

Semantic Search for Quantity Expressions

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Overview

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- ▶ Motivation: Problem and State Of The Art

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- ▶ Our Approach: Structure Of The Search Engine

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- ▶ The Implementation
- ▶ Time for Questions

Motivation (1)

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- ▶ everything is quantified

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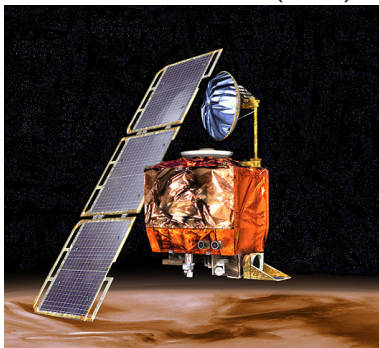
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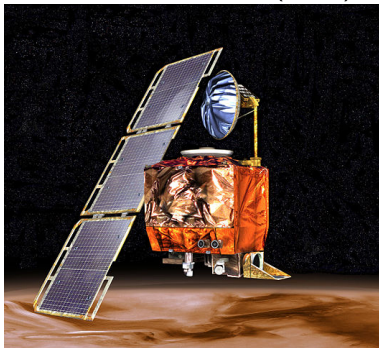
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- ▶ Different Units are a big problem

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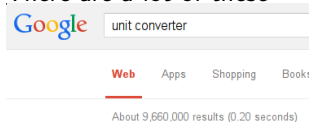
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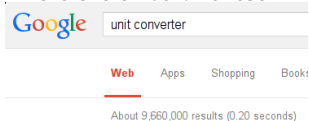
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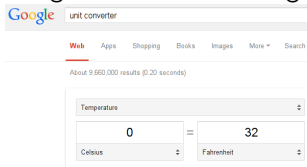


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- ▶ Google itself has one integrated



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- ▶ This is the kind of search engine we have built

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- ▶ Spotter is done by *Stiv Sherko*
- ▶ We only need to worry about the *Unit System*, the *Search Algorithm* and the *Frontend*

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- ▶ so we have 9 basic dimensions

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- ▶ We can use this to get a meta-mathematical formalisation of dimensions

Our Approach: The Unit System (3)

Dimension		
dimension	:	type
none	:	dimension
count	:	dimension
length	:	dimension
mass	:	dimension
time	:	dimension
current	:	dimension
temperature	:	dimension
luminous	:	dimension
amount	:	dimension
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- ▶ this results in the following formalisation:

Our Approach: The Unit System (5)

Quantity Expression	
QE	: dimension \rightarrow type
QENMul	: $\forall x : \text{dimension}. \text{number} \rightarrow \text{QE}(x) \rightarrow \text{QE}(x)$
QENDiv	: $\forall x : \text{dimension}. \text{QE}(x) \rightarrow \text{number} \rightarrow \text{QE}(x)$
QEMul	: $\forall x : \text{dimension}. \forall y : \text{dimension}. \text{QE}(x) \rightarrow \text{QE}(y)$
QEAdd	: $\forall x : \text{dimension}. \text{QE}(x) \rightarrow \text{QE}(x) \rightarrow \text{QE}(x)$
QEDiv	: $\forall x : \text{dimension}. \forall y : \text{dimension}. \text{QE}(x) \rightarrow \text{QE}(y)$