Tutorial on the TLA+ language and its support tools: Apalache

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TLA⁺ Community Meeting 2023

April 22, 2023





Apalache

Symbolic model checker for TLA+

apalache.informal.systems

bounded number of integer constants is OK

Symbolic model checker that works under the assumptions of TLC:

Fixed and finite constants (parameters)

Finite sets, function domains and co-domains

TLC's restrictions on formula structure

Bounded model checking to check safety

As few language restrictions as possible

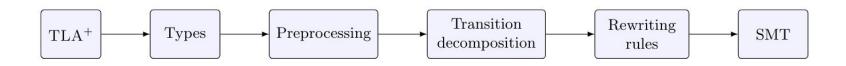
Technically,

Quantifier-free formulas in SMT:

QF_UFNIA

Unfolding quantified expressions:

 $\forall x \in S: P \text{ as } \bigwedge_{c \in S} P[c/x]$





Running example ERC20 Tokens



ERC20

ethereum.org/en/developers/docs/standards/tokens/erc-20/

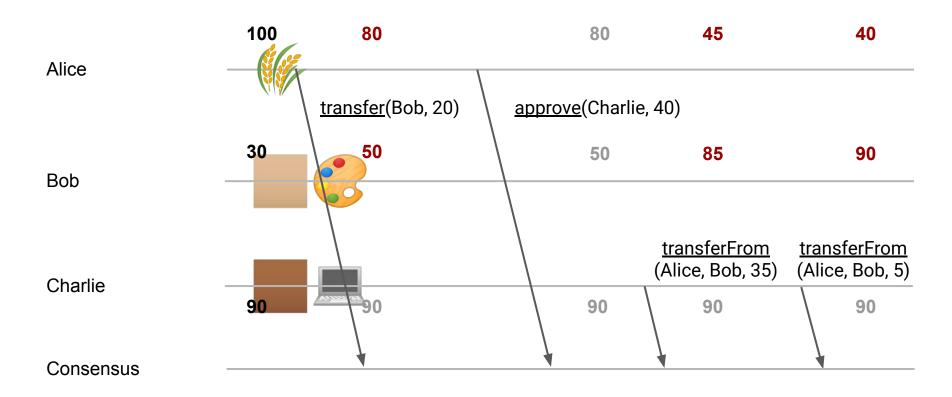
A foundational Solidity API for virtually all tokens running on Ethereum

Incorrect use leads to security issues

- Similar interfaces in Cosmos:
 - The bank module in Cosmos SDK in Golang
 - CW20: Cosmwasm contracts in Rust
 - ICS20: token transfer between Cosmos blockchains crossplatform

Can we do anything useful about it with TLA+?

ERC20 as diagrams (happy paths)



Step 1

Specifying the contract without specifying a state machine



Preambule

----- MODULE erc20 -----

EXTENDS Integers, Apalache, erc20_typedefs

CONSTANTS

* @type: Set(ADDR);

AllAddresses,

* @type: Int;

MAX_UINT

* The special address 0x0 in EVM

ZERO_ADDRESS \(\text{"0_OF_ADDR"} \)

ASSUME(ZERO_ADDRESS ∈ AllAddresses)

* The predicate that we use

* to check for overflows.

* In EVM, MAX_UINT = 2^{256} - 1

 $isUint(i) \triangleq 0 \leq i \land i \leq MAX_UINT$

Let's talk about types later

Contract constructor

```
\* @type: (ADDR, Int) => $state;
newErc20(sender, initialSupply) ≜ [
 balanceOf → [ a ∈ AllAddresses →
  IF a ≠ sender THEN 0 ELSE initialSupply
 totalSupply → initialSupply,
 allowance \rightarrow [a, b \in AllAddresses \rightarrow 0],
 owner → sender
```

