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```
%Tyler Matthews
%System Simluation Midterm P3
close; clc; close all;

A = [-4.7, -1.55, -0.55; 0.3, -2.75, -0.35; 1.1, 1.85, -2.55]
B = [1; 0; -1]
C = [2, 1, 1]
D = [0]
```

```
A =

   -4.7000   -1.5500   -0.5500
    0.3000   -2.7500   -0.3500
    1.1000    1.8500   -2.5500

B =

     1
     0
    -1

C =

     2     1     1

D =

     0
```

PART A

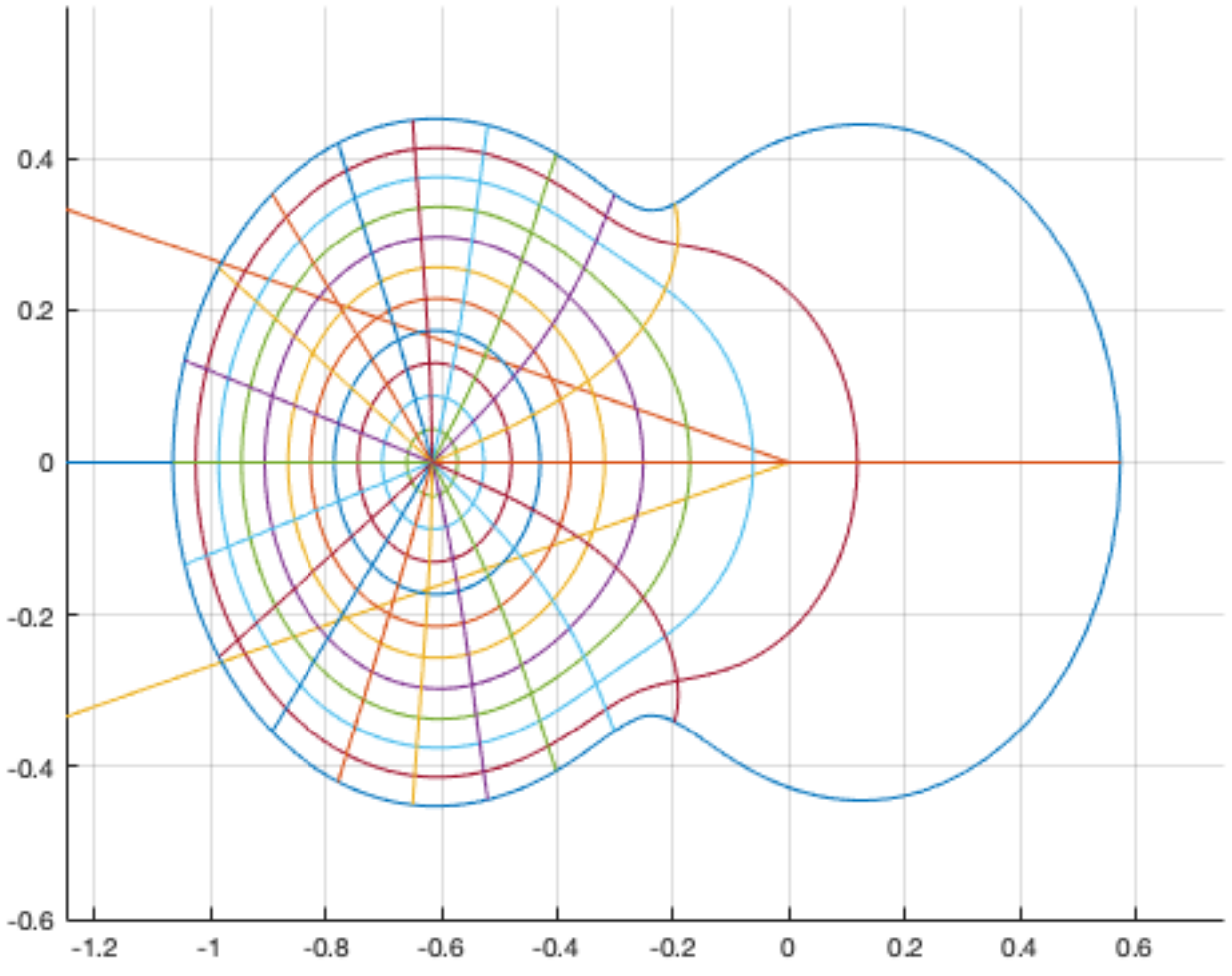
```
lamda = eig(A)
```

```
lamda =

  -4.0000 + 0.0000i
  -3.0000 + 0.8000i
```

```
  -3.0000 - 0.8000i
```

PART B

```
Nt=21;
Nr=12;

theta=linspace(0,2*pi,1001);
rho=linspace(0,0.5256,1001);
tvec=linspace(0,2*pi,Nt);
rvec=linspace(0,0.5256,Nr);

T = linspace(0,1,1001);

hold on
plot(real(lamda(1)*T), imag(lamda(1)*T))
plot(real(lamda(2)*T), imag(lamda(2)*T))
plot(real(lamda(3)*T), imag(lamda(3)*T))
hold off



for k=1:length(rvec)
 z=rvec(k)*exp(i*theta);
 w=(z.^2-z.*1.45 + 0.45)./(z.*1.27-0.73);
 hold on
 plot(real(w), imag(w))
 hold off
end

for k=1:length(tvec)-1
 z=rho*exp(i*tvec(k));
 w=(z.^2-z.*1.45 + 0.45)./(z.*1.27-0.73);
 hold on
 plot(real(w), imag(w))
 hold off
end


grid on
axis([-1.25 0.75 -0.6 0.6])
```



PART C

```
stable_acc = 0.146;
stable_inacc = 0.3133;
unstable = 1;

disp("Stable and accurate at T = " + stable_acc);
disp("Stable and inaccurate at T = " + stable_inacc);
disp("Unstable and inaccurate at T = " + unstable);
```

```
Stable and accurate at T = 0.146
Stable and inaccurate at T = 0.3133
Unstable and inaccurate at T = 1
```

PART D

```
num = [0 1.27 -0.73];
den = [1 -1.45 0.45];

