graphics, assessing the stability of DAPC results and using supplementary individuals.

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1 Introduction

Investigating genetic diversity using multivariate approaches relies on finding synthetic variables built as linear combinations of alleles (i.e. new-variable = a_1 allele₁+ a_2 allele₂+... where a_1 , a_2 etc. are real coefficients) and which reflect as well as possible the genetic variation amongst the studied individuals. However, most of the time we are not only interested in the diversity amongst individuals, but also and possibly more so in the diversity between groups of individuals. Typically, one will be analysing individual data to identify populations, or more largely genetic clusters, and then describe these clusters.

A problem occurring in traditional methods is they usually focus on the entire genetic variation. Genetic variability can be decomposed using a standard multivariate ANOVA model as:

total variance = (variance between groups) + (variance within groups)

or more simply, denoting X the data matrix:

$$VAR(\mathbf{X}) = B(\mathbf{X}) + W(\mathbf{X})$$

Usual approaches such as Principal Component Analysis (PCA) or Principal Coordinates Analysis (PCoA / MDS) focus on $VAR(\mathbf{X})$. That is, they only describe the global diversity, possibly overlooking differences between groups. On the contrary, DAPC optimizes $B(\mathbf{X})$ while minimizing $W(\mathbf{X})$: it seeks synthetic variables, the discriminant functions, which show differences between groups as best as possible while minimizing variation within clusters.

2 Identifying clusters using find.clusters

2.1 Rationale

DAPC in itself requires prior groups to be defined. However, groups are often unknown or uncertain, and there is a need for identifying genetic clusters before describing them. This can be achieved using k-means, a clustering algorithm which finds a given number (say, k) of groups maximizing the variation between groups, $B(\mathbf{X})$. To identify the optimal number of clusters, k-means is run sequentially with increasing values of k, and different clustering solutions are compared using Bayesian Information Criterion (BIC). Ideally, the optimal clustering solution should correspond to the lowest BIC. In practice, the 'best' BIC is often indicated by an elbow in the curve of BIC values as a function of k.

While k-means could be performed on the raw data, we prefer running the algorithm after transforming the data using PCA. This transformation has the major advantage of reducing the number of variables so as to speed up the clustering algorithm. Note that this does not imply a necessary loss of information since all the principal components (PCs) can be retained, and

therefore all the variation in the original data. In practice however, a reduced number of PCs is often sufficient to identify the existing clusters, while making the analysis essentially instantaneous.

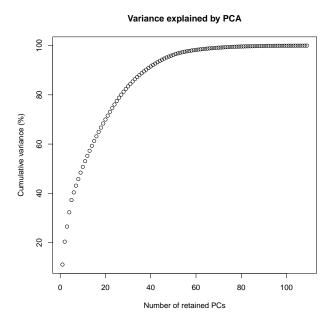
2.2 In practice

Identification of the clusters is achieved by find.clusters. This function first transforms the data using PCA, asking the user to specify the number of retained PCs interactively unless the argument n.pca is provided. Then, it runs k-means algorithm (function kmeans from the stats package) with increasing values of k, unless the argument n.clust is provided, and computes associated summary statistics (by default, BIC). See ?find.clusters for other arguments.

find.clusters is a generic function with methods for data.frame, objects with the class genind (usual genetic markers) and genlight (genome-wide SNP data). Here, we illustrate its use using a toy dataset simulated in [1], dapcIllus:

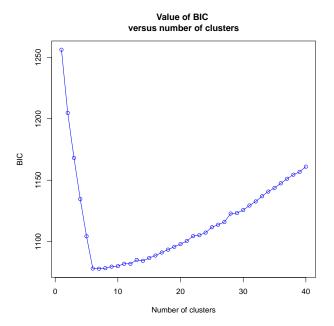
```
> library(adegenet)
> data(dapcIllus)
> class(dapcIllus)
[1] "list"
> names(dapcIllus)
[1] "a" "b" "c" "d"
    dapcIllus is a list containing four datasets; we shall only use the first one:
> x <- dapcIllus$a > x
    #####################
    genotypes of individuals -
S4 class: genind
@call: read.fstat(file = file, missing = missing, quiet = quiet)
@tab: 600 x 140 matrix of genotypes
@ind.names: vector of 600 individual names
@loc.names: vector of 30 locus names
Gloc.names. Vector of So Tocus names
Gloc.natl: number of alleles per locus
Gloc.fac: locus factor for the 140 columns of Gtab
@all.names: list of 30 components yielding allele names for each locus
@ploidv: 2
@ploidy: 2
@type: codom
Optionnal contents:
@pop: factor giving the population of each individual
@pop.names: factor giving the population of each individual
@other: - empty -
```

x is a dataset of 600 individuals simulated under an island model (6 islands) for 30 microsatellite markers. We use find.clusters to identify clusters, although true clusters are, in this case, known (and accessible using pop(x)). We specify that we want to evaluate up to k = 40 groups (max.n.clust=40):



The function displays a graph of cumulated variance explained by the eigenvalues of the PCA. Apart from computational time, there is no reason for keeping a small number of components; here, we keep all the information, specifying to retain 200 PCs (there are actually less PCs —around 110—, so all of them are kept).