Specifying transfer

```
\* @type: ($state, ADDR, ADDR, Int) => $result;
LET fromBalance ≜ state.balanceOf[fromAddr] IN
 I FT err ≜
 CASE ¬(fromAddr ≠ ZERO_ADDRESS) →
    "FRC20: transfer from the zero address"
  □¬(toAddr ≠ ZERO_ADDRESS) →
    "ERC20: transfer to the zero address"
   \Box \neg (fromBalance \ge amount) \rightarrow
    "FRC20: transfer amount exceeds balance"
  □ OTHER → ""
 IN
```

```
IF err ≠ "" THEN Error(err)
ELSE
 LFT newBalances ≜
   IF fromAddr = toAddr
   THEN state.balanceOf
   ELSE state.balanceOf EXCEPT
      ![fromAddr] = fromBalance - amount,
      ![toAddr] = @ + amount]
 IN
Ok(TRUE,
    state EXCEPT !.balanceOf = newBalances |)
      overflows?
```

Step 2

Simple state machine to model check



State machine to model check

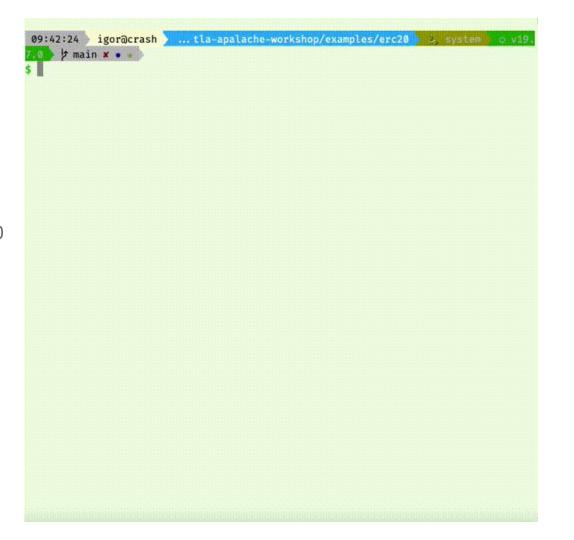
```
\* invoke only 'transfer' with various inputs
----- MODULE erc20 tests -----
                                                      Next1 ≜
AllAddresses ≜ { "0_OF_ADDR", "alice_OF_ADDR",
                                                        \exists sender, to Addr \in All Addresses:
                 "bob_OF_ADDR", "eve_OF_ADDR" }
                                                         ∃ amount ∈ AMOUNTS:
MAX_UINT \triangleq 2^{256} - 1
                                                          fromResult(transfer(state,
AMOUNTS ≜ 0..MAX_UINT
                                                           sender, toAddr, amount))
INSTANCE erc20
VARIABLE \* @type: $state;
                                                      \* @type: $result => Bool;
 state
                                                      fromResult(result) ≜
Init ≜
                                                        ∧ VariantTag(result) = "Ok"
 ∃ sender ∈ AllAddresses \ { ZERO_ADDRESS }:
                                                        ∧ VariantGetUnsafe("Ok", result).returnedTrue
  \exists initialSupply \in AMOUNTS:
                                                        ∧ state' = VariantGetUnsafe("Ok", result).state
   state = newErc20(sender, initialSupply)
```

Running Apalache

Check for 10 steps:

zeroAddressInv ≜

state.balanceOf[ZERO_ADDRESS] = 0



Bounded model checking

Input: Init, Next and Inv

- 0. Init $\wedge \neg Inv$
- 1. (Init·Next) ∧ ¬Inv'
- 2. (Init·Next·Next) $\land \neg Inv'$

. . .

k. (Init·Next·...·Next) ∧ ¬Inv'

Backend:

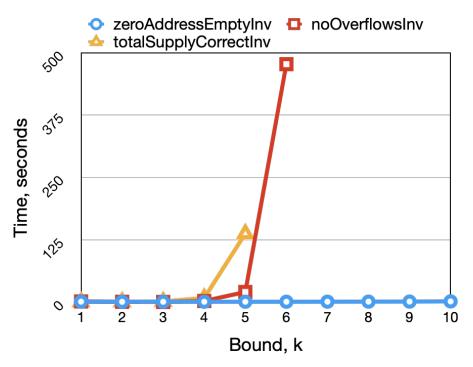


k is the bound

Checking other invariants

```
\* @type: (ADDR -> Int) => Int;
sumOverBalances(balances) ≜
LET \* @type: (Int, ADDR) => Int;
Add(sum, addr) ≜ sum + balances[addr]
IN
ApaFoldSet(Add, 0, DOMAIN balances)
```

```
totalSupplyInv ≜ state.totalSupply = sumOverBalances(state.balanceOf)
```



noOverflowInv ≜

∧ isUint(state.totalSupply)

