APPENDICES BOOKLET

CONTENTS

Auckland Rental Data

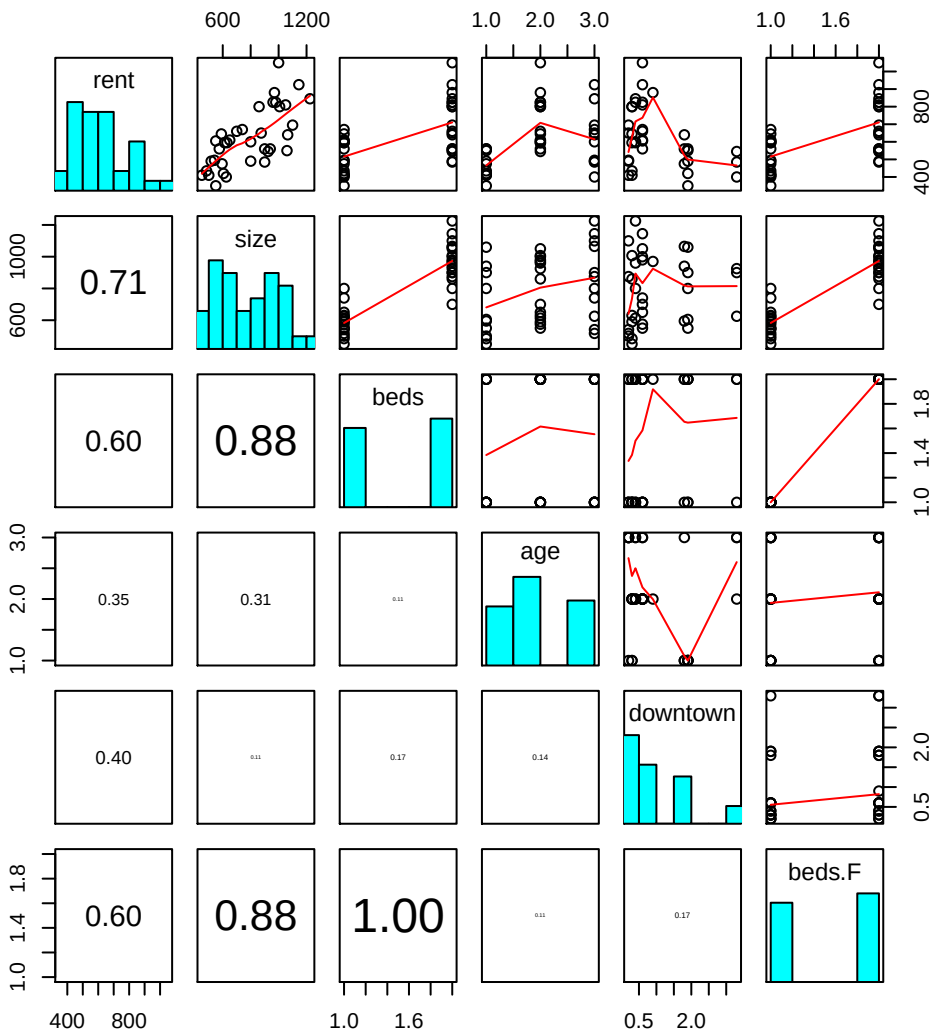
Data were collected on the monthly rental and other characteristics of 36 randomly selected apartments in Auckland. We wish to build a model to explain the monthly rental of an apartment. The variables measured were

`rent`	The monthly rental (in NZ$)
`size`	The apartment size (in square feet)
`beds`	The number of bedrooms (either 1 or 2)
`age`	The age of the apartment building (`new`, `recent`, or `old`)
`downtown`	The distance from the city centre (in miles)