l1 = lamda * stable_acc
l2 = lamda * stable_inacc
l3 = lamda * unstable

stable_accurate_poles = roots(den - num*l1)
stable_inaccurate_poles = roots(den - num*l2)
unstable_inaccurate_poles = roots(den - num*l3)
```

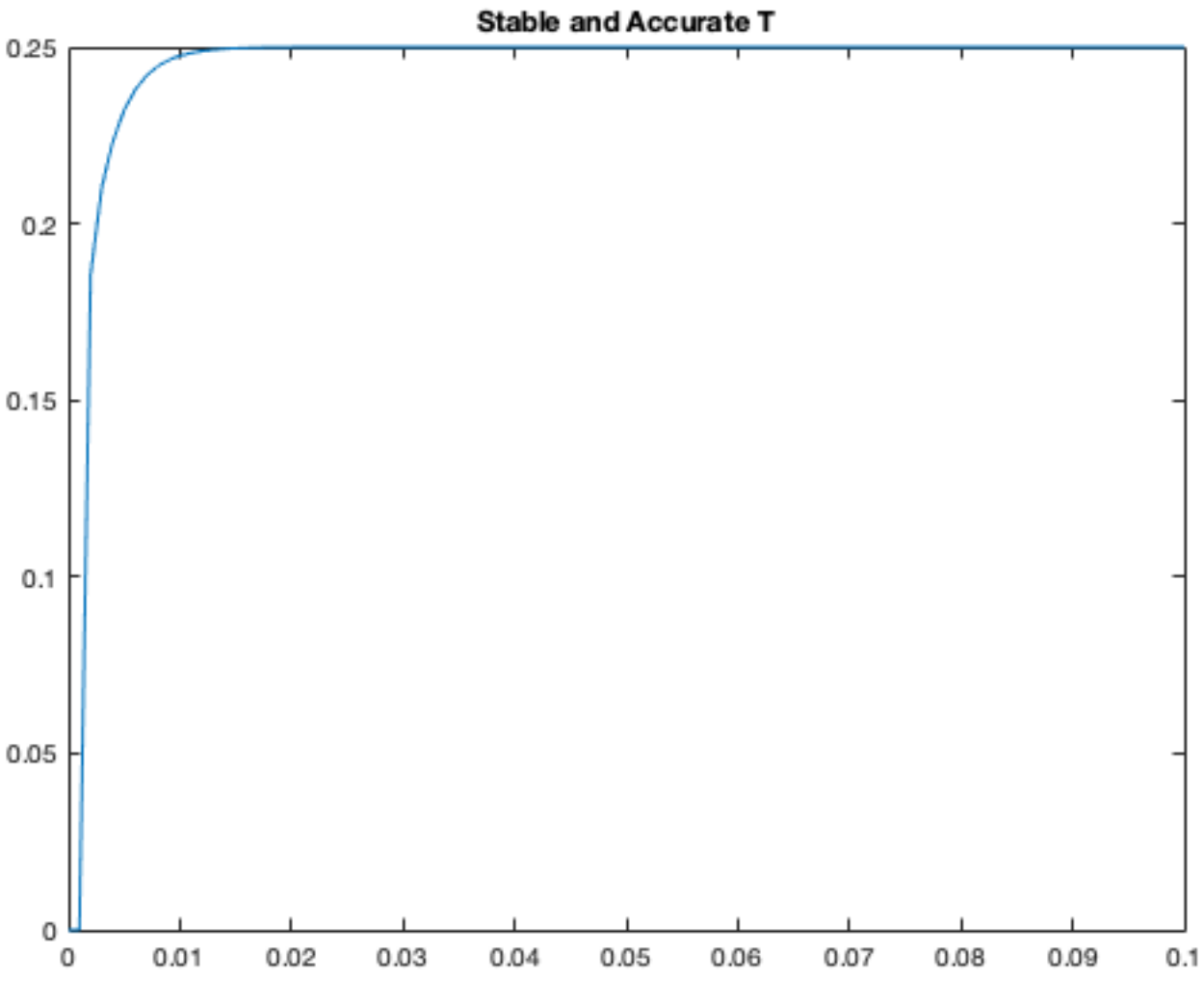
```
l1 =

