LambdaJS quick reference

Marek Materzok

December 11, 2015

1 Syntax

```
let (x = e) e | \mathbf{rec} (x = e) e | \mathbf{if} (e) e \mathbf{else} e |
             label i : e \mid \mathbf{break} \ i \ e \mid \mathbf{throw} \ e \mid \mathbf{try} \ e \ \mathbf{catch} \ (x) \ e \mid \mathbf{try} \ e \ \mathbf{finally} \ e \mid
             e[e\langle pa\rangle] | e[e\langle pa\rangle = e] | e[\mathbf{delete} \ e] | e[\langle oa\rangle] | e[\langle oa\rangle = e] |
              \{[oa:e,\ldots]s:pe,\ldots\}
             \{value : e, writable : e, enumerable : e, configurable : e\} <math>|
              \{getter : e, setter : e, enumerable : e, configurable : e\}
             b \mid n \mid k \mid s \mid \mathbf{undef} \mid \mathbf{null} \mid \mathbf{empty}
             true | false
             IEEE floating-point numbers
             UTF-16 encoded strings
  k
             32-bit integers
un
             typeof | strlen | is-primitive | is-closure | is-object |
              to-string | to-number | to-boolean | to-int | ntoc | cton |
             |\cdot| \sim |-| abs | floor | ceil | \dots
             + | - | * | / | \% | < | == | === | +_s | <_s | \& | | | ^ | << | >> | >>> |
bin
             has-own-property | has-internal | is-accessor | char-at | ...
             value | writable | getter | setter | enumerable | configurable
             {\bf proto}\,|\,{\bf class}\,|\,{\bf extensible}\,|\,{\bf code}\,|\,i
```

2 Semantics

Presented in big-step style; the formalized pretty-big-step semantics in Coq can be obtained from it. Abort-handling rules (for throws and breaks) are not presented.

2.1 Additional syntax

```
\begin{array}{lll} v & ::= & l \mid (\Delta; x, \ldots; e) \mid ptr \\ ptr & ::= & heap \ pointers \\ r & ::= & v \mid \mathbf{throw} \ v \mid \mathbf{break} \ i \ v \\ o & ::= & \left\{ [\mathbf{proto} : v, \mathbf{class} : s, \mathbf{extensible} : b, \mathbf{code} : v, \ldots] \ s : p, \ldots \right\} \\ p & ::= & \left\{ \mathbf{value} : v, \mathbf{writable} : v, \mathbf{enumerable} : b, \mathbf{configurable} : b \right\} \mid \\ & \left\{ \mathbf{getter} : v, \mathbf{setter} : v, \mathbf{enumerable} : b, \mathbf{configurable} : b \right\} \end{array}
```

2.2 Helper functions and predicates

2.2.1 Handling empty results

The following is used in the semantic rules for the double semicolon:

```
egin{array}{lll} v+\mathbf{empty}&=&v\\ v+v'&=&v'&v'
empty\\ v+\mathbf{throw}\;v'&=&\mathbf{throw}\;v\\ v+\mathbf{break}\;i\;v'&=&\mathbf{break}\;i\;(v+v') \end{array}
```

2.2.2 Control flow breaking results

$$\overline{\text{abort}(\mathbf{throw}\ v)} \qquad \overline{\text{abort}(\mathbf{break}\ i\ v)}$$

2.2.3 Restrictions on object and property attributes

Used in semantic rules for setting attributes.

2.2.4 Property attribute writing

Note: changing the attribute type does not occur often (probably only in DefineOwnProperty). I consider removing this from the semantics and adding a simpler primitive instead.