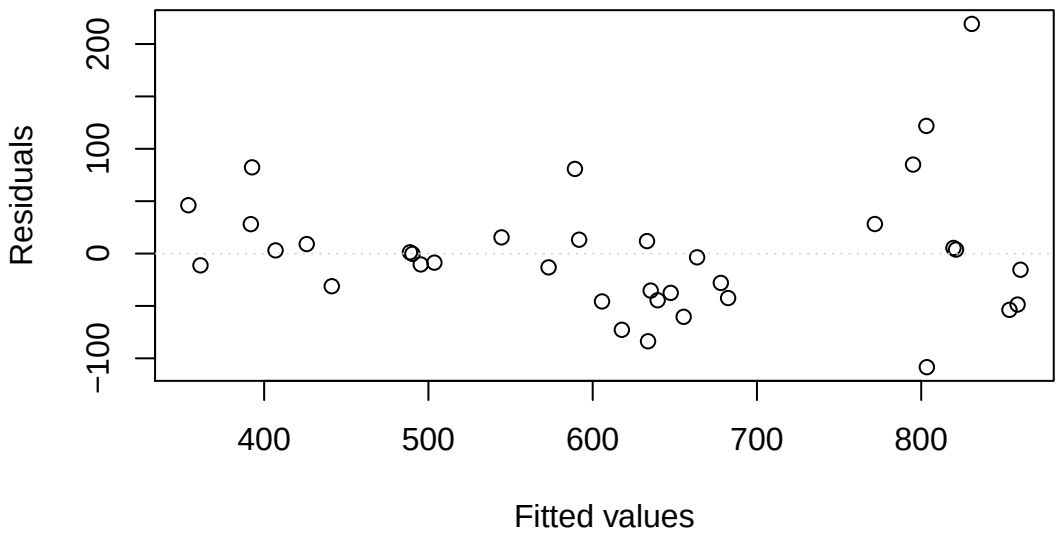
```
> ## Printing the first six observations.
> head(rent.df)
  rent size beds age downtown
1  810 1050    2 Old      0.6
2  560  575    1 Old      0.6
3  550 1060    2 New      1.9
4  610  650    1 Old      0.6
5  800 1007    2 Old      0.3
6  435  484    1 New      0.3
```

```
> rent.df = within(rent.df, {
+     beds.F = factor(beds)
+ })
> summary(rent.df$age)
   New    Old Recent
    10     15     11
> summary(rent.df$size)
   Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
  450.0   593.8   800.0   791.0   972.5  1225.0
> summary(rent.df$downtown)
   Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
 0.2000  0.3000  0.6000  0.9861  1.8000  3.3000
```

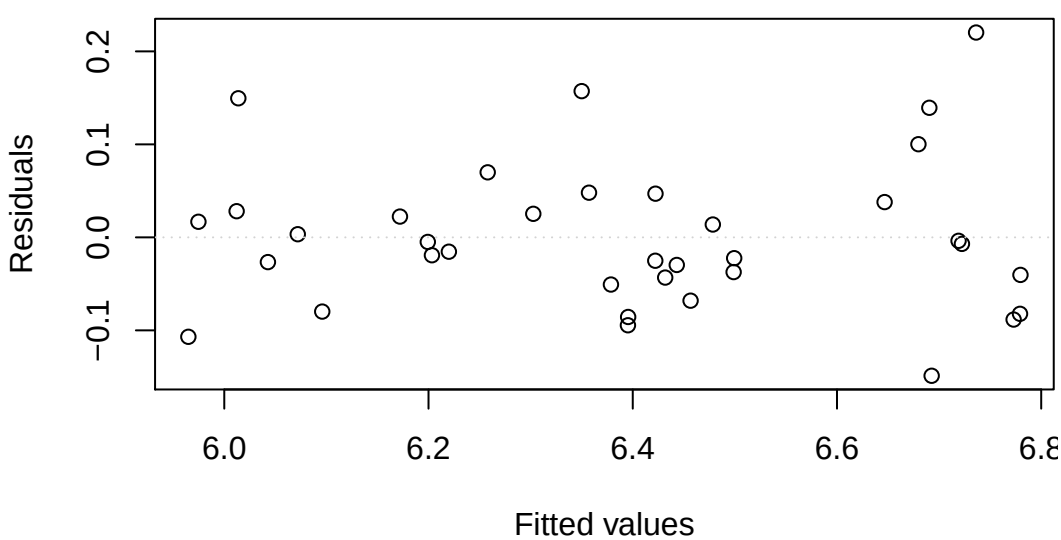
```
> pairs20x(rent.df)
```



```
> rent1.fit=lm(rent ~ size + downtown + beds.F + age,
+              data = rent.df)
> eovcheck(rent1.fit)
```

