

# Uncertainty Quantification in Deep Learning

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# Outline



Why

... do we need  
uncertainty  
quantification?

What

... uncertainties are  
there?

How

... can we quantify  
uncertainties?

Why do we need UQ?

# The Real World is Messy



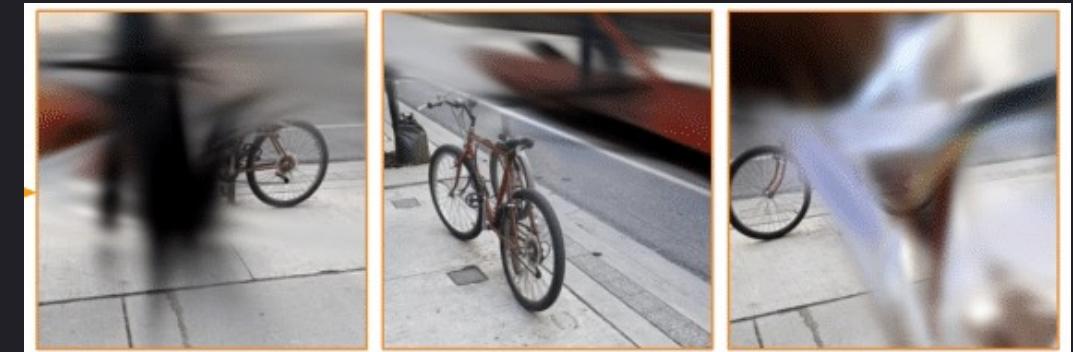
# The Real World is Messy

## Distribution Shifts

Train			Val (OOD)	Test (OOD)	
d = Hospital 1	d = Hospital 2	d = Hospital 3	d = Hospital 4	d = Hospital 5	
y = Normal					
y = Tumor					

Source: P W Koh *et al.* WILDS: A Benchmark of in-the-Wild Distribution Shifts. In ICML, 2021.

## Various Sources of Noise



Source: S Sabour *et al.* SpotlessSplats: Ignoring Distractors in 3D Gaussian Splatting. In ICML, 2021.

# Expectations for ML Systems

Our systems/models should be **safe** and **trustworthy**.

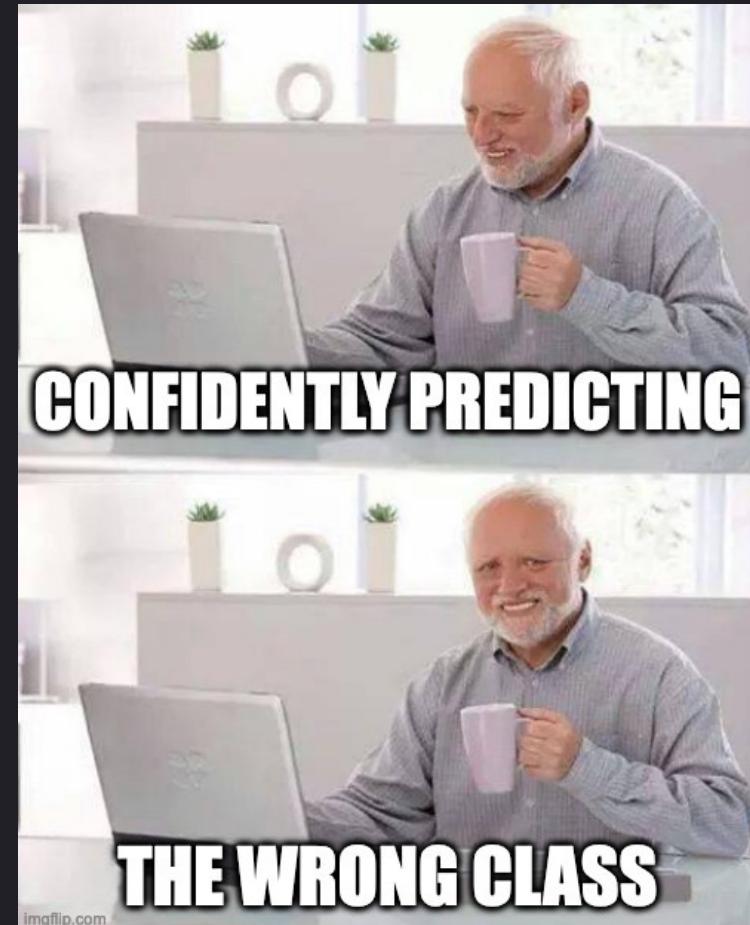
For this, we require they are:

