# Testing Kandle-based strategies using an ocaml simulator

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You need to install ocaml. Eg via the opam package manager

# 1 Setup

### 1.1 Setup price series

```
To run a test we first need to get a price series.
   There are two options.
   We can use a csv file of historical data (see h function):
let h
"number_of_lines:nb_lines (* nb_lines to read after header *)
~filename:filename
                            (* path to csv file *)
~column:col
                            (* index of price column in file *)
                            (* split char in the csv file *)
~splitchar:c
   Or we can use a BM or GBM with parameters:
let gbrowmo
~initial_value:ival
                            (* initial price value *)
~drift:drift
                            (* drift of BM *)
                            (* volatility of BM *)
~volatility:vol
~timestep:dt
                            (* integration step *)
```

```
~duration:duration (* total duration *) = ...
```

Both methods output a price series as an array of floats.

#### 1.2 Setup Kandle

To define a Kandle instance one needs:

- a (relative) price grid
- an initial allocation of capital (in quote),
- and the fraction  $\alpha$  of the said quote to be swapped to base (to provide Kandle's asks) The relative price grid is defined by picking any 2 of the following 3 parameters:
- (half) number of points,
- range multiplier,
- gridstep (aka ratio)

The initial price (or entry price) used to center the grid is taken from the price series (hence the name 'relative' price grid).

### 2 Plain simulation

A simulation is the interaction of a Kandle with a price series.

The output of a simulation run is a 6-uple:

- the return
- the number of up crossings and up exits (above range)
- the number of down crossings and down exits (below range)
- the final price of the price series

~duration:duration

To set up a run of the simulation, we combine both sets of parameters (using here range and gridstep for the price grid). Inputs:

(\* number of price moves \*)

```
Outputs:

(mtmf /. mtmi -. 1.),
!rebu,
!cross_above,
!rebd, !cross_below,
price_series.(start + duration - 1)

Fig. 1 shows an example of a 1000 runs, 10000 steps each.
The syntax is

./a.out 10_000 10 1.25

with arguments (in this order): number of repetitions, number of points on the grid, and ratio of the grid.
The compiled code will generate a csv file return_vs_final_price_scatter_1.25_10_stopped.csv.
The csv file can be visualised using a python script called hist.py with similar syntax python hist.py 10 1.25.
```

#### 3 Simulation with exit

There is a variant, called sim\_stopped, that will stop if the price down exits the range. So no need for specifying a duration. Either the simulation will stop (an return the time of exit and price), and it will run all the way to the end of the price series.

Inputs:

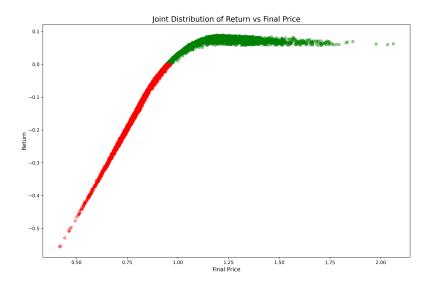


Figure 1: On the x-axis the final price, on the y-axis the return. In red (green) realisations with a negative (positive) return.

!rebd, !lower\_exit,
!current\_index,
!current\_price

**NB1** -  $sim_stopped$  returns the growth rate mtmf /. mtmi not the return mtmf /. mtmi - 1.

Fig. 2 shows an example of a 1000 runs, 10000 steps each (under 2sec of execution, using the native compiler ocamlopt). We see the green and red walls at the ends of the range near the  $\pm 20\%$  mark.

## 4 Simulation with reset

There is also a sim\_reset variant where each time the price exits the range, the strategy re-enters with the same grid translated to the new current price.

Fig. 3 shows an example where r = 1.02, 1 offer on each side of the entry price, and a price GBM  $\mu = 0$ ,  $\sigma = 0.08$ . One sees that the peyoff shape is very different, and looks extremely similar to a buy and hold with half the cash invested (black line) with some low

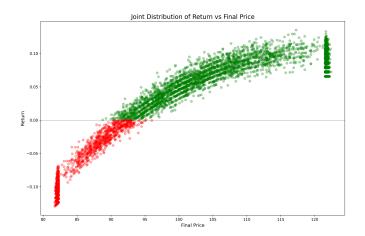


Figure 2: On the x-axis the final price, on the y-axis the return. The Kandle grid has 4 points (on each side of the entry price of 100), with a ratio of 1.05.

amount of noise induced by the path-dependent crossings.