Then, the function displays a graph of BIC values for increasing values of k:



This graph shows a clear decrease of BIC until k=6 clusters, after which BIC increases. In this case, the elbow in the curve also matches the smallest BIC, and clearly indicates 6 clusters should be retained. In practice, the choice is often trickier to make for empirical dataset.

The output of find.clusters is a list:

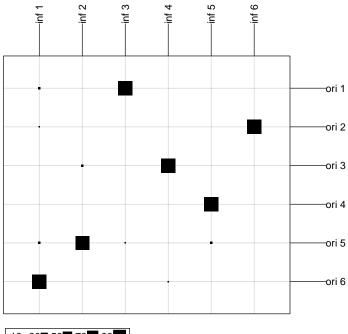
> grp\$size

```
[1] 105 97 98 99 102 99
```

The components are respectively the chosen summary statistics (here, BIC) for different values of k (slot Kstat), the selected number of clusters and the associated BIC (slot stat), the group memberships (slot grp) and the group sizes (slot size). Here, since we know the actual groups, we can check how well they have been retrieved by the procedure. Actual groups are accessed using pop:

> table(pop(x), grp\$grp)

> table.value(table(pop(x), grp\$grp), col.lab=paste("inf", 1:6), row.lab=paste("ori", 1:6))



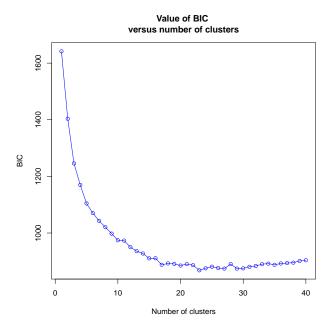
10■ 30■ 50■ 70■ 90

Rows correspond to actual groups ("ori"), while columns correspond to inferred groups ("inf"). Here, we can see that original groups have nearly been perfectly identified by the method.

2.3 How many clusters are there really in the data?

Although the most frequently asked when trying to find clusters in genetic data, this question is equally often meaningless. Clustering algorithms help making a caricature of a complex reality, which is most of the time far from following known population genetics models. Therefore, we are rarely looking for actual panmictic populations from which the individuals have been drawn. Genetic clusters can be biologically meaningful structures and reflect interesting biological processes, but they are still models.

A slightly different but probably more meaningful question would be: "How many clusters are useful to describe the data?". A fundamental point in this question is that clusters are merely tools used to summarise and understand the data. There is no longer a "true k", but some values of k are better, more efficient summaries of the data than others. For instance, in the following case:



, the concept of "true k" is fairly hypothetical. This does not mean that clutering algorithms should necessarily be discarded, but surely the reality is more complex than a few clear-cut, isolated populations. What the BIC decrease says is that 10-20 clusters would provide useful summaries of the data. The actual number retained is merely a question of personnal taste.

3 Describing clusters using dapc

3.1 Rationale

DAPC aims to provide an efficient description of genetic clusters using a few synthetic variables. These are constructed as linear combinations of the original variables (alleles) which have the largest between-group variance and the smallest within-group variance. Coefficients of the alleles used in the linear combination are called *loadings*, while the synthetic variables are themselves referred to as *discriminant functions*.

Moreover, being based on the Discriminant Analysis, DAPC also provides membership probabilities of each individual for the different groups based on the retained discriminant functions. While these are different from the admixture coefficients of software like STRUCTURE, they can still be interpreted as proximities of individuals to the different clusters. Membership probabilities also provide indications of how clear-cut genetic clusters are. Loose clusters will result in fairly flat distributions of membership probabilities of individuals across clusters, pointing to possible admixture.

Lastly, using the allele loadings, it is possible to represent new individuals (which have not participated to the analysis) onto the factorial planes, and derive membership probabilities as welll. Such individuals are referred to as supplementary individuals.

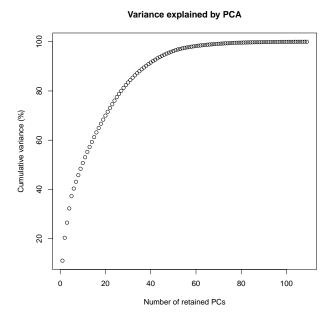
3.2 In practice

DAPC is implemented by the function dapc, which first transforms the data using PCA, and then performs a Discriminant Analysis on the retained principal components. Like find.clusters, dapc is a generic function with methods for data.frame, and objects with the class genind (usual genetic markers) and genlight (genome wide SNP data).

We run the analysis on the previous toy dataset, using the inferred groups stored in grp\$grp:

```
> dapc1 <- dapc(x, grp$grp)</pre>
```

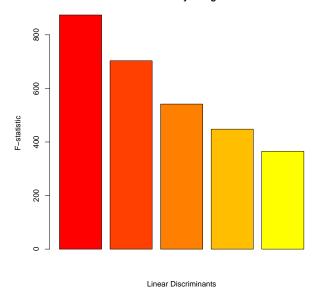
The method displays the same graph of cumulated variance as in find.cluster. However, unlike k-means, DAPC can benefit from not using too many PCs. Indeed, retaining too many components with respect to the number of individuals can lead to over-fitting and unstability in the membership probabilities returned by the method (see section below about the stability of membership probabilities).