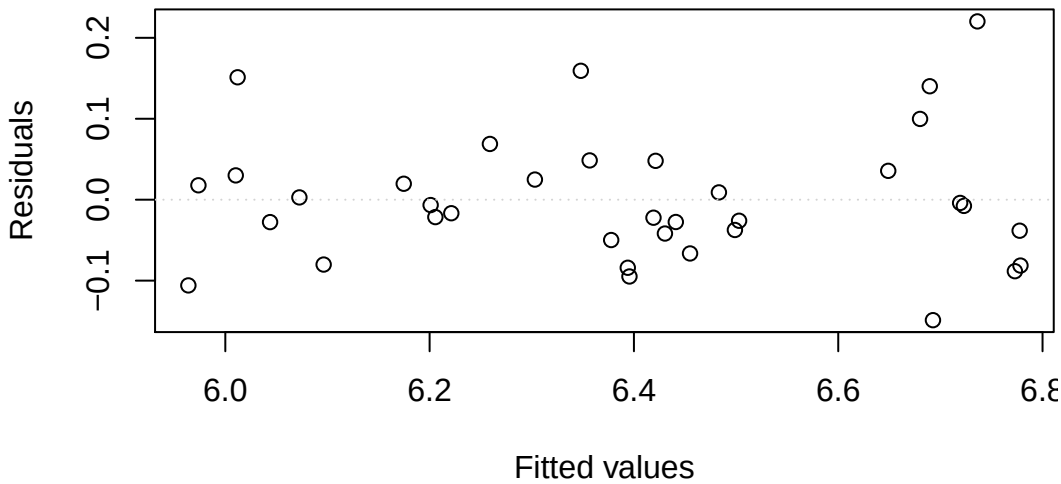



```
> rent2.fit=lm(log(rent) ~ size + downtown + beds.F + age,
+              data = rent.df)
> eovcheck(rent2.fit)
```

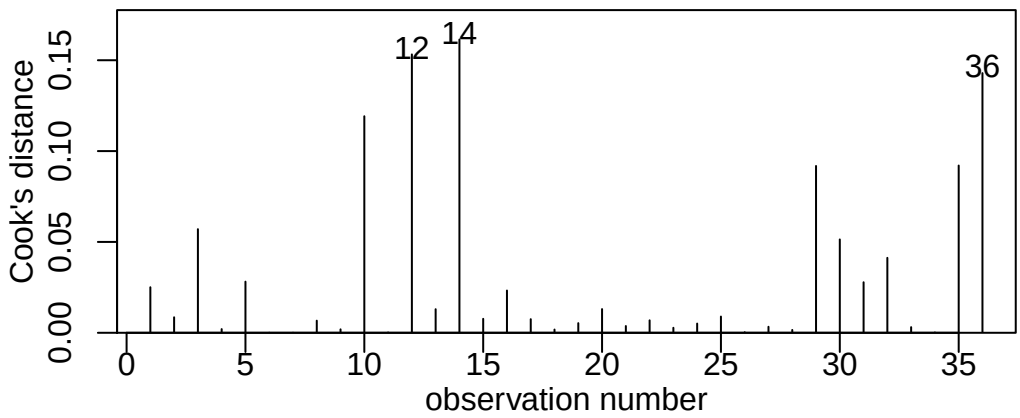


```
> summary(rent2.fit)

Call:
lm(formula = log(rent) ~ size + downtown + beds.F + age, data = rent.df)

Residuals:
     Min       1Q   Median       3Q      Max
-0.14881 -0.04509 -0.01117  0.03061  0.22029

Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)  5.6866876  0.0919170  61.868  < 2e-16 ***
size         0.0008595  0.0001548   5.551 4.92e-06 ***
downtown    -0.1024085  0.0168748  -6.069 1.15e-06 ***
beds.F2     -0.0076631  0.0657676  -0.117   0.9080
ageOld       0.2591978  0.0385543   6.723 1.89e-07 ***
ageRecent    0.0887542  0.0430398   2.062   0.0479 *
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.08653 on 30 degrees of freedom
Multiple R-squared:  0.9104,Adjusted R-squared:  0.8955
F-statistic: 60.98 on 5 and 30 DF,  p-value: 8.289e-15
```