$$\left\{ \begin{array}{l} \mathbf{p}a:v,\dots \}(pa=v') &=& \{pa:v',\dots \} \\ \mathbf{value}:v_1 \\ \mathbf{writable}:b_1 \\ \mathbf{enumerable}:b_2 \\ \mathbf{configurable}:b_3 \\ \mathbf{getter}:v_1 \\ \mathbf{setter}:v_2 \\ \mathbf{enumerable}:b_1 \\ \mathbf{configurable}:b_2 \end{array} \right\} (pa=v) &=& \left\{ \begin{array}{l} \mathbf{getter}:\mathbf{undef} \\ \mathbf{setter}:\mathbf{undef} \\ \mathbf{enumerable}:b_2 \\ \mathbf{value}:\mathbf{undef} \\ \mathbf{writable}:\mathbf{true} \\ \mathbf{enumerable}:b_1 \\ \mathbf{configurable}:b_2 \end{array} \right\} (pa=v) &=& \left\{ \begin{array}{l} pa \text{ is one of:} \\ \mathbf{value}:\mathbf{undef} \\ \mathbf{writable}:\mathbf{true} \\ \mathbf{enumerable}:b_1 \\ \mathbf{configurable}:b_2 \end{array} \right\} (pa=v) &=& \left\{ \begin{array}{l} pa \text{ is one of:} \\ \mathbf{value}:\mathbf{undef} \\ \mathbf{value}:\mathbf{value} \\ \mathbf{value}:\mathbf{value}:\mathbf{value} \\ \mathbf{value}:\mathbf{value}:\mathbf{value} \\ \mathbf{value}:\mathbf{value} \\ \mathbf{value}:\mathbf{value} \\ \mathbf{value}:\mathbf{value}:\mathbf{value} \\ \mathbf{value}:\mathbf{value}:\mathbf{value} \\ \mathbf{value}:\mathbf{value}:\mathbf{value}:\mathbf{value} \\ \mathbf{value}:\mathbf{v$$

2.3 Semantic rules

2.3.1 Variables and functions

2.3.2 Operators

2.3.3 Control flow

$$\frac{\Delta;\Phi;e \Downarrow \Phi';\mathbf{true} \quad \Delta;\Phi';e_1 \Downarrow \Phi'';r}{\Delta;\Phi;\mathbf{if}\,(e)\,\,e_1\,\mathbf{else}\,\,e_2 \Downarrow \Phi'';r} \qquad \qquad \frac{\Delta;\Phi;e \Downarrow \Phi';\mathbf{false} \quad \Delta;\Phi';e_2 \Downarrow \Phi'';r}{\Delta;\Phi;\mathbf{if}\,(e)\,\,e_1\,\mathbf{else}\,\,e_2 \Downarrow \Phi'';r}$$

$$\frac{\Delta;\Phi;e\Downarrow\Phi';\mathbf{break}\;i\;v}{\Delta;\Phi;\mathbf{label}\;i:e\Downarrow\Phi';v} \qquad \frac{\Delta;\Phi;e\Downarrow\Phi';r\;\;\forall v,r\neq\mathbf{break}\;i\;v}{\Delta;\Phi;\mathbf{label}\;i:e\Downarrow\Phi';r} \qquad \frac{\Delta;\Phi;e\Downarrow\Phi';v}{\Delta;\Phi;\mathbf{break}\;i\;e\Downarrow\Phi';\mathbf{break}\;i\;v}$$

$$\frac{\Delta;\Phi;e\Downarrow\Phi';v}{\Delta;\Phi;\mathbf{throw}\;e\Downarrow\Phi';\mathbf{throw}\;v} \qquad \qquad \frac{\Delta;\Phi;e_1\Downarrow\Phi';r \qquad \forall v,r\neq\mathbf{throw}\;v}{\Delta;\Phi;\mathbf{try}\;e_1\;\mathbf{catch}\,(x)\,e_2\Downarrow\Phi';r}$$

$$\frac{\Delta; \Phi; e_1 \Downarrow \Phi'; r \qquad \Delta; \Phi'; e_2 \Downarrow \Phi''; v}{\Delta; \Phi; \mathbf{try} \ e_1 \ \mathbf{finally} \ e_2 \Downarrow \Phi''; r} \qquad \frac{\Delta; \Phi; e_1 \Downarrow \Phi'; r \qquad \Delta; \Phi'; e_2 \Downarrow \Phi''; r' \quad \mathbf{abort}(r')}{\Delta; \Phi; \mathbf{try} \ e_1 \ \mathbf{finally} \ e_2 \Downarrow \Phi''; r'}$$

2.3.4 Property access

$$\frac{\Delta;\Phi;e_1 \Downarrow \Phi';ptr \qquad \Delta;\Phi';e_2 \Downarrow \Phi'';s \qquad \Phi''(ptr) = \{[\dots]\,s:\{pa:v\},\dots\}}{\Delta;\Phi;e_1\,[e_2\langle pa\rangle] \Downarrow v;\Phi''}$$

$$\Delta; \Phi_1; e_2 \Downarrow \Phi_2; s \qquad \Delta; \Phi_2; e_3 \Downarrow \Phi_3; v \qquad \Phi_3(ptr) = o \qquad o = \{[\dots] \dots\} \qquad s \text{ not a property in } o$$