The bottomline is therefore retaining a few PCs without sacrificing too much information. Here, we can see that little information is gained by adding PCs after the first 40. We therefore retain 40 PCs.

Then, the method displays a barplot of eigenvalues for the discriminant analysis, asking for a number of discriminant functions to retain (unless argument ${\tt n.da}$ is provided).

Discriminant analysis eigenvalues



For small number of clusters, all eigenvalues can be retained since all discriminant functions can be examined without difficulty. Whenever more (say, tens of) clusters are analysed, it is likely that the first few dimensions will carry more information than the others, and only those can then be retained and interpreted.

The object dapc1 contains a lot of information:

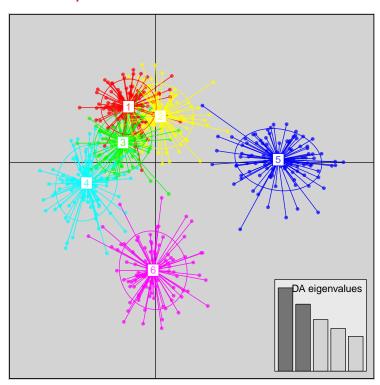
> dapc1

```
************************************
       class: dapc
$call: dapc.genind(x = x, pop = grp$grp, n.pca = 40, n.da = 100)
$n.pca: 40 first PCs of PCA used
$n.da: 5 discriminant functions saved
$var (proportion of conserved variance): 0.915
$eig (eigenvalues): 874.1 703.2 541.5 447.9 365.3 vector
                                                         length content
1 $eig
           5
                 eigenvalues
2 $grp
           600
                 prior group assignment
3 $prior
           6
                 prior group probabilities
           600
                 posterior group assignment
4 $assign
5 $pca.cent 140
                 centring vector of PCA
6 $pca.norm 140
                 scaling vector of PCA
7 $pca.eig 109
                 eigenvalues of PCA
 data.frame
              nrow ncol content
               600 40
                        retained PCs of PCA
 $tab
2 $means
                   40
                        group means
3 $loadings
               40
                   5
                        loadings of variables
4 $ind.coord
              600
                  5
                        coordinates of individuals (principal components)
```

```
5 $grp.coord 6 5 coordinates of groups
6 $posterior 600 6 posterior membership probabilities
7 $pca.loadings 140 40 PCA loadings of original variables
8 $var.contr 140 5 contribution of original variables
```

For details about this content, please read the documentation (?dapc). Essentially, the slots ind.coord and grp.coord contain the coordinates of the individuals and of the groups used in scatterplots. Contributions of the alleles to each discriminant function are stored in the slot var.contr. Eigenvalues, corresponding to the ratio of the variance between groups over the variance within groups for each discriminant function, are stored in eig. Basic scatterplots can be obtained using the function scatterplot:

> scatter(dapc1)



The obtained graph represents the individuals as dots and the groups as inertia ellipses. Eigenvalues of the analysis are displayed in inset. These graphs are fairly easy to customize, as shown below.

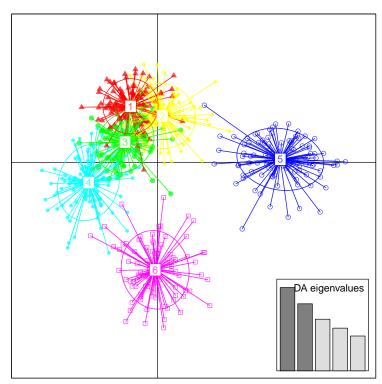
3.3 Customizing DAPC scatterplots

DAPC scatterplots are the main result of DAPC. It is therefore essential to ensure that information is displayed efficiently, and if possible to produce pretty figures. Possibility are almost unlimited, and here we just illustrate a few possibilities offered by scatter. Note that scatter is a generic function,

with a dedicated method for objects produced by dapc. Documentation of this function can be accessed by typing ?scatter.dapc.

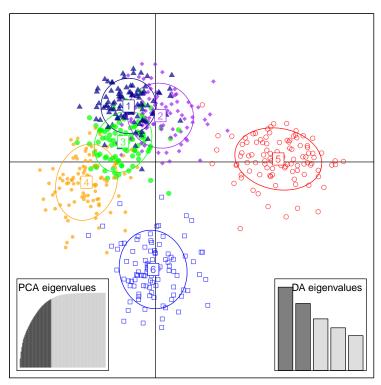
We illustrate some graphical possibilities trying to improve the display of the analysis presented in the previous section. While the default background (grey) allows to visualize rainbow colors (the default palette for the groups) more easily, it is not so pretty and is probably better removed for publication purpose. We also move the inset to a more appropriate place where it does not cover individuals, and use different symbols for the groups.