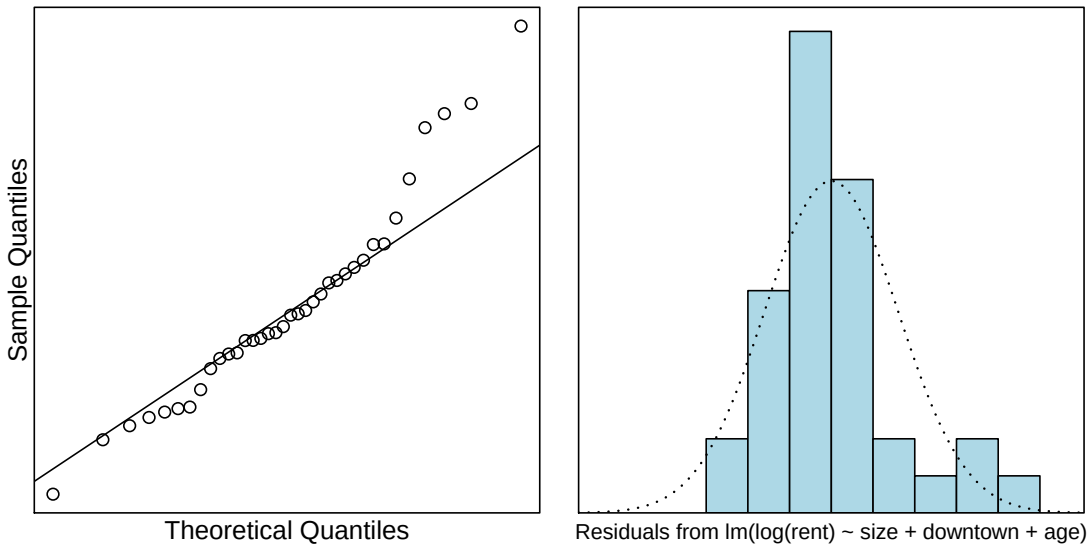
```
> rent3.fit = lm(log(rent) ~ size + downtown + age, data = rent.df)
> summary(rent3.fit)

Call:
lm(formula = log(rent) ~ size + downtown + age, data = rent.df)

Residuals:
     Min       1Q   Median       3Q      Max
-0.14880 -0.04378 -0.01215  0.03145  0.22034

Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)  5.695e+00  5.609e-02 101.540  < 2e-16 ***
size         8.434e-04  6.983e-05  12.078 2.94e-13 ***
downtown    -1.027e-01  1.640e-02  -6.264 5.80e-07 ***
ageOld       2.593e-01  3.793e-02   6.837 1.16e-07 ***
ageRecent    9.038e-02  4.005e-02   2.256   0.0312 *
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.08514 on 31 degrees of freedom
Multiple R-squared:  0.9104,Adjusted R-squared:  0.8988
F-statistic: 78.73 on 4 and 31 DF,  p-value: 8.741e-16
> eovcheck(rent3.fit)
```



```
> cooks20x(rent3.fit)
```




```
> normcheck(rent3.fit, main = "")
```



```
> exp(confint(rent3.fit))
                  2.5 %      97.5 %
(Intercept) 265.2570610 333.4455396
size          1.0007013   1.0009863
downtown      0.8727017   0.9330716
ageOld        1.1995592   1.4002531
ageRecent     1.0087282   1.1877668


> 100 * (exp(confint(rent3.fit)[2:5, ]) - 1)
                 2.5 %      97.5 %
size        0.07012659  0.09863448
downtown  -12.72982697 -6.69283734
ageOld     19.95592060 40.02531162
ageRecent   0.87282378 18.77668023


> ## For a 100-unit change in size.
> 100 * (exp(100 * confint(rent3.fit)[2, ]) - 1)
   2.5 %   97.5 %
 7.26176 10.36092
```