$$o \text{ extensible} \qquad v \text{ is valid } pa \qquad \Phi' = \Phi_3(ptr) = \{[\dots] s : \text{defaultprop}(pa = v), \dots\})$$

$$\Delta; \Phi; e_1 \mid [e_2 \langle pa \rangle = e_3] \Downarrow \Phi'; v$$

$$\frac{\Delta; \Phi; e_1 \Downarrow \Phi_1; ptr \quad \Delta; \Phi_1; e_2 \Downarrow \Phi_2; s \quad \Delta; \Phi_2; e_3 \Downarrow \Phi_3; v \quad \Phi_3(ptr) = o}{o = \{[\dots] \ s : p, \dots\} \quad v \text{ is valid } pa \quad pa \text{ writable in } p \quad \Phi' = \Phi_3(ptr = \{[\dots] \ s : p(pa = v), \dots\}) }{\Delta; \Phi; e_1 \ [e_2 \langle pa \rangle = e_3] \Downarrow \Phi'; v }$$

$$\frac{\Delta;\Phi;e_1 \Downarrow \Phi_1;ptr \qquad \Delta;\Phi_1;e_2 \Downarrow \Phi_2;s}{\Phi_2(ptr) = \{[\dots]s: \{\textbf{configurable}: \textbf{true},\dots\},\dots\} \qquad \Phi' = \Phi_2(ptr = \{[\dots]\dots\})}{\Delta;\Phi;e_1 [\textbf{delete}\ e_2] \Downarrow v;\Phi'}$$

2.3.5 Object attributes

$$\frac{\Delta; \Phi; e \Downarrow ptr; \Phi' \qquad \Phi'(ptr) = \{ [oa:v, \dots] \dots \}}{\Delta; \Phi; e [\langle oa \rangle] \Downarrow v; \Phi'}$$

$$\frac{\Delta; \Phi; e_1 \Downarrow \Phi_1; ptr \quad \Delta; \Phi_1; e_2 \Downarrow \Phi_2; v \quad \Phi_2(ptr) = o \quad o = \{[oa:v', \dots] \dots\}}{v \text{ is valid } oa \quad o \text{ extensible} \quad oa \text{ writable} \quad \Phi' = \Phi_2(ptr = \{[oa:v, \dots] \dots\})}{\Delta; \Phi; e_1 [\langle oa \rangle = e_2] \Downarrow \Phi'; v}$$

2.3.6 Object creation

$$\forall i, \Delta; \Phi_{i-1}; e_i \downarrow \Phi_i; v_i \qquad v_3 \text{ and } v_4 \text{ are bools}$$

$$\overline{\Delta}; \Phi_0; \{ \mathbf{getter} : e_1, \mathbf{setter} : e_2, \mathbf{enumerable} : e_3, \mathbf{configurable} : e_4 \} \Downarrow \Phi_4; \{ \mathbf{getter} : v_1, \mathbf{setter} : v_2, \mathbf{enumerable} : v_3, \mathbf{configurable} : v_4 \}$$

$$\forall i, \Delta; \Phi_{i-1}; e_i \downarrow \Phi_i; v_i \qquad v_2, v_3 \text{ and } v_4 \text{ are bools}$$

$$\overline{\Delta}; \Phi_0; \{ \mathbf{value} : e_1, \mathbf{writable} : e_2, \mathbf{enumerable} : e_3, \mathbf{configurable} : e_4 \} \downarrow \Phi_4; \{ \mathbf{value} : v_1, \mathbf{writable} : v_2, \mathbf{enumerable} : v_3, \mathbf{configurable} : v_4 \}$$

$$\forall i, \Delta; \Phi_{i-1}; e_i \Downarrow \Phi_i; v_1 \qquad \forall i, \Delta; \Phi_{n+i-1}; pe_i \Downarrow \Phi_{n+i}; p_i \qquad oa_1, \dots, oa_n \text{ distinct} \qquad s1, \dots, s_m \text{ distinct} \\ \{\mathbf{proto}, \mathbf{class}, \mathbf{extensible}, \mathbf{code}\} \subseteq \{oa_i : i \in \{1, \dots, n\}\} \qquad \forall i, v_i \text{ is valid } oa_i \qquad ptr \not\in \Phi_{n+m}$$

$$\Delta$$
; Φ ; $\{[oa_1:e_1,\ldots,oa_n:e_n]s_1:pe_1,\ldots,s_m:pe_m\} \ \psi$
 $\Phi_{n+m}(ptr = \{[oa_1:v_1,\ldots,oa_n:v_n]s_1:p_1,\ldots,s_m:p_m\}); ptr$

2.4 Operators

Please note that operators are partial functions: they can be undefined for some inputs. Operators can access the heap (for object-related operators) but cannot modify it. The "otherwise" clauses in the definitions are used when no other clause can be used.