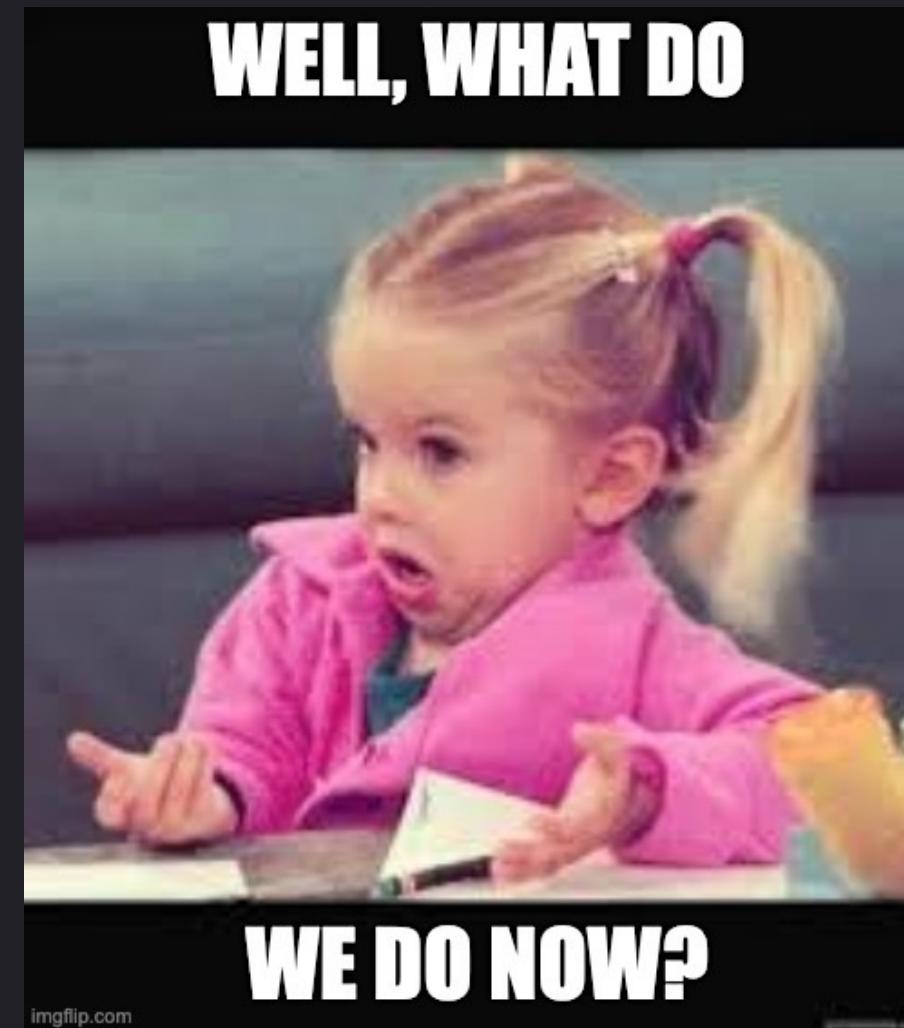
- **Accurate** in their predictions
- **Robust** to input-perturbations (noise, adversarial attacks)
- "Know when they don't know" (recognize out-of-domain data)
- **Act** if they are uncertain (*e.g.*, active learning, reasoning)

# However, ...

- Accurate Predictions
- Sensitive to perturbations
- Don't know when they don't know
- Overconfident in their predictions

Often considered “unreliable”