For Question (c) Only

```
> rent4.fit = lm(log(rent) ~ beds.F, data = rent.df)
> summary(rent4.fit)

Call:
lm(formula = log(rent) ~ beds.F, data = rent.df)

Residuals:
     Min       1Q   Median       3Q      Max
-0.36894 -0.21071 -0.01347  0.16764  0.40800

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept)  6.22687    0.05227 119.131  < 2e-16 ***
beds.F2      0.32167    0.07195   4.471 8.24e-05 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.2155 on 34 degrees of freedom
Multiple R-squared:  0.3702,Adjusted R-squared:  0.3517
F-statistic: 19.99 on 1 and 34 DF,  p-value: 8.243e-05
```

Lobster Survival Data

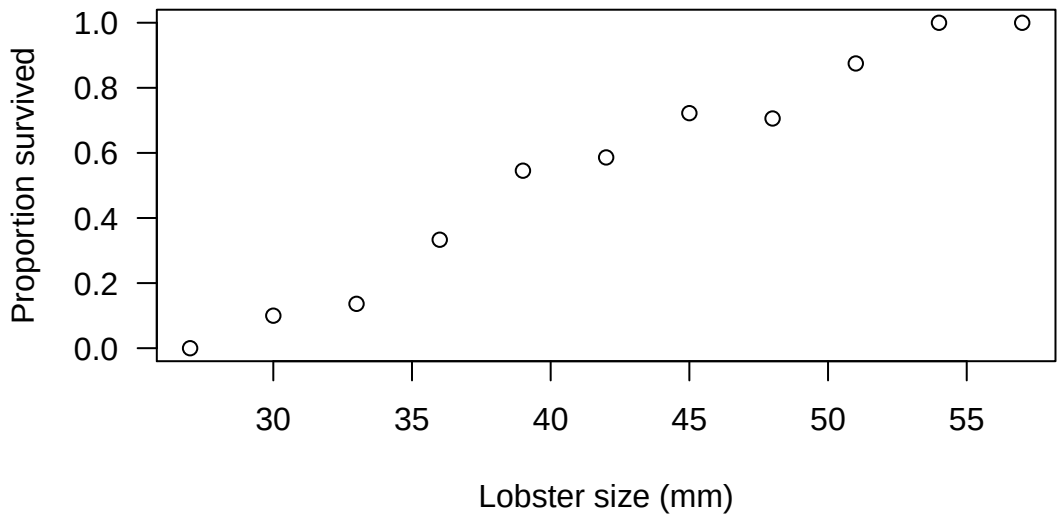
Biologists collected data to investigate how a lobster's size affects its survival. In total, they collected 159 juvenile lobsters from their natural habitat, and measured their size. They tethered the lobsters to the ocean floor for one night. Any lobsters that were missing were assumed to have been eaten by a predator. The surviving lobsters were released.

The variables in the data set are

`size`	Lobster length, measured to the nearest 3 mm
`n`	The number of lobsters of a particular length
`survived`	The number of lobsters of a particular length that survived