 $\land \forall a \in DOMAIN$ state.balanceOf: isUint(state.balanceOf[a])

 $\land \forall p \in DOMAIN$ state.allowance: isUint(state.allowance[p])

Step 3

Understanding the underlying techniques



Translation to SMT

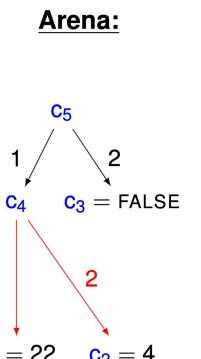
Mimic the semantics implemented by TLC (explicit model checker)

Compute layout of data structures, constrain contents with SMT

Define operational semantics via reduction rules (for bounded data structures)

Trade efficiency for expressivity

Static picture of TLA⁺ values and relations between them



SMT:

integer sort Int

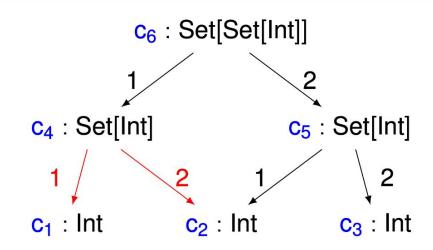
Boolean sort Bool

name, e.g., "abc", uninterpreted sort

finite set:

- a constant c of uninterpreted sort $set_{ au}$
- propositional constants for members $in_{\langle c_1,c \rangle}, \ldots, in_{\langle c_n,c \rangle}$

Arenas for sets: { { 1, 2 }, { 2, 3} }



SMT defines the contents, e.g., to get {{1}, {2}}:

$$in_{\langle c_1, c_4 \rangle} \wedge \neg in_{\langle c_2, c_4 \rangle} \wedge in_{\langle c_2, c_5 \rangle} \wedge \neg in_{\langle c_3, c_5 \rangle}$$
 [OOPSLA'19]

What about integers?

TLA⁺

```
isUint(i) \triangleq 0 ≤ i \land i ≤ MAX_UINT isUint(state.totalSupply)
```

SMT

```
(and (<= 0 c_i) (<= c_i c_MAX_UINT))
```

TLA⁺

```
\* @type: (ADDR -> Int) => Int;
sumOverBalances(balances) ≜
 LET \* @type: (Int, ADDR) => Int;
  Add(sum, addr) ≜ sum + balances[addr]
 IN
 ApaFoldSet(Add, 0, DOMAIN balances)
SMT (after removing duplicates)
(= c_0 0)
(= c_1 (+ c_0 (ite in_1_s 1 0)))
(= c_n (+ c_{n-1}) (ite in_n \le 1 \ 0)))
```

Alternative encoding

Using SMT arrays for TLA⁺ sets and functions: QF_AUFNIA

- Rodrigo Otoni, IK, J. Kukovec, P. Eugster, N. Sharygina

Symbolic Model Checking for TLA+ Made Faster [TACAS'23]

(See the talk by Rodrigo on Thursday!)

Working faster on classical fault-tolerant algorithms

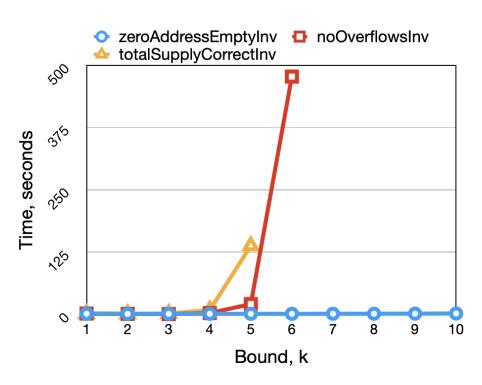
Step 4 Inductive reasoning



What value of *k* is convincing?

