

Kernel-Based Object Tracking

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Introduction

Two major components of tracking:

- Target Representation and Localization
- Filtering and Data Association

We introduce an Approach toward target representation and localization based on **Mean-Shift Algorithm**[2].

Target Representation

- ① Target in the image
is represented by an **ellipsoidal region**, which then will be
normalized to a **unit circle**.
⇒ Normalized pixel locations $\{x_i^*\}_{i=1 \dots n}$ centered in 0.
- ② Feature Space
RGB color space quantized into $16 \times 16 \times 16$ bins.
⇒ $m = 16^3 = 4096$ -bins histogram

③ Target Model

is represented by its **probability density function (pdf)** in the feature space.

$$\hat{q}_u = C \sum_{i=1}^n k(\|x_i^*\|^2) \delta[b(x_i^*) - u]$$

- $k : [0, \infty) \rightarrow \mathbb{R}$ is convex and monotonic decreasing **profile of an isotropic kernel**: $K(x) = k(\|x\|^2)$
- $b : \mathbb{R}^2 \rightarrow \{1 \dots m\}$ return bin of the pixel in the quantized feature space
- $C = \frac{1}{\sum_{i=1}^n k(\|x_i^*\|^2)}$ is a constant, which ensures $\sum_{u=1}^m \hat{q}_u = 1$

$\{x_i\}_{i=1 \dots n_h}$ are normalized pixel locations of target candidate, centered in y in the current frame.

③ Target Candidate

is also represented by its **probability density function** (pdf) in the feature space.

$$\hat{p}_u(y) = C_h \sum_{i=1}^{n_h} k\left(\left\|\frac{y - x_i}{h}\right\|^2\right) \delta[b(x_i) - u]$$

- $k : [0, \infty) \rightarrow \mathbb{R}$ is convex and monotonic decreasing **profile of an isotropic kernel**: $K(x) = k(\|x\|^2)$
- h : defines the scale of the target candidate
- $b : \mathbb{R}^2 \rightarrow \{1 \dots m\}$ return bin of the pixel in the quantized feature space
- $C_h = \frac{1}{\sum_{i=1}^{n_h} k\left(\left\|\frac{y - x_i}{h}\right\|^2\right)}$ is a constant, which ensures $\sum_{u=1}^m \hat{p}_u = 1$

Similarity Function

To calculate distance between target and candidates we need to define a **distance function between two distributions**.

$$d(y) = \sqrt{1 - \hat{\rho}(y)}$$

where $\hat{\rho}(y) \equiv \hat{\rho}[\hat{p}(y), \hat{q}] = \sum_{u=1}^m \sqrt{\hat{p}_u(y)\hat{q}_u}$ is the sample estimate of **Bhattacharrya coefficient**.

Note : $d(y)$ is smooth \Rightarrow we can apply gradient-based optimization!

Target Localization

The Problem of Target Localization is equal to **Minimization of $d(y)$** OR **Maximization of Bhattacharrya coefficient $\hat{\rho}(y)$.**

Let \hat{y}_0 be a target location in the previous frame.

$$\hat{\rho}[\hat{p}(y), \hat{q}] \approx \frac{1}{2} \sum_{u=1}^m \sqrt{\hat{p}_u(\hat{y}_0) \hat{q}_u} + \frac{C_h}{2} \sum_{u=1}^m w_i k\left(\left\|\frac{y - x_i}{h}\right\|^2\right)$$

$$\text{where } w_i = \sum_{u=1}^m \sqrt{\frac{\hat{q}_u}{\hat{p}_u(\hat{y}_0)}} \delta[b(x_i) - u].$$

Maximize the second term, because the first term is independent on y :

$$\hat{y}_1 = \frac{\sum_{i=1}^{n_h} x_i w_i g\left(\left\|\frac{y - x_i}{h}\right\|^2\right)}{\sum_{i=1}^{n_h} w_i g\left(\left\|\frac{y - x_i}{h}\right\|^2\right)}$$

where $g(x) = -k'(x)$, assumed that $k'(x)$ exist almost everywhere.

Epanechnikov Kernel

In d -dimensional case

$$k(x) = \begin{cases} \frac{1}{2} c_d^{-1} (d+2)(1 - \|x\|) & \text{if } \|x\| \leq 1 \\ 0 & \text{otherwise} \end{cases}$$

where c_d is the volume of the unit d -dimensional sphere.

In one dimensional case: $d = 1$, $c_d = 2\pi$.

For this Kernel $g(x)$ is a constant. If we use it for \hat{y}_1 we become:

$$\hat{y}_1 = \frac{\sum_{i=1}^{n_h} x_i w_i g\left(\left\|\frac{y-x_i}{h}\right\|^2\right)}{\sum_{i=1}^{n_h} w_i g\left(\left\|\frac{y-x_i}{h}\right\|^2\right)} \Rightarrow \hat{y}_1 = \frac{\sum_{i=1}^{n_h} x_i w_i}{\sum_{i=1}^{n_h} w_i}$$

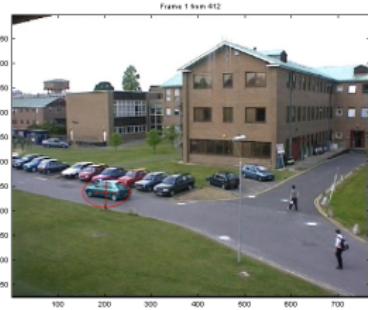
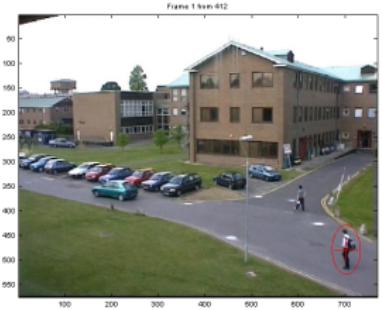
Algorithm

Input: Target model $\{q_u\}_{u=1\dots m}$

Location \hat{y}_0 of target in previous frame

- ① Initialize location of the target in the current frame with \hat{y}_0 , compute $\{\hat{p}(\hat{y}_0)_u\}_{u=1\dots m}$
- ② Compute weights $w_i = \sum_{u=1}^m \sqrt{\frac{\hat{q}_u}{\hat{p}_u(\hat{y}_0)}} \delta[b(x_i) - u]$
- ③ Compute the next location $\hat{y}_1 = \frac{\sum_{i=1}^{n_h} x_i w_i}{\sum_{i=1}^{n_h} w_i}$
- ④ If $\|\hat{y}_1 - \hat{y}_0\| < \epsilon$ Stop
Else $\hat{y}_0 = \hat{y}_1$ and go to 2

Calculation Results



Red Cup



Owl



PETS01D1Human1man



PETS01D1Human1car



References I

- [1] D. Comaniciu and P. Meer. Mean shift: A robust approach toward feature space analysis. *IEEE Computer Society*, 24:603–619, 2002.
- [2] D. Comaniciu, V. Ramesh, and P. Meer. Kernel-based object tracking. *IEEE Computer Society*, 25:564–577, 2003.

The End

Thank you for your Attention!