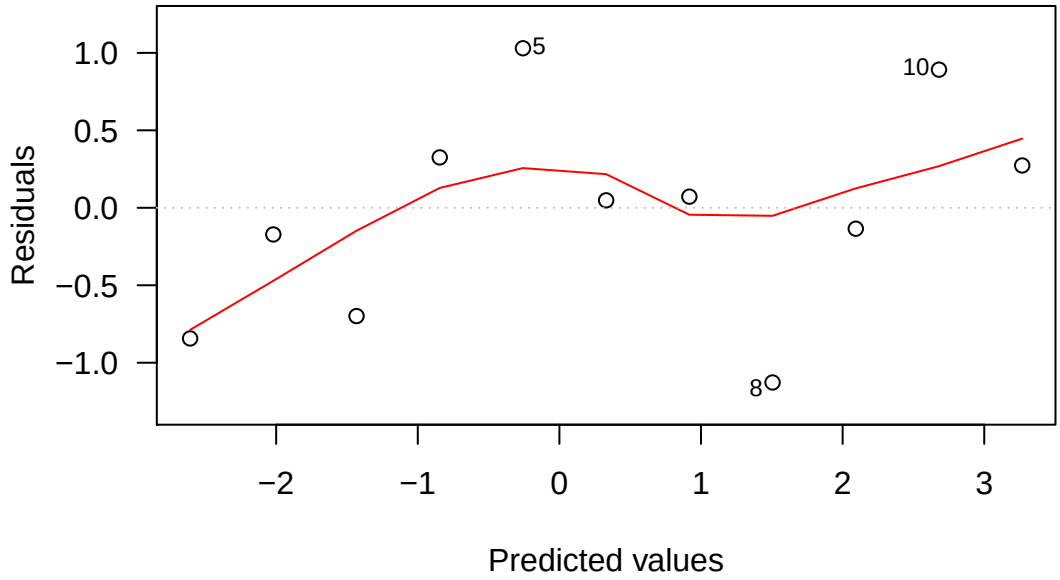
```
> lobster.df = within(lobster.df, {
+     p = survived/n
+ })
> lobster.df
   size  n survived         p
1    27  5        0 0.0000000
2    30 10        1 0.1000000
3    33 22        3 0.1363636
4    36 21        7 0.3333333
5    39 22       12 0.5454545
6    42 29       17 0.5862069
7    45 18       13 0.7222222
8    48 17       12 0.7058824
9    51  8        7 0.8750000
10   54  6        6 1.0000000
11   57  1        1 1.0000000
```

```
> plot(p ~ size, data = lobster.df,
+      xlab = "Lobster size (mm)",
+      ylab = "Proportion survived")
```




```
> lobster1.fit = lm(p ~ size, data = lobster.df)
> summary(lobster1.fit)

Call:
lm(formula = p ~ size, data = lobster.df)

Residuals:
      Min        1Q    Median        3Q       Max
-0.089376 -0.036212  0.000887  0.033829  0.106301

Coefficients:
             Estimate Std. Error t value Pr(>|t|)
(Intercept) -0.948038   0.086867  -10.91 1.72e-06 ***
size         0.035569   0.002017   17.63 2.75e-08 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.06348 on 9 degrees of freedom
Multiple R-squared:  0.9719,Adjusted R-squared:  0.9687
F-statistic: 310.8 on 1 and 9 DF,  p-value: 2.752e-08
```

```
> lobster2.fit = glm(p ~ size, family = "binomial", weights = n, data = lobs
> summary(lobster2.fit)

Call:
glm(formula = p ~ size, family = "binomial", data = lobster.df,
    weights = n)

Deviance Residuals:
     Min        1Q    Median        3Q       Max
-1.12729  -0.43534   0.04841   0.29938   1.02995

Coefficients:
            Estimate Std. Error z value Pr(>|z|)
(Intercept) -7.89597    1.38501  -5.701 1.19e-08 ***
size         0.19586    0.03415   5.735 9.77e-09 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

    Null deviance: 52.1054  on 10  degrees of freedom
Residual deviance:  4.5623  on  9  degrees of freedom
AIC: 32.24

Number of Fisher Scoring iterations: 4


> plot(lobster2.fit, which = 1)
```




```
> lobster2.fit$deviance
[1] 4.562321
> lobster2.fit$df.residual
[1] 9
> 1 - pchisq(lobster2.fit$deviance, lobster2.fit$df.residual)
[1] 0.8706732
> confint(lobster2.fit)
```

Waiting for profiling to be done...

```
                 2.5 %     97.5 %
(Intercept) -10.8034921 -5.3449644
size          0.1329987  0.2675871
> exp(confint(lobster2.fit))
```

Waiting for profiling to be done...

```
                   2.5 %      97.5 %
(Intercept) 2.032839e-05 0.004772121
size        1.142249e+00 1.306807434
```