Improve the model checker,
 get stuck at larger k

Alternative: inductive reasoning



Checking invariants in one step

```
initArbitrary ≜
 ∃ owner ∈ AllAddresses \ { ZERO_ADDRESS }:
  \exists balances \in [AllAddresses \rightarrow Int]:
   ∃ allowances ∈
     [ AllAddresses × AllAddresses → Int ]:
    A state = [balanceOf → balances,
       totalSupply → sumOverBalances(balances),
       allowance → allowances,
       owner → owner
    ∧ isValid
isValid ≜
totalSupplyInv ∧ zeroAddressInv ∧ noOverflowInv
```

```
$ apalache-mc check \
  --init=initArbitrary \
  --next=Next1 --inv=isValid \
  --length=1 erc20_tests.tla
$ V in 2 seconds
$ apalache-mc check \
  --init=Init \
  --next=Next1 --inv=isValid \
  --length=0 erc20_tests.tla
     in 2 seconds
```

Checking the postcondition

```
transferPrePost \( \text{\Left} \)
 ∃ sender toAddr ∈ AllAddresses:
  LET ob ≜ state.balanceOf IN
  LET nb ≜ state'.balanceOf IN
    \wedge V sender = toAddr \wedge nb = ob
      V ∧ sender ≠ toAddr
        \land nb[sender] \leq ob[sender]
        \land nb[toAddr] \ge ob[toAddr]
        ∧ nb[toAddr] - ob[toAddr] = ob[sender] - nb[sender]
        \land \forall a \in AllAddresses:
            a \notin \{ \text{ sender, toAddr} \} \Rightarrow \text{nb[a]} = \text{ob[a]}
    ∧ state'.allowance = state.allowance
    ∧ state'.owner = state.owner
    ∧ state'.totalSupply = state.totalSupply
```

```
$ apalache-mc check \
--init=initArbitrary \
--next=Next1 \
--inv=transferPrePost \
--length=2 erc20_tests.tla

$ ✓ in 2 seconds
```

Step 5

Specifying approve and transferFrom



Specifying approve

```
\* @type: ($state, ADDR, ADDR, Int) => $result;
approve(state, sender, spender, amount) ≜
 LET err ≜
 CASE ¬(sender ≠ ZERO_ADDRESS) →
    "ERC20: transfer from the zero address"
   □¬(spender ≠ ZERO_ADDRESS) →
    "ERC20: transfer to the zero address"
   □ OTHER → ""
 IN
```

Specifying transferFrom

```
\* @type: ($state, ADDR, ADDR, ADDR, Int) => $result;
transferFrom(state, sender, fromAddr, toAddr, amount) \(\text{\Reg}\)
                                                           LET updatedState ≜
 LET currentAllowance ≜
                                                             IF currentAllowance = MAX_UINT
  state.allowance[fromAddr, sender] IN
                                                             THFN state
 LET err ≜
                                                             ELSE | state EXCEPT
  CASE ¬(currentAllowance ≥ amount) →
                                                               !.allowance[fromAddr, sender] = @ - amount
     "ERC20: insufficient allowance"
   □ ¬(fromAddr ≠ ZERO_ADDRESS) →
     "ERC20: approve from the zero address"
                                                            IN
   □¬(toAddr ≠ ZERO_ADDRESS) →
                                                            IF err ≠ ""
     "ERC20: approve to the zero address"
                                                            THEN Error(err)
   □ OTHER → ""
                                                            ELSE transfer(updatedState,
 IN
                                                                          fromAddr, toAddr, amount)
                Since 'transfer' is not an action.
                composition is easy
```

Checking the inductive invariant

```
$ apalache-mc check --init=initArbitrary --next=Next --inv=isValid \
--length=1 erc20_tests.tla

$ ✓ in 3 seconds
```

\$ apalache-mc check --init=Init --next=Next --inv=isValid \
 --length=0 erc20_tests.tla

\$ V in 2 seconds

Step 7 Type definitions



Type definitions

```
----- MODULE erc20_typedefs -----
EXTENDS Variants
(* Type definitions for ERC20.
  ADDR is an uninterpreted type representing
  an account address.
 // A state of an ERC20 contract/token
 @typeAlias: state = {
  balanceOf: ADDR -> Int.
  totalSupply: Int,
  allowance: <<ADDR, ADDR>> -> Int,
  owner: ADDR
```

```
(* The result of applying an ERC20 method
  @typeAlias: result =
    Error(Str)
   | Ok({ returnedTrue: Bool, state: $state }); *)
erc20_typedefs ≜ TRUE
\* A convenience operator for constructing an Error
\* @type: Str => $result;
Error(msg) ≜ Variant("Error", msg)
\* A convenience operator for constructing an Ok result
\* @type: (Bool, $state) => $result;
Ok(returnedTrue, state) ≜
  Variant("Ok",
   [returnedTrue \rightarrow returnedTrue, state \rightarrow state])
```