2.4.1 typeof

Consistent with JS typeof on JS primitives (ES5 11.4.3).

```
typeof(\Phi, b) =
                                "boolean"
           typeof(\Phi, n)
                                "number"
           \mathbf{typeof}(\Phi, k) =
                                "int"
            typeof(\Phi, s) =
                                "string"
      typeof(\Phi, undef) =
                                "undefined"
        typeof(\Phi, null) =
                                "null"
     typeof(\Phi, empty)
                                "empty"
\mathbf{typeof}(\Phi, (\Delta; x, \dots; e)) = \mathbf{"function"}
          typeof(\Phi, ptr) = "object"
```

2.4.2 type testing operators

These are redundant (they can be implemented with **typeof**), but are used often and so it is useful to have them.

```
\begin{array}{lcl} \textbf{is-primitive}(\Phi,v) & = & \textbf{true} \text{ if } v \text{ is } b, n, s, \textbf{undef}, \textbf{null} \\ \textbf{is-primitive}(\Phi,v) & = & \textbf{false} \text{ otherwise} \\ \textbf{is-closure}(\Phi,(\Delta;x,\ldots;e)) & = & \textbf{true} \\ \textbf{is-closure}(\Phi,v) & = & \textbf{false} \text{ otherwise} \\ \textbf{is-object}(\Phi,ptr) & = & \textbf{true} \\ \textbf{is-object}(\Phi,v) & = & \textbf{false} \text{ otherwise} \\ \end{array}
```

2.4.3 string operators

```
\begin{array}{rcl} \mathbf{strlen}(\Phi,s) & = & length \ of \ s \\ \mathbf{ntoc}(\Phi,k) & = & one \ character \ string \ with \ code \ k \\ \mathbf{cton}(\Phi, "\mathtt{c"}) & = & character \ code \ of \ c \\ \mathbf{char-at}(\Phi,s,k) & = & kth \ character \ of \ s \\ +_s(\Phi,s_1,s_2) & = & s_1 \ appended \ to \ s_2 \\ <_s(\Phi,s_1,s_2) & = & \mathbf{true} \ if \ s_1 \ precedes \ s_2 \ lexicographically \\ <_s(\Phi,s_1,s_2) & = & \mathbf{false} \ otherwise \end{array}
```

2.4.4 number operators

Number operators work as specified in IEEE 754.

```
\begin{array}{rcl} -(\Phi,n) & = & -n \\ \mathbf{abs}(\Phi,n) & = & \mathrm{abs} \ n \\ \mathbf{floor}(\Phi,n) & = & \mathrm{floor} \ n \\ \mathbf{ceil}(\Phi,n) & = & \mathrm{ceil} \ n \\ +(\Phi,n_1,n_2) & = & n_1+n_2 \\ -(\Phi,n_1,n_2) & = & n_1-n_2 \\ *(\Phi,n_1,n_2) & = & n_1n_2 \\ /(\Phi,n_1,n_2) & = & n_1/n_2 \\ \%(\Phi,n_1,n_2) & = & n_1 \mod n_2 \\ <(\Phi,n_1,n_2) & = & \mathbf{true} \ \mathrm{if} \ n_1 < n_2 \ (\mathrm{IEEE} \ 754) \\ <(\Phi,n_1,n_2) & = & \mathbf{false} \ \mathrm{otherwise} \end{array}
```

2.4.5 integer operators

Bit shifts are defined as in the ECMA specification (ES5 11.7).

```
\begin{array}{rclcrcl} & \sim (\Phi,k) & = & \sim k \\ \& (\Phi,k_1,k_2) & = & k_1\&k_2 \\ & \mid (\Phi,k_1,k_2) & = & k_1\mid k_2 \\ & \smallfrown (\Phi,k_1,k_2) & = & k_1 \smallfrown k_2 \\ << (\Phi,k_1,k_2) & = & k_1 << k_2 \\ >> (\Phi,k_1,k_2) & = & k_1 >> k_2 \\ >>> (\Phi,k_1,k_2) & = & k_1 >>> k_2 \\ >>> (\Phi,k_1,k_2) & = & k_1 >>> k_2 \end{array}
```