> scatter(dapc1, posi.da="bottomright", bg="white", pch=17:22)

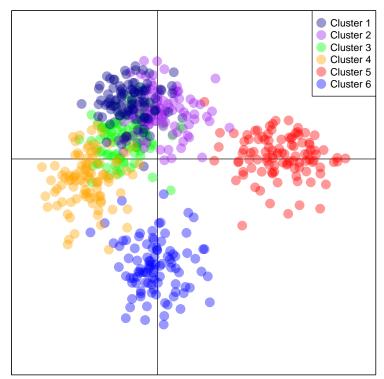


This is still not entirely satisfying: we need to define other colors more visible over a white background, and we can remove the segments linking the points to their ellipses:

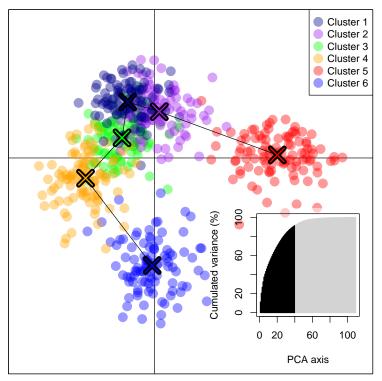
```
> myCol <- c("darkblue","purple","green","orange","red","blue")
> scatter(dapc1, posi.da="bottomright", bg="white", pch=17:22, cstar=0, col=myCol, scree.pca=TRUE, posi.pca="bot
```



Another possibility is remove the labels within the ellipses and add a legend to the plot. We also use the same symbol for all individuals, but use bigger dots and transparent colours to have a better feel for the density of individuals on the factorial plane.

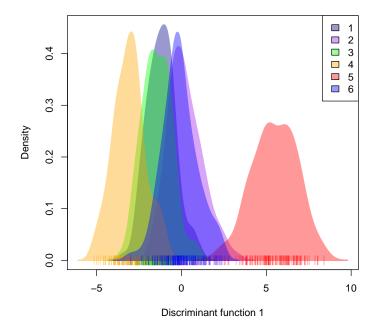


We can also add a minimum spanning tree based on the (squared) distances between populations within the entire space. This allows one to bear in mind the actual proximities between populations inside the entire space, which are not always well represented in susbsets of discriminant functions of lesser rank. We also indicate the centre of each group with crosses. Lastly, we remove the DAPC eigenvalues, not very useful in this case, and replace them manually by a graph of PCA eigenvalues retained in dimension-reduction step (retained eigenvalues in black, similar to using scree.pca=TRUE).



Lastly, note that scatter can also represent a single discriminant function, which is especially useful when only one of these has been retained (e.g. in the case k=2). This is achieved by plotting the densities of individuals on a given discriminant function with different colors for different groups:

> scatter(dapc1,1,1, col=myCol, bg="white", scree.da=FALSE, legend=TRUE, solid=.4)



3.4 Interpreting variable contributions

In DAPC, the variable actually analyzed are principal components of a PCA. Loadings of these variables are generally uninformative, since PCs themselves do not all have straightforward interpretations. However, we can also compute contributions of the alleles, which can turn out to be very informative. In general, there are many alleles and their contribution is best plotted for a single discriminant function at a time.

Variable contributions are stored in the var.contr slot of a dapc object. They can be plotted using loadingplot. We illustrate this using the seasonal influenza dataset H3N2, which contains 1903 isolates genotyped for 125 SNPs located in the hemagglutinin segment (see ?H3N2):

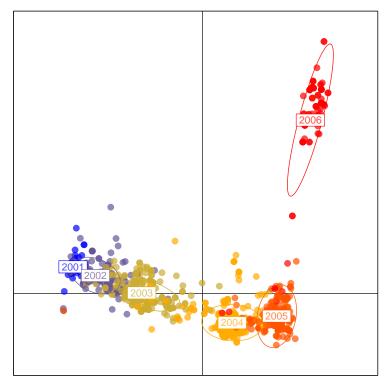
```
@loc.names: vector of 125 locus names
@loc.fac: locus factor for the 334 columns of @tab
@all.names: list of 125 components yielding allele names for each locus
@ploidy: 1
@type: codom

Optionnal contents:
@pop: - empty -
@pop.names: - empty -
@other: a list containing: x xy epid

> pop(H3N2) <- H3N2$other$epid
> dapc.flu <- dapc(H3N2, n.pca=30,n.da=10)</pre>
```

The first discriminant function shows the temporal evolution of the influenza virus, while the second one shows the originality of 2006 strains.

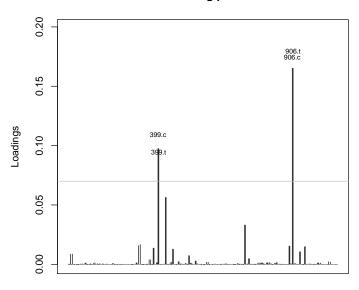
```
> myPal <- colorRampPalette(c("blue","gold","red"))
> scatter(dapc.flu, col=transp(myPal(6)), scree.da=FALSE, cell=1.5, cex=2, bg="white",cstar=0)
```



We can assess which alleles most highlight the originality of 2006 using loadingplot:

```
> set.seed(4)
> contrib <- loadingplot(dapc.flu$var.contr, axis=2, thres=.07, lab.jitter=1)</pre>
```