Type checker Snowcat



- Damas & Milner type inference + row types (no inductive types)
- Resolving type imprecision between function-like types
- May require type annotations for records, tuples, functions, and sequences

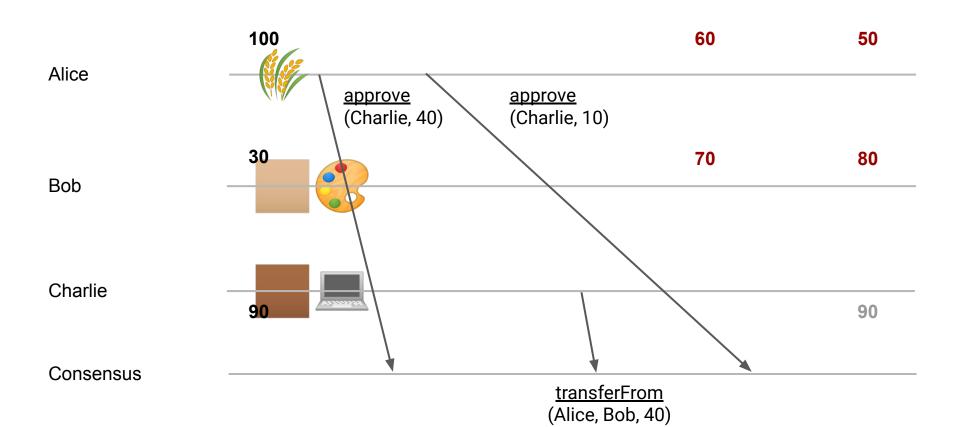
Int	Bool	Str
UNINTERPRETED	Set(a)	Seq(a)
a -> b	< <a, b,="" c="">></a,>	
{ f1: a, f2: b, f3: c }	Tag1(a) Tag2(b) Tag3(c)	(a, b, c) => d

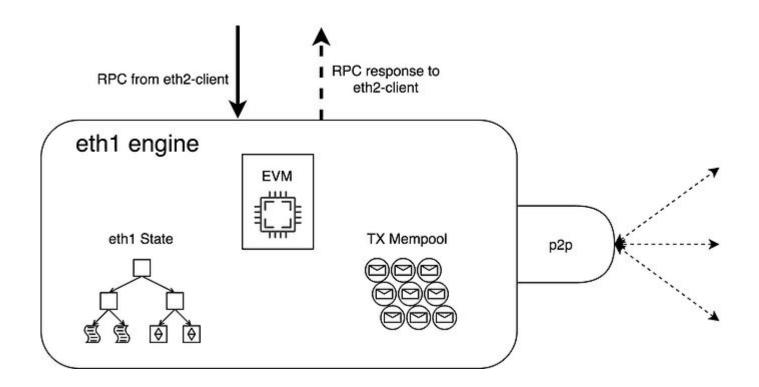
apalache.informal.systems/docs/tutorials/snowcat-tutorial.html

Step 6 Specifying mempool



Revisit the diagram: an unhappy path





Source: ethereum.org/en/developers/docs/networking-layer/

docs.openzeppelin.com/contracts/4.x/api/token/erc20#IERC20

approve(address spender, uint256 amount) → bool

external #

Sets amount as the allowance of spender over the caller's tokens.

Returns a boolean value indicating whether the operation succeeded.