  -0.5840 + 0.0000i
  -0.4380 + 0.1168i
  -0.4380 - 0.1168i


l2 =

  -1.2532 + 0.0000i
  -0.9399 + 0.2506i
  -0.9399 - 0.2506i


l3 =

  -4.0000 + 0.0000i
  -3.0000 + 0.8000i
  -3.0000 - 0.8000i


stable_accurate_poles =

   0.6442 + 0.8364i
   0.2689 - 0.4750i


stable_inaccurate_poles =

   0.3648 + 1.0768i
   0.0985 - 0.5902i


unstable_inaccurate_poles =

  -0.1449 + 1.1381i
  -0.1740 - 0.7222i
```

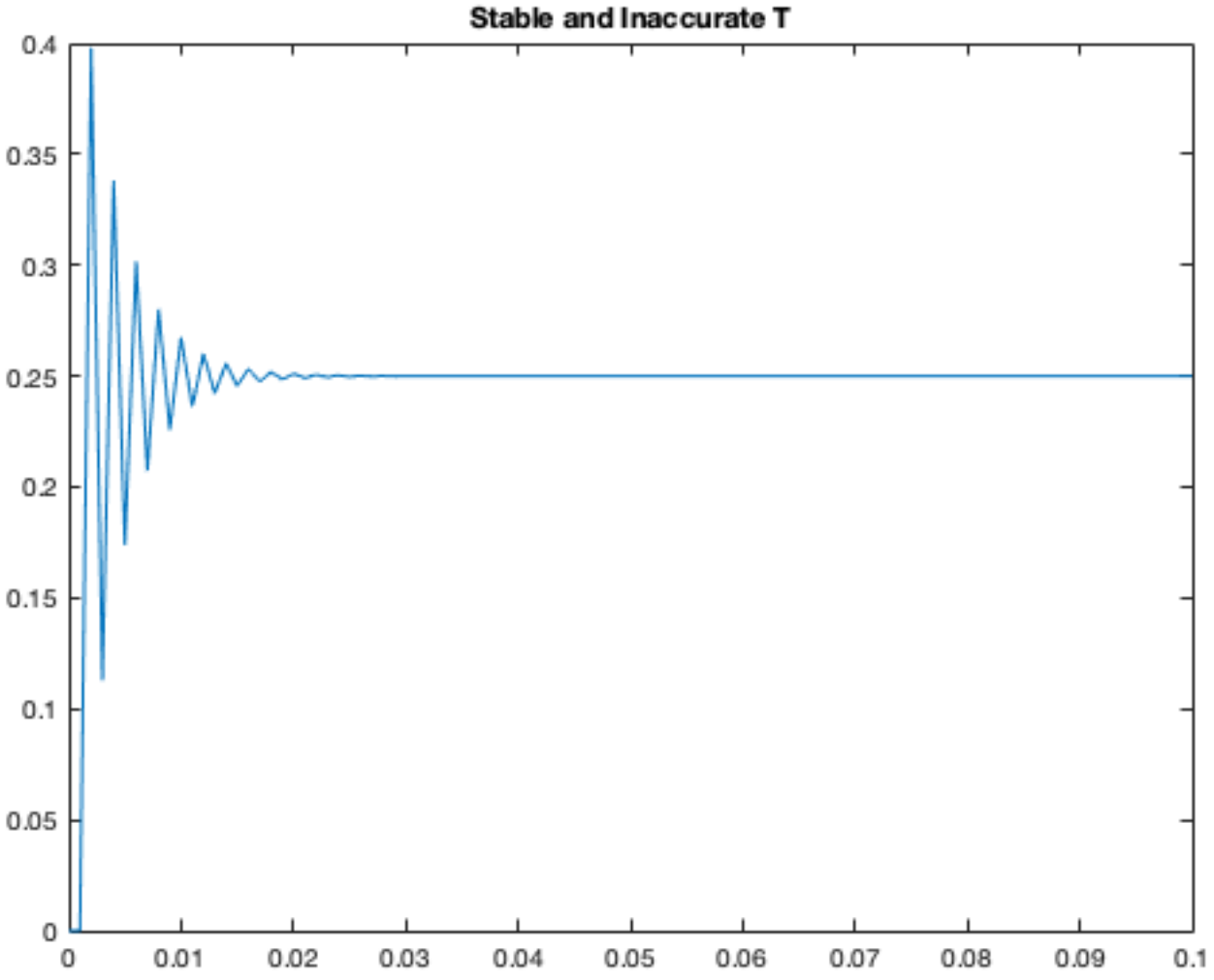
PART E

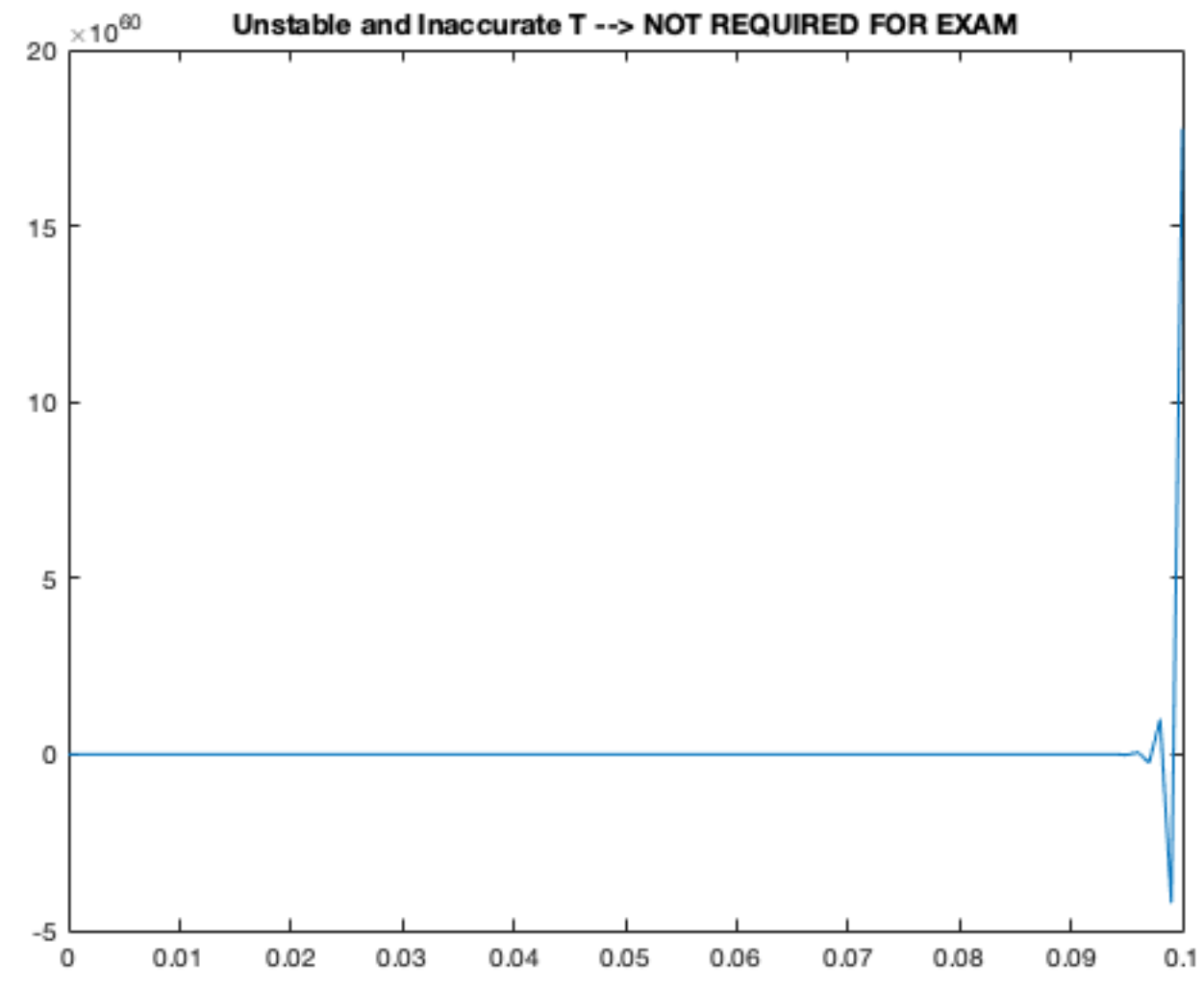
```
N = 10000;
t = linspace(0,10,N);
u = ones(1,N);
fx1 = zeros(1,N);
fx2 = zeros(1,N);
fx3 = zeros(1,N);
x1 = zeros(1,N);
x2 = zeros(1,N);
x3 = zeros(1,N);
y = zeros(1,N);