2.4.6 to-string

Consistent with ToString on JS primitives (ES5 9.8).

```
\mathbf{to\text{-}string}(\Phi, \mathbf{true}) =
                                          "true"
         to-string(\Phi, false) =
                                          "false"
             to-string(\Phi, n) =
                                          string representation of n
             to-string(\Phi, k) =
                                          string\ representation\ of\ k
              to-string(\Phi, s) =
       to-string(\Phi, undef) =
                                          "undefined"
         to-string(\Phi, null) =
                                          "null"
      \mathbf{to\text{-}string}(\Phi, \mathbf{empty})
                                    =
                                          "empty"
\mathbf{to\text{-string}}(\Phi, (\Delta; x, \dots; e))
                                          "closure"
                                    =
           \mathbf{to\text{-}string}(\Phi, ptr)
                                          "object"
```

2.4.7 to-number

Consistent with ToNumber on JS primitives (ES5 9.3).

```
to-number (\Phi, true)
       to-number(\Phi, false)
                                  =
                                     0
            to-number (\Phi, n)
                                  =
            to-number (\Phi, k)
                                      k as floating point
            to-number (\Phi, s)
                                      s parsed as number
      to-number(\Phi, undef)
                                      NaN
         to-number (\Phi, null)
                                      0
     to-number (\Phi, \mathbf{empty})
                                      NaN
to-number (\Phi, (\Delta; x, \ldots; e))
                                      NaN
          \mathbf{to}-number(\Phi, ptr)
                                      NaN
```

2.4.8 to-int

Floating point to integer conversion is carried out as in ToInt32/ToUint32 (ES5 9.5, 9.6).

```
to-number(\Phi, true)
       to-number(\Phi, false)
                                    0
           to-number (\Phi, n)
                                =
                                    n converted to an integer
           to-number (\Phi, k)
                                    k
           to-number (\Phi, s)
                                    s parsed as number
      to-number(\Phi, undef)
                                    0
        to-number (\Phi, null)
                                = 0
     to-number(\Phi, empty)
                                = 0
to-number (\Phi, (\Delta; x, \ldots; e))
                                = 0
         \mathbf{to}-number(\Phi, ptr) = 0
```

2.4.9 to-boolean

Consistent with ToBoolean on JS primitives (ES5 9.2).

```
to-boolean(\Phi, b) = b
           to-boolean(\Phi, n) = false if n is 0, -0, NaN
           to-boolean(\Phi, n) =
                                   true otherwise
           to-boolean (\Phi, 0)
                              = false
           to-boolean(\Phi, k) = true otherwise
          to-boolean(\Phi,"") = false
           \mathbf{to}-boolean(\Phi, s) = \mathbf{true} otherwise
     to-boolean(\Phi, undef) = false
        to-boolean(\Phi, null)
                               = false
     to-boolean(\Phi, empty)
                               = false
to-boolean(\Phi, (\Delta; x, . . . ; e))
                                   true
         to-boolean(\Phi, ptr)
                                   true
```

2.4.10 strict equality

Consistent with JS strict equality on JS primitives (ES5 11.9.6).

2.4.11 same value

Consistent with JS SameValue algorithm on JS primitives (ES5 9.12).

$$=== (\Phi, l, l) = \mathbf{true}$$

$$=== (\Phi, ptr, ptr) = \mathbf{true}$$

$$=== (\Phi, v_1, v_2) = \mathbf{false} \text{ otherwise}$$

2.4.12 has-own-property

$$\begin{array}{lll} \mathbf{has\text{-}own\text{-}property}(\Phi(ptr=\{[\dots]\,s:p,\dots\}),ptr,s) &=& \mathbf{true} \\ & \mathbf{has\text{-}own\text{-}property}(\Phi(ptr=o),ptr,s) &=& \mathbf{false} \text{ otherwise} \\ \end{array}$$

2.4.13 has-internal

has-internal(
$$\Phi(ptr = \{[i:v,\dots],ptr,"i") = true$$

has-internal($\Phi(ptr = o),ptr,s) = false$ otherwise

2.4.14 is-accessor

```
\begin{array}{lll} \mathbf{is\text{-}accessor}(\Phi(ptr=\{[\dots]\,s:\{\mathbf{getter}:v,\dots\},\dots\}),ptr,s) &=& \mathbf{true} \\ & \mathbf{is\text{-}accessor}(\Phi(ptr=\{[\dots]\,s:p,\dots\}),ptr,s) &=& \mathbf{false} \text{ otherwise} \\ \end{array}
```