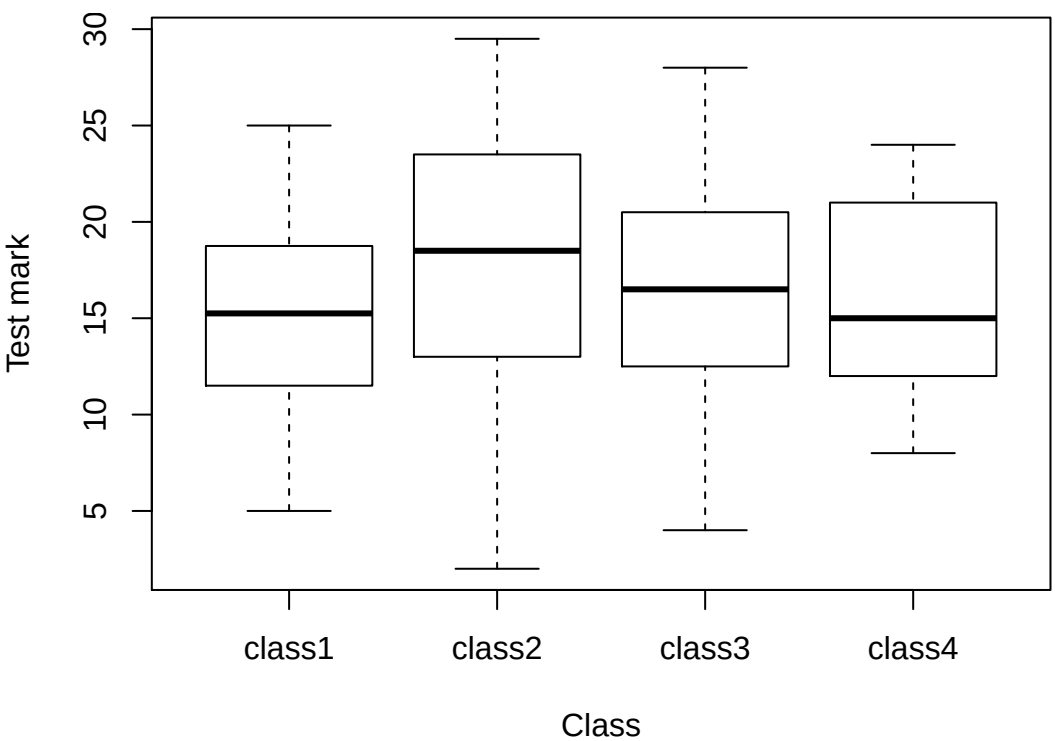
Southwest University Test Data

STATS 201 students at Southwest University completed a mid-semester test on 16 April 2018. Each student in the course belongs to one of four 'classes'. The lecturer was interested in whether or not some classes have better students than others, on average.

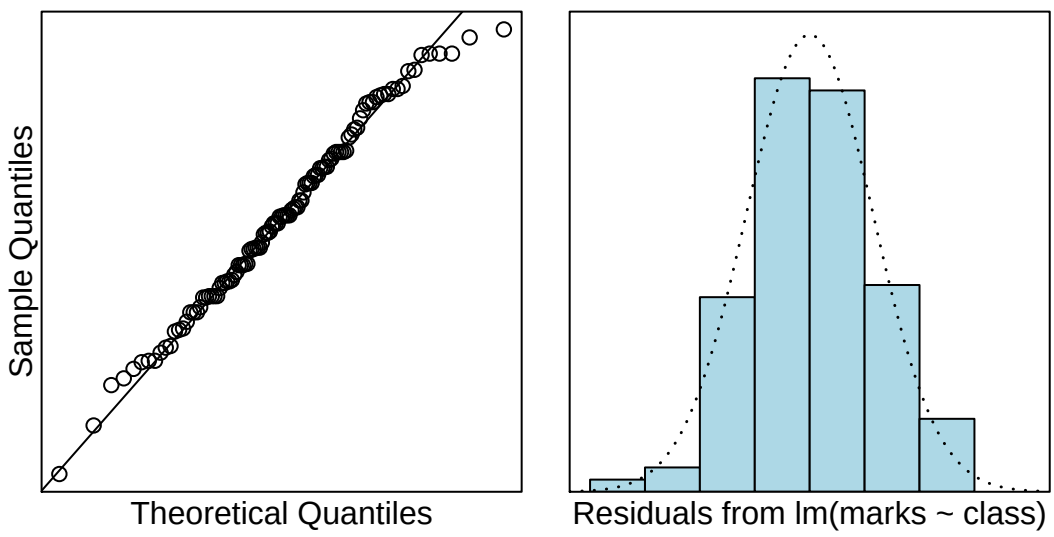
The variables in the data set are

`marks`	The student's score on the test
`class`	The student's class; either `class1`, `class2`, `class3`, or `class4`