for k = 1:N-1
    fx1(k+1) = -4.7*x1(k+1)-1.55*x2(k+1)-0.55*x3(k+1)+u(k+1);
```

```
    fx2(k+1) = 0.3*x1(k+1)-2.75*x2(k+1)-0.35*x3(k+1);
    fx3(k+1) = 1.1*x1(k+1)+1.85*x2(k+1)-2.55*x3(k+1)-u(k+1);

    x1(k+2) = 1.45*x1(k+1) - 0.45*x1(k) + stable_acc * (1.27*fx1(k+1) - 0.73*fx1(k));
    x2(k+2) = 1.45*x2(k+1) - 0.45*x2(k) + stable_acc * (1.27*fx2(k+1) - 0.73*fx2(k));
    x3(k+2) = 1.45*x3(k+1) - 0.45*x3(k) + stable_acc * (1.27*fx3(k+1) - 0.73*fx3(k));

    y(k) = 2*x1(k)+x2(k)+x3(k);
end
figure
plot(t,y)
xlim([0 0.1])
title('Stable and Accurate T')

N = 10000;
t = linspace(0,10,N);
u = ones(1,N);
fx1 = zeros(1,N);
fx2 = zeros(1,N);
fx3 = zeros(1,N);
x1 = zeros(1,N);
x2 = zeros(1,N);
x3 = zeros(1,N);
y = zeros(1,N);

for k = 1:N-1
    fx1(k+1) = -4.7*x1(k+1)-1.55*x2(k+1)-0.55*x3(k+1)+u(k+1);
    fx2(k+1) = 0.3*x1(k+1)-2.75*x2(k+1)-0.35*x3(k+1);
    fx3(k+1) = 1.1*x1(k+1)+1.85*x2(k+1)-2.55*x3(k+1)-u(k+1);

%     x1(k+1) = x1(k) + stable_inacc*fx1(k);
%     x2(k+1) = x2(k) + stable_inacc*fx2(k);
%     x3(k+1) = x3(k) + stable_inacc*fx3(k);

    x1(k+2) = 1.45*x1(k+1) - 0.45*x1(k) + stable_inacc * (1.27*fx1(k+1) - 0.73*fx1(k));
    x2(k+2) = 1.45*x2(k+1) - 0.45*x2(k) + stable_inacc * (1.27*fx2(k+1) - 0.73*fx2(k));
    x3(k+2) = 1.45*x3(k+1) - 0.45*x3(k) + stable_inacc * (1.27*fx3(k+1) - 0.73*fx3(k));


    y(k) = 2*x1(k)+x2(k)+x3(k);
end
figure
plot(t,y)
xlim([0 0.1])
title('Stable and Inaccurate T')

N = 10000;
t = linspace(0,10,N);
u = ones(1,N);
fx1 = zeros(1,N);
fx2 = zeros(1,N);
fx3 = zeros(1,N);
x1 = zeros(1,N);
x2 = zeros(1,N);
x3 = zeros(1,N);
y = zeros(1,N);
```

```
for k = 1:N-1
    fx1(k+1) = -4.7*x1(k+1)-1.55*x2(k+1)-0.55*x3(k+1)+u(k+1);
    fx2(k+1) = 0.3*x1(k+1)-2.75*x2(k+1)-0.35*x3(k+1);
    fx3(k+1) = 1.1*x1(k+1)+1.85*x2(k+1)-2.55*x3(k+1)-u(k+1);

    x1(k+2) = 1.45*x1(k+1) - 0.45*x1(k) + unstable * (1.27*fx1(k+1) - 0.73*fx1(k));
    x2(k+2) = 1.45*x2(k+1) - 0.45*x2(k) + unstable * (1.27*fx2(k+1) - 0.73*fx2(k));
    x3(k+2) = 1.45*x3(k+1) - 0.45*x3(k) + unstable * (1.27*fx3(k+1) - 0.73*fx3(k));

    y(k) = 2*x1(k)+x2(k)+x3(k);
end
figure
plot(t,y)
xlim([0 0.1])
title('Unstable and Inaccurate T --> NOT REQUIRED FOR EXAM')
```




Stable and Inaccurate T
0.4
0.35
0.3
0.25
0.2
0.15
0.1
0.05
0
0
0.01
0.02
0.03
0.04
0.05
0.06
0.07
0.08
0.09
0.1


Unstable and Inaccurate T --> NOT REQUIRED FOR EXAM
×10^60
20
15
10
5
0
-5
0
0.01
0.02
0.03
0.04
0.05
0.06
0.07
0.08
0.09
0.1

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