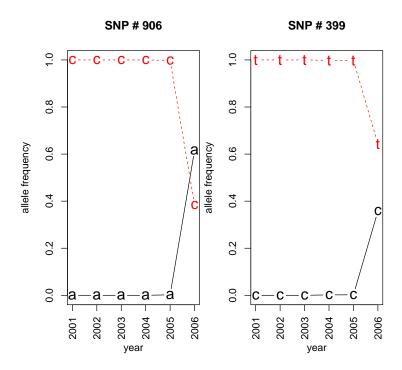
Loading plot



Variables

temp is a list invisibly returned by loadingplot which contains the most contributing alleles (i.e., contributions above a given threshold – argument threshold). In this case, SNPs 906 and 399 reflect most the temporal evolution of the virus. We can look into their allele frequencies over 2002-2006:

```
> par(mfrow=c(1,2), mar=c(5.1,4.1,4.1,.1),las=3)
> matplot(freq906, pch=c("a","c"), type="b",xlab="year",ylab="allele frequency", xaxt="n", cex=1.5, main="SNP # 9
> axis(side=1, at=1:6, lab=2001:2006)
> matplot(freq399, pch=c("c","t"), type="b", xlab="year",ylab="allele frequency", xaxt="n", cex=1.5, main="SNP #
> axis(side=1, at=1:6, lab=2001:2006)
```



In both cases, a new allele appeared in 2005 at a very low frequency, and reached high or even dominant frequencies a year later. Irrespective of the mecanism underlying these changes (drift or selection), this illustrates that in seasonal influenza, specific nucleotides can undergo drastic changes within only a couple of years.

3.5 Interpreting group memberships

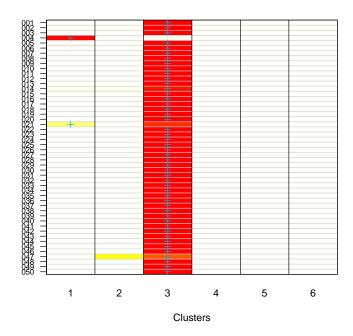
Besides scatterplots of discriminant functions, group memberships of DAPC can be exploited. Note that caution should be taken when interpreting group memberships of a DAPC based on too many PCs, as there are risks of overfitting the discriminant functions (see section below). But despite this possible bias, group memberships can be used as indicators of how clear-cut genetic clusters are. Note that this is most useful for groups defined by an external criteria, i.e. defined biologically, as opposed to identified by k-means. It is less useful for groups identified using find.clusters, since we expect k-means to provide optimal groups for DAPC, and therefore both classifications to be mostly consistent.

Membership probabilities are based on the retained discriminant functions. They are stored in dapc objects in the slot posterior:

Each row corresponds to an individual, each column to a group. This information can be summarized using summary on the dapc object:

The slot assign.per.pop indicates the proportions of successful reassignment (based on the discriminant functions) of individuals to their original clusters. Large values indicate clear-cut clusters, while low values suggest admixed groups.

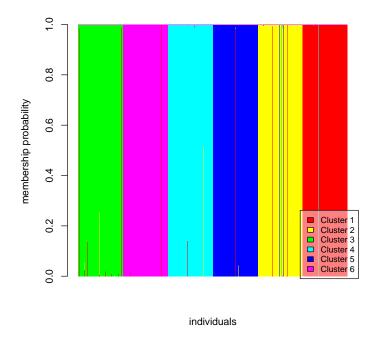
This information can also be visualized using assignplot (see ?assignplot for display options); here, we choose to represent only the first 50 individuals to make the figure readable:



This figure is the simple graphical translation of the posterior table above. Heat colors represent membership probabilities (red=1, white=0); blue crosses represent the prior cluster provided to DAPC. Here in most individuals, DAPC classification is consistent with the original clusters (blue crosses are on red rectangles), except for one discrepancy in individual 21, classified in group 1 while DAPC would assign it to group 3. Such figure is particularly useful when prior biological groups are used, as one may infer admixed or misclassified individuals.

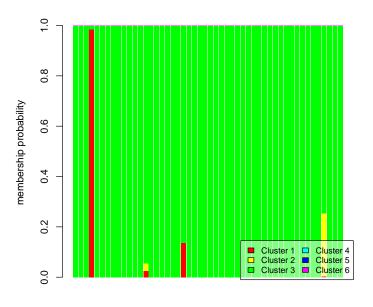
Note that this information can also be plotted in a STRUCTURE-like (!) way using compoplot (see ?compoplot to customize the plot). We can plot information of all individuals to have a global picture of the clusters composition.

> compoplot(dapc1, posi="bottomright", txt.leg=paste("Cluster", 1:6), lab="", ncol=1, xlab="individuals")



We can also have a closer look at a subset of individuals; for instance, for the first 50 individuals:

> compoplot(dapc1, subset=1:50, posi="bottomright", txt.leg=paste("Cluster", 1:6), lab="", ncol=2, xlab="individu

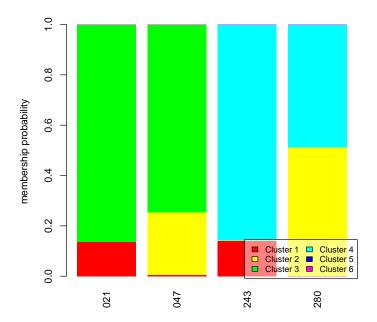


individuals

Obviously, we can use the power of R to lead our investigation further. For instance, which are the most 'admixed' individuals? Let us consider as admixed individuals having no more than 90% of probability of membership in a single cluster:

```
> temp <- which(apply(dapc1$posterior,1, function(e) all(e<0.9)))
> temp

021 047 243 280
    21 47 243 280
> compoplot(dapc1, subset=temp, posi="bottomright", txt.leg=paste("Cluster", 1:6), ncol=2)
```