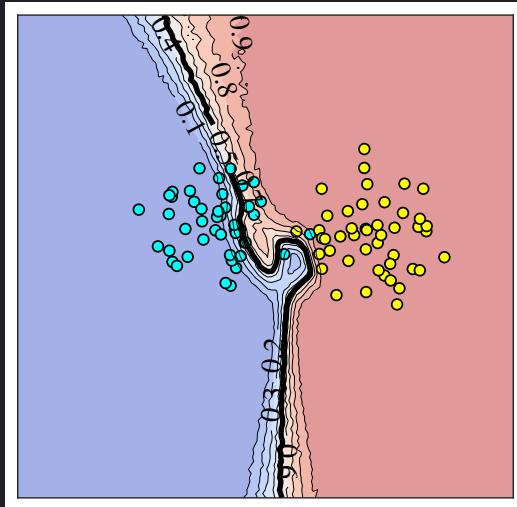




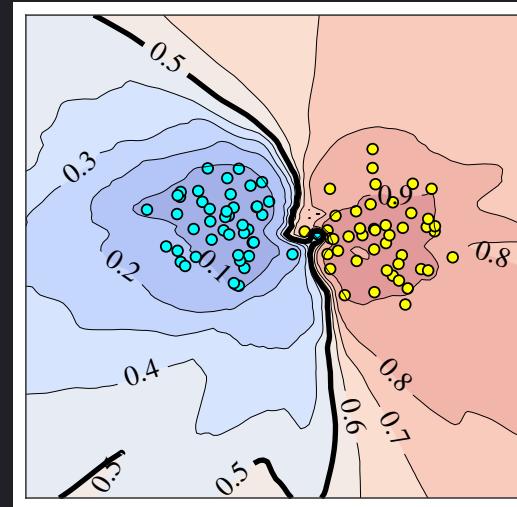
# Uncertainty Quantification can Help...