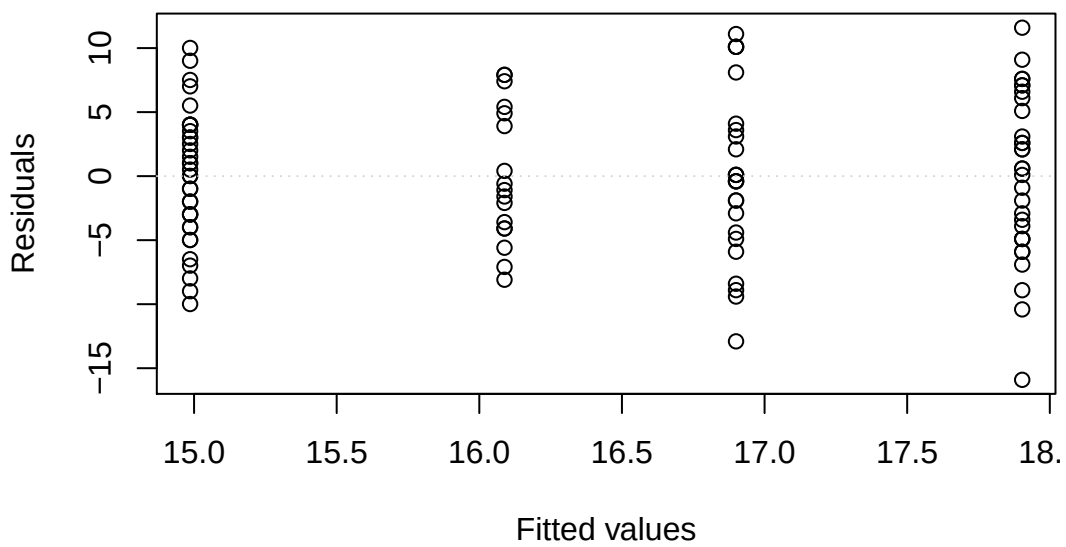
```
> boxplot(marks ~ class, data = test.df, xlab = "Class",
+         ylab = "Test mark")
```



```
> test.fit = lm(marks ~ class, data = test.df)
> normcheck(test.fit)
```




```
> eovcheck(test.fit)
```



```
> anova(test.fit)
Analysis of Variance Table

Response: marks
           Df Sum Sq Mean Sq F value Pr(>F)
class       3  149.8  49.947  1.4523 0.2319
Residuals 105 3611.1  34.391


> summary(test.fit)

Call:
lm(formula = marks ~ class, data = test.df)

Residuals:
     Min       1Q   Median       3Q      Max
-15.9032  -4.0882   0.0139   4.0139  11.5968

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept)  14.9861     0.9774  15.333   <2e-16 ***
classclass2   2.9171     1.4369   2.030   0.0449 *
classclass3   1.9139     1.5267   1.254   0.2128
classclass4   1.1021     1.7258   0.639   0.5245
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 5.864 on 105 degrees of freedom
Multiple R-squared:  0.03984,Adjusted R-squared:  0.01241
F-statistic: 1.452 on 3 and 105 DF,  p-value: 0.2319


> confint(test.fit)
                   2.5 %    97.5 %
(Intercept) 13.04810861 16.924114
classclass2  0.06799374  5.766236
classclass3 -1.11336779  4.941146
classclass4 -2.31977970  4.524028
```

```
> multipleComp(test.fit)
                    Estimate Tukey.L Tukey.U Tukey.p
class1  -  class2 -2.9171147 -6.6684  0.8342  0.1836
class1  -  class3 -1.9138889 -5.8997  2.0719  0.5944
class1  -  class4 -1.1021242 -5.6075  3.4033  0.9193
class2  -  class3  1.0032258 -3.1122  5.1187  0.9200
class2  -  class4  1.8149905 -2.8055  6.4355  0.7349
class3  -  class4  0.8117647 -4.0011  5.6246  0.9713
```