4 On the stability of group membership probabilities

4.1 When and why group memberships can be unreliable

In DAPC, discriminant functions are linear combinations of variables (principal components of PCA) which optimize the separation of individuals into predefined groups. Based on the retained discriminant functions, it is possible to derive group membership probabilities, which can be interpreted in order to assess how clear-cut or admixed the clusters are. Unfortunately, retaining too many PCs with respect to the number of individuals can lead to over-fitting the discriminant functions. In such case, discriminant functions become so "flexible" that they could discriminate almost perfectly any cluster. As a result, membership probabilities can become drastically inflated for the best-fitting cluster, resulting in apparent perfect discrimination.

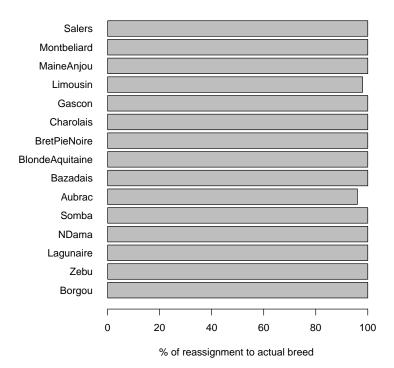
This point can be illustrated using the microbov dataset (704 cattles of 15 breeds typed for 30 microsatellite markers). We first examine the % of successful reassignment (i.e., quality of discrimination) for different numbers of retained PCs. First, retaining 3 PCs during the dimension-reduction step, and all discriminant functions:

```
> data(microbov)
> microbov
    #####################
   genotypes of individuals -
S4 class: genind
@call: genind(tab = truenames(microbov)$tab, pop = truenames(microbov)$pop)
Otab: 704 x 373 matrix of genotypes
@ind.names: vector of 704 individual names
@loc.names: vector of 30 locus names
@loc.namles: vector or 30 locus names
@loc.nall: number of alleles per locus
@loc.fac: locus factor for the 373 columns of @tab
@all.names: list of 30 components yielding allele names for each locus
@ploidy: 2
@type: codom
Optionnal contents:
@pop: factor giving the population of each individual @pop.names: factor giving the population of each individual
Oother: a list containing: coun breed spe
> temp <- summary(dapc(microbov, n.da=100, n.pca=3))$assign.per.pop*100
> par(mar=c(4.5,7.5,1,1))
> barplot(temp, xlab="% of reassignment to actual breed", horiz=TRUE, las=1)
            Salers
      Montbeliard
      MaineAnjou
         Limousin
          Gascon
        Charolais
     BretPieNoire
 BlondeAquitaine
         Bazadais
           Aubrac
           Somba
          NDama
        Lagunaire
             Zebu
          Borgou
                     0
                                20
                                             40
                                                         60
                                                                     80
```

% of reassignment to actual breed

We can see that some breeds are well discriminated (e.g. Zebu, Lagunaire, > 90%) while others are entirely overlooked by the analysis (e.g. Bretone Pie Noire, Limousin, <10%). This is because too much genetic information is lost when retaining only 3 PCs. We repeat the analysis, this time keeping 300 PCs:

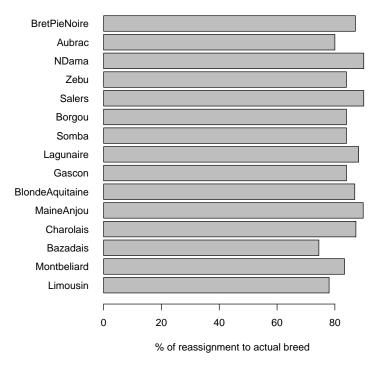
```
> temp <- summary(dapc(microbov, n.da=100, n.pca=300))$assign.per.pop*100
> par(mar=c(4.5,7.5,1,1))
> barplot(temp, xlab="% of reassignment to actual breed", horiz=TRUE, las=1)
```



We now obtain almost 100% of discrimination for all groups. Is this result satisfying? Actually not. The number of PCs retained is so large that discriminant functions could model any structure and virtually any set of clusters would be well discriminated. This can be illustrated by running the analysis using randomized groups:

```
> x <- microbov
> pop(x) <- sample(pop(x))
> temp <- summary(dapc(x, n.da=100, n.pca=300))$assign.per.pop*100

> par(mar=c(4.5,7.5,1,1))
> barplot(temp, xlab="% of reassignment to actual breed", horiz=TRUE, las=1)
```



Groups have been randomised, and yet we still get very good discrimination. There is therefore a trade-off between finding a space with a good power of discrimination using DAPC, and retaining too many dimensions and cause overfitting.