## 4.1 Discussion of price-tracking Kandle (sim reset)

**NB2** - price-tracking Kandle is subtly different from a simple MM strategy which translates its price grid each time the price moves (at a given frequency), regardless of whether one of its offers was consumed or not. It would be interesting to simulate that as well. The difference is that in the latter case even in the absence of crossing the price stays always  $\epsilon$  away from the current price.

Todo: implement the vanilla MM strategy and measure the payoff difference (MM should be better).

Idea: One can 'neutralise' the determinstic part of the pay-off by adding  $-\beta S_t$  (eg by shorting a certain amount  $\beta$  of the underlying on a perp market, or by borrowing some of the underlying on a mending platform). The exact offset to be determined by fitting a regression line to a numerical experiment - will depend on  $(r, \sigma)$ .

For large ratios r > 1.1 (aka grid steps), there are < 1 crossings on average and the constant is very nearly  $\beta = \frac{1}{2}$  (ie a complete buy-and-hold). As r decreases, the mean number of crossings increases and the constant  $\beta$  seem to decrease. To investigate empirically.

**QS1** - Is there for given  $\sigma$  a value  $r^*(\sigma)$  of r that maximises the mean return? [similar to prior work done for plain Kandle]

Todo: Try same experiments with multiple price points (not just 2)

Can we combine sim with reset with a stop loss? Eg, is it useful to stop resetting after k moves, or a certain minimum residual capital



Figure 3: The regression line is close to that of a buy-and-hold strategy with half the cash invested in the risky asset.

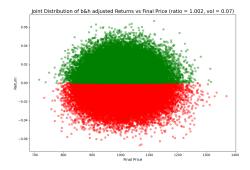


Figure 4: adjusted return vs exit price (ratio = 1.002, vol = 0.07)

(or on a momentum signal)?

A small remark: concretely, when ruining on chain, price-tracking Kandle does not have access to the next price (as the simulation does) only that  $p_{n+1} > rp_n$ ; to correct this one can use multiple offers to improve the upper bound, and/or use an oracle at update time

(eg consult another liquidity source).

#### 4.2 Analysis of sim reset

Let  $\alpha \in [0,1]$  be the cash ratio (amount of initial capital kept in quote). Set  $\alpha' := 1 - \alpha$  to simplify notations. The total gain under a given price run is:

$$\Gamma(\alpha) = (\alpha + \alpha' r)^{n_u} (\alpha + \alpha' / r)^{n_d} \tag{1}$$

where  $n_u$  is the number of up-crossings,  $n_d$  is the number of down-crossings along the price trajectories.

The crossing numbers are random and only depend on vol-and-grid,  $\sigma$  and r.

As  $\alpha + \alpha' r > 1$  (barycenter of 1 and r > 1), and  $\alpha + \alpha' / r < 1$  (barycenter of 1 and 1/r < 1), it follows that  $\Gamma > 1$  is the strategy is profitable for a given trajectory as soon as  $n_u > n_d$ .

In partcular if  $\alpha = \alpha' = \frac{1}{2}$ , we get:

$$\log(\Gamma(1/2)) = n_u \log(\frac{1+r}{2}) + n_d \log(\frac{1+1/r}{2})$$
  
=  $N(f_u \log(\frac{1+r}{2}) + f_d \log(\frac{1+1/r}{2}))$ 

where in the last line we assume  $N = n_u + n_d > 0$  (not always true! especially for large ranges).

The above is > 0 iff:

$$f_d/f_u \le \frac{\log(1+r) - \log 2}{\log 2 - \log(1+r^{-1})} =: k(r)$$

where  $k(r) \ge 1$  is increasing and converges to  $\log(1+r)/\log(2) - 1$  for large r. This suggests that larger rs are more likely to generate profits. To make sure we need to study how the  $f_d$ ,  $f_u$  distribution depends on r. It seems unlikely but it could be that larger r are biased downwards, ie  $f_d/f_u$  is increasing function of r. [in sims up and down crossings look equally likely]

Todo: study the distribution of  $f_u$  as a function of r and  $\sigma$ . [Also look at std]

We can see the effect of changing  $\alpha$ .

If  $\alpha = 0$  (base only),  $\Gamma(0) = r^{n_u - n_d}$ . If we go full base, we win iff the process crosses more up than down.

If  $\alpha' = 0$  (quote only),  $\Gamma(1) = 1$ . Indeed if we never buy the underlying, all that can happen is the execution of a bid, the output of which that strategy re-sells immediately at same price (assuming no fees, no slippage), and therefore the initial wealth never changes. Ie (modulo fees and slippage), setting  $\alpha = 0$  amounts to not playing.

**NB** - Euler-Maruyama for large  $\sqrt{dt}$ , large  $\sigma$  can lead to negative prices in a GBM; so better use the integral form.