A IMPORTANT

Beware that changing an allowance with this method brings the risk that someone may use both the old and the new allowance by unfortunate transaction ordering. One possible solution to mitigate this race condition is to first reduce the spender's allowance to 0 and set the desired value afterwards: https://github.com/ethereum/EIPs/issues/20#issuecomment-263524729



3sGgpQ8H commented on Nov 29, 2016 • edited >

Attack vector on ERC20 API (approve/transferFrom methods) and suggested improvements:

https://docs.google.com/document/d/1YLPtQxZu1UAvO9cZ1O2RPXBbT0mooh4DYKjA_jp-RLM/ (commenting enabled)





States & tx submission

```
----- MODULE erc20_mempool -----
... \* skipping the constant definitions
INSTANCE erc20
VARIABLES
 \* @type: $state;
 contractState,
 \* @type: Set($tx);
 mempool,
 \* @type: $tx;
 lastTx,
 \* @type: Str;
 lastTxStatus
```

```
submit(tx) ≜
 \land mempool' = mempool \cup { tx }
 \land lastTx' = tx
 ∧ lastTxStatus' = "pending"
 ∧ UNCHANGED contractState
```

Committing

```
\* @type: $tx => Bool;
commit(tx) ≜
 \land mempool' = mempool \land { tx }
 \land \lor \land \lor VariantTag(tx) = "TransferTx"
    ∧ LET ttx ≜
        VariantGetUnsafe("TransferTx", tx) IN
      LET res ≜
        transfer(contractState, ttx.sender, ___
                 ttx.toAddr, ttx.amount) IN
      fromResult(tx, res) _
   \vee \wedge VariantTag(tx) = "ApproveTx"
    ∧ ... \* similar to TransferTx
   V ∧ VariantTag(tx) = "TransferFromTx"
    ∧ ... \* similar to TransferTx
```

```
\* boilerplate to propagate the result
\* @type: ($tx, $result) => Bool;
fromResult(tx, result) ≜
 \land lastTx' = tx
 ∧ IF VariantTag(result) ≠ "Error"
  THEN
    ∧ lastTxStatus' = "success"
    ∧ contractState' =
      VariantGetUnsafe("Ok", result).state
  ELSE
    ∧ lastTxStatus' =
      VariantGetUnsafe("Error", result)
    ∧ UNCHANGED contractState
```

Exactly the definition from erc20!

Initialization + Transitions

```
Init ≜
                                                     Next ≜
 ∧ ∃ sender ∈ AllAddresses \ { ZERO_ADDRESS }:
                                                      \* execute the contract methods
                                                      ∃ sender ∈ AllAddresses:
    \exists initial Supply \in AMOUNTS:
    contractState = newErc20(sender, initialSupply)
                                                       ∃ amount ∈ AMOUNTS:
                                                         V ∃ toAddr ∈ AllAddresses:
 \land mempool = \{\}
 \Lambda lastTx = NoneTx
                                                           submit(TransferTx(sender, toAddr, amount))
 ∧ lastTxStatus = ""
                                                        V ∃ spender ∈ AllAddresses:
                                                           submit(ApproveTx(sender, spender, amount))
                                                         V ∃ fromAddr, toAddr ∈ AllAddresses:
                                                           submit(TransferFromTx(sender, fromAddr,
                                                                                   toAddr, amount))
                                                         \lor \exists tx \in mempool:
                                                           commit(tx)
```

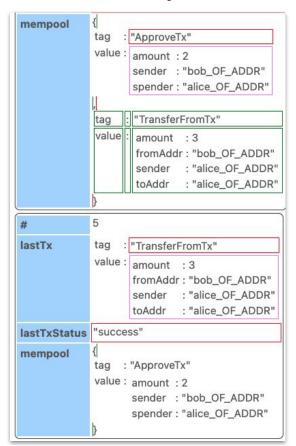
Expectation as an invariant

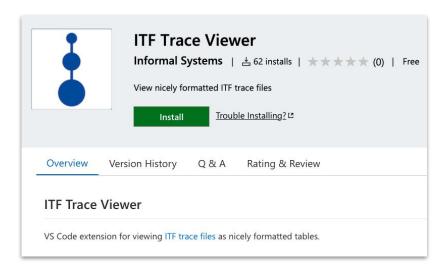
```
noTransferFromWhileApproveInFlight \( \Delta \)
 LET Violation ≜
  ∧ lastTxStatus = "success"
  ∧ VariantTag(lastTx) = "TransferFromTx"
  ∧ LET ltx ≜ VariantGetUnsafe("TransferFromTx", lastTx) IN
    \wedge ltx.amount > 0
    \land \exists tx \in mempool:
       ∧ VariantTag(tx) = "ApproveTx"
       ∧ LET atx ≜ VariantGetUnsafe("ApproveTx", tx) IN
         \land atx.sender = ltx.fromAddr \land atx.spender = ltx.sender
         \wedge atx.amount < ltx.amount \wedge atx.amount > 0
 IN
 ¬Violation
```