4.2 Using the a-score

The trade-off between power of discrimination and over-fitting can be measured by the a-score, which is simply the difference between the proportion of successful reassignment of the analysis (observed discrimination) and values obtained using random groups (random discrimination). It can be seen as the proportion of successful reassignment corrected for the number of retained PCs. It is implemented by a.score, which relies on repeating the DAPC analysis using randomized groups, and computing a-scores for each group, as well as the average a-score:

```
        sim.1
        0.74
        0.84
        0.8235294
        0.5666667
        0.58

        sim.2
        0.76
        0.72
        0.8627451
        0.5333333
        0.78

        sim.3
        0.60
        0.78
        0.8627451
        0.5000000
        0.70

        sim.4
        0.64
        0.74
        0.8627451
        0.5333333
        0.70

        sim.5
        0.72
        0.76
        0.9607843
        0.5000000
        0.80
```

> temp\$pop.score

Borgou	Zebu	Lagunaire	NDama	Somba
0.6380000	0.7420000	0.8509804	0.5166667	0.7180000
Aubrac	Bazadais	BlondeAquitaine	BretPieNoire	Charolais
0.4940000	0.8382979	0.3016393	0.4741935	0.5563636
Gascon	Limousin	MaineAnjou	Montbeliard	Salers
0.6640000	0.4280000	0.8653Ŏ61	0.6733333	0.7720000

> temp\$mean

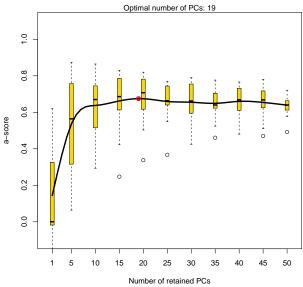
[1] 0.6355187

The number of retained PCs can be chosen so as to optimize the a-score; this is achived by optim.a.score:

```
> dapc2 <- dapc(microbov, n.da=100, n.pca=50)</pre>
```

> temp <- optim.a.score(dapc2)</pre>

a-score optimisation - spline interpolation

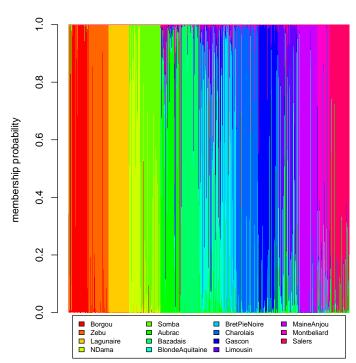


Since evaluating solutions for 1, 2, ... 100 retained PCs is unusefully computer-intensive, as a first approximation the method evaluates a few numbers of retained PCs in this range, and uses spline interpolation to approximate the optimal number of PCs to retain. Then, one can evaluate all solutions within a restrained range using the argument n.pca. For the microbov dataset, we should probably retained between 10 and 30 PCs during the dimension-reduction step.

We perform the analysis with 20 PCs retained, and then map the membership probabilities as before:

```
> dapc3 <- dapc(microbov, n.da=100, n.pca=20)
> myCol <- rainbow(15)

> par(mar=c(5.1,4.1,1.1,1.1), xpd=TRUE)
> compoplot(dapc3, lab="", posi=list(x=12,y=-.01), cleg=.7)
```



And as before, we can investigate further admixed individuals, which we arbitrarily define as those having no more than 0.5 probability of membership to any group:

```
> temp <- which(apply(dapc3$posterior,1, function(e) all(e<0.5)))
> temp
```

```
AFBIBOR9511
                            FRBTAUB9070
                                          FRBTAUB9078
                                                        FRBTAUB9225 FRBTBDA29851
              FRBTAUB9062
                       233
                                     241
                                                   249
                                                                265
FRBTBDA29856
             FRBTBDA29879
                           FRBTBDA35248
                                         FRBTBDA35256
                                                       FRBTBDA35259
                                                                     FRBTBDA35267
                                     361
                       374
         372
                                     382
                                                   386
                                                                405
                                                                              409
FRBTBPN1915
                           FRBTGAS14183
             FRBTCHA15957
                                                        FRBTGAS9200
                                                                    FRBTLIM30832
                                          FRBTMBE1496
FRBTLIM30839
             FRBTLIM30855
                            FRBTMA25298
                                                        FRBTMBE1514
         550
                                     579
                                                   625
                                                                636
                                                                              651
```

- > lab <- pop(microbov)
 > par(mar=c(8,4,5,1), xpd=TRUE)
 > compoplot(dapc3, subset=temp, cleg=.6, posi=list(x=0,y=1.2),lab=lab)
- BondeAquitaine
 BondeA

Admixture appears to be the strongest between a few breeds (Blonde d'Aquitaine, Bretonne Pie-Noire, Limousine and Gascone). Some features are fairly surprising; for instance, the last individual is fairly distant from its cluster, but has almost 50% chances of being assigned to two other breeds.

5 Using supplementary individuals

5.1 Rationale

Statistically speaking, supplementary individuals are observations which do not participate to constructing a model, but which we would like to predict using a model fitted on other ("training") data. In the context of DAPC,

we may know groups for most individuals, but some individuals could be of unknown or uncertain group. In this case, we need to exclude individuals from the analysis, and then project them as supplementary individuals onto the discriminant functions. The only requirement for this operation is that supplementary individuals have been typed for the same loci as the rest of the dataset.

Technically, using supplementary individuals consists in transforming the new data using the centring and scaling of the "training data", and then using the same discriminant coefficients as for the contributing individuals to predict the position of the new individuals onto the discriminant functions.

