Semantic Search for Quantity Expressions

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Motivation: Problem and State Of The Art

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- Our Approach: Structure Of The Search Engine

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- ► Time for Questions

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- everything is quantified

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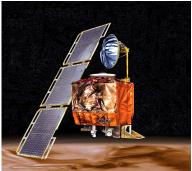
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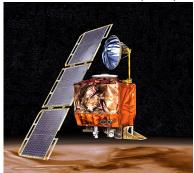
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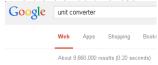
Different Units are a big problem



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- This is the kind of search engine we have built

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- ► For the first two points, we use a meta-mathematical approach

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- MMT is a software that allows us to make use of these concepts
- ► It is easy to write down your own theories and related them with views



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- ▶ We can use this to get a *Theory of Dimensions*:

Dimension		
dim	:	type
none	:	dim
count	:	dim
length	:	dim
mass	:	dim
time	:	dim
current	:	dim
temperature	:	dim
luminous	:	dim
amount	:	dim
•	:	$dim \to dim \to dim$
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 - 6. The *quotient* of two existing QEs such as $1 \frac{\text{Meter}}{\text{Second}}$

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 - 5. The sum of two existing QEs (of the same dimension)
 - 6. The quotient of two existing QEs such as $1 \frac{Meter}{Second}$
- ▶ this results in the following *Theory of Quantity Expressions*:

Quantity Expression		
import Dimension		
QE	:	dim o type
QENMul	:	$\forall x: dim.\mathbb{R} o QE\left(x ight) o QE\left(x ight)$
QENDiv	:	$orall x: dim.QE\left(x ight) ightarrow \mathbb{R} ightarrow QE\left(x ight)$
QEAdd	:	$\forall x : dim.QE(x) \to QE(x) \to QE(x)$
QEMul	:	$\forall x, y : dim.QE\left(x\right) \to QE\left(y\right) \to QE\left(x \cdot y\right)$
QEDiv	:	$\forall x, y : dim.QE\left(x\right) o QE\left(y\right) o QE\left(rac{x}{y} ight)$

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Non SI Lengths
import Quantity Expression
Thou: QE (length)
Foot = QENMul (1000, Thou)
Yard = QENMul (3, Foot)
Chain = QENMul (22, Yard)
Furlong = QENMul (10, Chain)
Mile = QENMul (8, Furlong)
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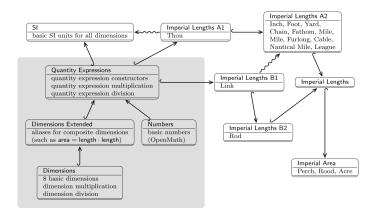
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- ▶ We have a big (easily extensible) theory graph of unit theories
- ▶ Here is a small part of it



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- and then have an efficient index

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The Implementation

► TODO

Time for Questions

Thank You For Listening