\$ apalache-mc check \
--inv=noTransferFromWhileApproveInFlight \
erc20_mempool.tla

\$ X in 3 seconds

Counterexample





by Hernan Vanzetto @ Informal

ITF: Informal Trace Format

- TLA⁺ traces in JSON
- Every engineer can parse JSON
- Extremely simple format
- Designed for tool integration

```
"#meta": {
 "format": "ITF",
 "varTypes": {
"vars": [ "lastTx", "mempool", ... ],
"states": [ {
 "#meta": { "index": 0 },
 "lastTxStatus": "",
 "mempool": { "#set": [ ] },
 "contractState": {
  "allowance": {
   "#map": [
      { "#tup": [ "alice_OF_ADDR", "0_OF_ADDR" ] },
```

Step 7 Discussion



Functional operator composition

We rarely see it in TLA⁺ specs

```
transferFrom(state,
sender, fromAddr, toAddr, amount) ≜
...

IF err ≠ ""

THEN Error(err)

ELSE transfer(updatedState,
fromAddr, toAddr, amount)
```

- ERC20 is closer to the original contract easier to match the code
- Composition F(G(x)) does not require the \cdot operator: $A \cdot B$
- Easier to reuse in other specs, as we have seen in the mempool example

- The logic of TLA⁺ supports this kind of modeling too

Protocol designers

- Onboarding is not too hard
- ✓ Happy to see counterexamples
- Check state invariants with Apalache
- Longer executions? No time for inductive invariants
- Apalache is slow—
- Antipatterns
- Randomized symbolic execution
- Parallel execution in the cloud



apalache.informal.systems

Apalache

The Symbolic Model Checker for TLA+

View the Project on GitHub

informalsystems/apalache

Download ZIP File Download TAR Ball GitHub





OWTOs/ho...

Apalache: symb... @A... · Sep 7, 2022



1

You were asking for precise type checking of @tlaplus records in Apalache, a lot. Since yesterday (v0.29.0), it is the default. We will keep the old records for backwards compatibility till October 30, 2022. How to transition to new records and variants: apalache.informal.systems/docs/H

Apalache: symbolic model





Features • Installation • Manual • Releases • Chat • Contribute

Apalache translates TLA+ into the logic supported by SMT solvers such as Microsoft Z3. Apalache can check inductive invariants (for fixed or bounded parameters) and check safety of bounded executions (bounded model checking). To see the list of supported TLA+ constructs, check the supported features. In general, Apalache runs under the same assumptions as TLC.

To learn more about TLA+, visit Leslie Lamport's page on TLA+ and see his video course. Also, check out TLA+ language manual for engineers.

Tutorials

- Type checking TLA+ with Snowcat
- · Extended version of the Apalache tutorial

Talks

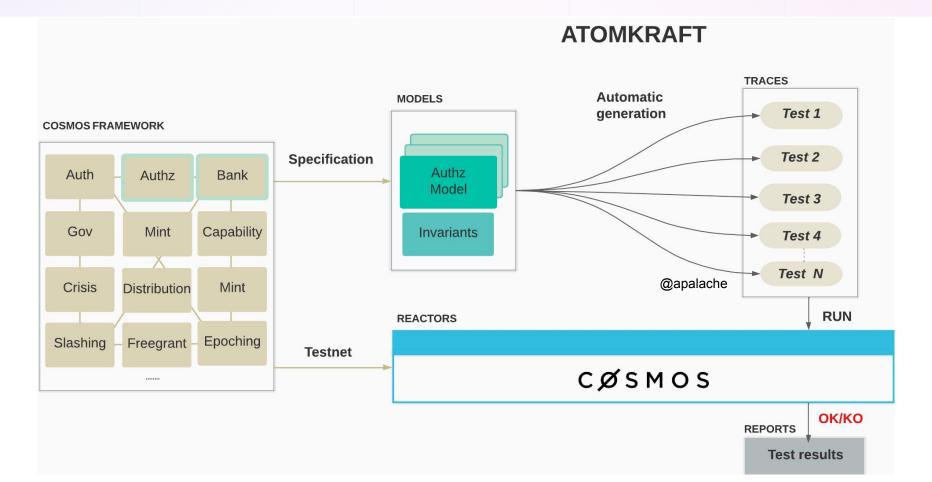
- Informal Systems Tutorial: TLA+ Basics
- Extended version of the Apalache tutorial. TLA+ tutorial at DISC 2021 (October 2021).
- How TLA+ and Apalache Helped Us to Design the Tendermint Light