5.2 In practice

We will illustrate the practice of supplementary individuals using the cattle breeds data previously analyzed (microbov dataset). We first split the dataset into two parts: one used for the analysis, and one used as supplementary individuals:

```
> data(microbov)
> set.seed(2)
> kept.id <- unlist(tapply(1:nInd(microbov), pop(microbov), function(e) sample(e, 20,replace=FALSE)))
> x <- microbov[kept.id]
> x.sup <- microbov[-kept.id]
> nInd(x)

[1] 300
> nInd(x.sup)
```

 ${\tt x}$ is a **genind** containing the data to be analyzed; ${\tt x.sup}$ contains the supplementary individuals.

We perform the DAPC of x, and use predict to predict results for the supplementary individuals:

```
> dapc4 <- dapc(x,n.pca=20,n.da=15)
> pred.sup <- predict.dapc(dapc4, newdata=x.sup)
> names(pred.sup)

[1] "assign"    "posterior"    "ind.scores"

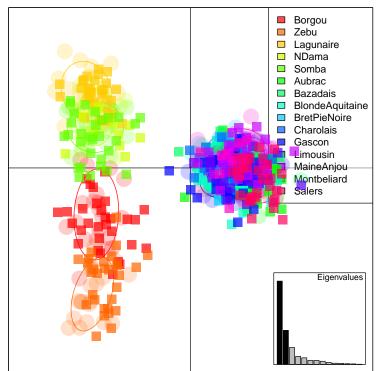
> head(pred.sup$assign)

[1] Borgou Borgou Borgou Borgou Borgou
15 Levels: Borgou Zebu Lagunaire NDama Somba Aubrac ... Salers
> pred.sup$ind.scores[1:5,1:3]
```

```
LD1
                                                LD3
001 -3.896992 -5.288381
002 -2.445063 -4.422078
003 -4.692576 -2.717198
                                      0.4570651
                                      0.2134797
0.4914203
004 -4.919515 -2.317070 -0.2390356
005 -4.718570 -0.200391 -0.9196541
> round(pred.sup$posterior[1:5, 1:5],3)
                 Zebu Lagunaire NDama Somba
      Borgou Zebu
0.612 0.388
                                         0.000 0.000
      0.983 0.017
1.000 0.000
                                      0 0.000 0.000
0 0.000 0.000
002
003
                 0.000
                                      Ö
                                         0.000
                                                  0.000
004
       1.000
       0.688
                 0.000
                                      0
                                         0.208 0.105
```

The list pred.sup contains all the predictions about the new data based on the analysis stored in dapc4. The slot assign contains the assignment of new individuals to groups; ind.scores contains the coordinates of the new individuals on the discriminant functions; posterior contains the posterior membership probabilities. We can visualize the information by different ways. First, we can represent the new individuals using a scatterplot:

```
> col <- rainbow(length(levels(pop(x))))
> col.points <- transp(col[as.integer(pop(x))],.2)
> scatter(dapc4, col=col, bg="white", scree.da=0, pch="", cstar=0, clab=0, xlim=c(-10,10), legend=TRUE)
> par(xpd=TRUE)
> points(dapc4$ind.coord[,1], dapc4$ind.coord[,2], pch=20, col=col.points, cex=5)
> col.sup <- col[as.integer(pop(x.sup))]
> points(pred.sup$ind.scores[,1], pred.sup$ind.scores[,2], pch=15, col=transp(col.sup,.7), cex=2)
> add.scatter.eig(dapc4$eig,15,1,2, posi="bottomright", inset=.02)
```



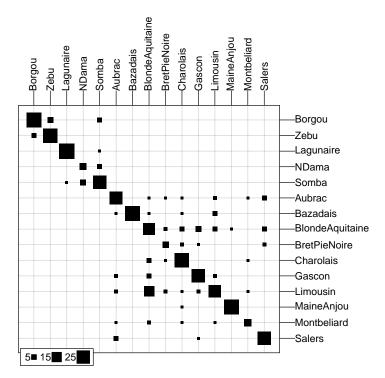
Light dots and ellipses correspond to the original analysis, while more solid squares indicate supplementary individuals. Results are fairly satisfying:

```
> mean(as.character(pred.sup$assign)==as.character(pop(x.sup)))
```

[1] 0.7549505

Around 75% of individuals have been assigned to their actual cluster. For more details about which breed was assigned to which cluster, we can display the contingency table of the actual cluster vs the inferred one:

> table.value(table(pred.sup\$assign, pop(x.sup)), col.lab=levels(pop(x.sup)))



Columns correspond to actual clusters of the supplementary individuals, while rows correspond to inferred clusters. Overall, groups are fairly well retrieved, but we can notice that individuals of Blonde d'Aquitaine breed are poorly identified compared to other breeds.

References

[1] Jombart T, Devillard S and Balloux, F (2010). Discriminant analysis of principal components: a new method for the analysis of genetically structured populations. *BMC Genetics* 11: 94.

- [2] Jombart, T. (2008) adegenet: a R package for the multivariate analysis of genetic markers. *Bioinformatics* 24: 1403-1405.
- [3] R Development Core Team (2011). R: A language and environment for statistical computing. R Foundation for Statistical Computing, Vienna, Austria. ISBN 3-900051-07-0.