Model-based testing

```
€ ○ ○ ○ ① □ …
 model > = hanoi.tla > {} hanoi
       Udit Gulati, 2 months ago | 1 author (Udit Gulati)
                                  Udit Gulati, 2 months ago - check if model file exists
       ---- MODULE hanoi ----
                                                                                        Tenanger ....
       EXTENDS Apalache, Integers, Sequences, SequencesExt
                                                                                        COLUMN TWO
                                                                                         100.000
       VARIABLES
           \* @type: Seq(Seq(Int));
           hanoi,
           \* @type: {tag: Str, source: Int, target: Int};
           action
       M DICC -- 2
                                                                       | | bash + ∨ | | | | | | | ··· ^ ×
 PROBLEMS (1) OUTPUT
                                  GITLENS
                        TERMINAL
                                            DEBUG CONSOLE
 modelator/examples/hanoi on 7 dev [!?] is 📦 v0.1.0 via 🐍 v3.10.10
o at 21:29:30 >
```



Automatic generation/execution of test suites



Appendix Symbolic simulation



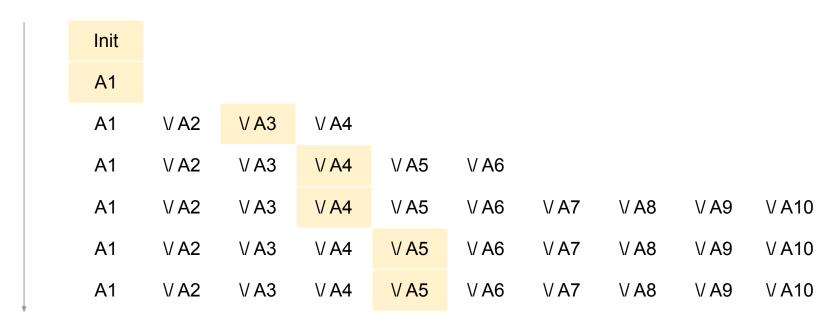
Bounded model checking: Agreement

decisions = { v0, v1 }	32 CPUs/cloud ⇒ 1 min
UponProposalInPrecommitNoDecision	1 CPU ⇒ 6 min 25 sec
UponProposalInPrevoteOrCommitAndPrevote	3 correct, 2 faulty
UponProposalInPrecommitNoDecision	
UponProposalInPrevoteOrCommitAndPrevote	32 CPUs/cloud ⇒ 43 sec
UponProposalInPropose	1 CF 0 → 2 IIIII 32 Sec
UponProposalInPropose	1 CPU ⇒ 2 min 52 sec
Init	2 correct, 2 faulty:

Why slow down?

Init									
A1									
A1	VA2	∨ A3	VA4						
A1	VA2	V A 3	VA4	V A 5	V A 6				
A1	VA2	V A 3	VA4	V A 5	V A6	V A7	V A8	V A 9	V A10
A1	VA2	V A 3	VA4	V A 5	V A6	V A7	V A8	V A 9	V A10
A1	V A2	V A 3	VA4	V A 5	V A 6	V A7	VA8	V A 9	V A10

Randomized symbolic execution



¬Invariant

Is it better?

- Run 20 experiments for Agreement on n = 4, f = 2 with hyperfine:

31.340 s ± 24.897 s

vs 172 s in non-randomized

- In practice, it finds violations faster

- (No large scale experiments though)

What guarantees do we have?