Reduce Overconfidence

NN w/o UQ

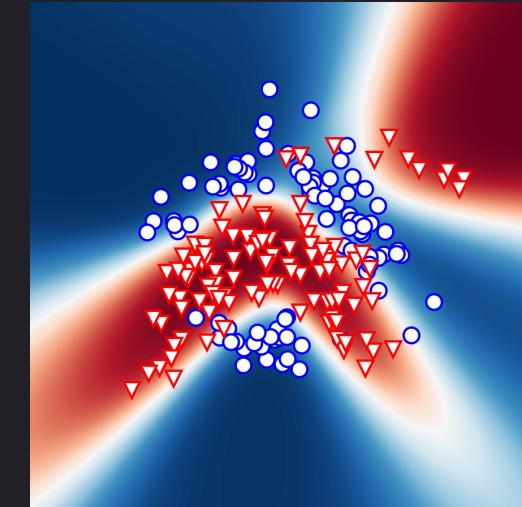


NN w UQ

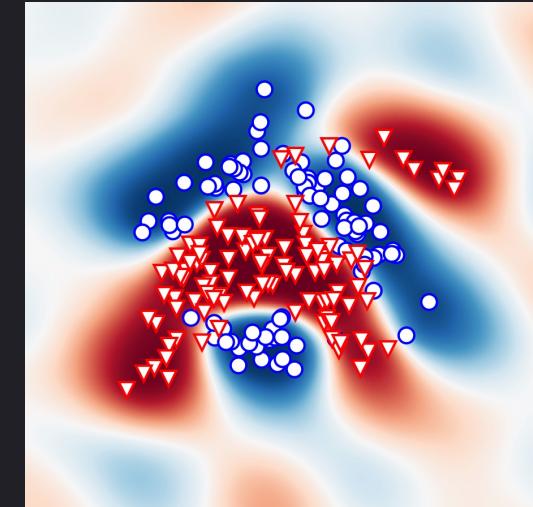


Understand Inductive Biases

ReLU



Periodic Function

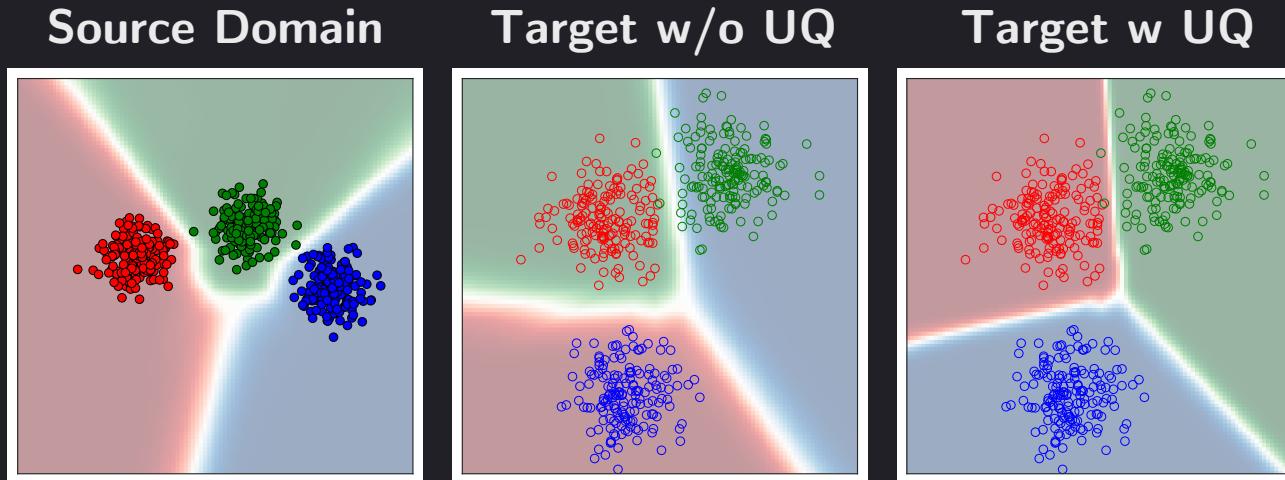


Source: A Kristiadi, M Hein, P Hennig. Being Bayesian, Even Just a Bit, Fixes Overconfidence in ReLU Networks. In ICML, 2020.

Source: L Meronen, M Trapp, A Solin. Periodic activation functions induce stationarity. In NeurIPS, 2021.

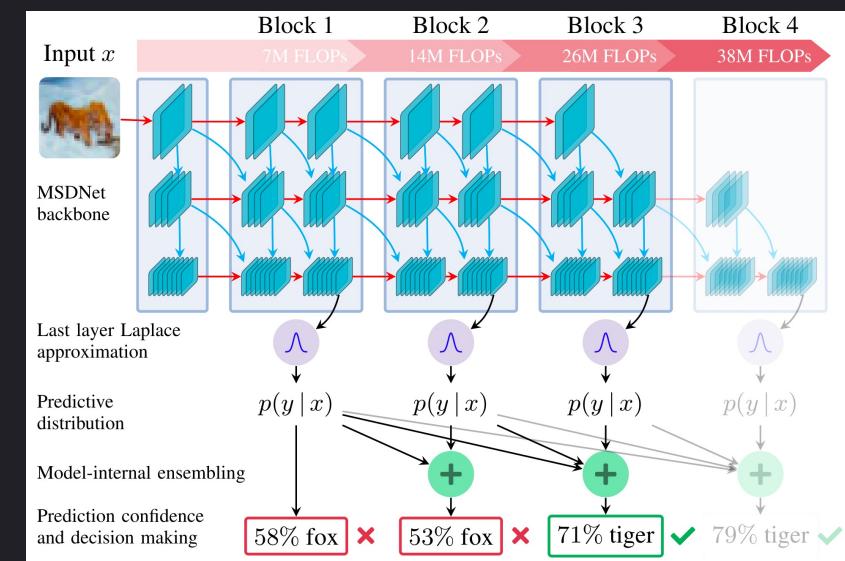
# Uncertainty Quantification can Help...

Robustify our Methods



Source: S Roy *et al.* Uncertainty-guided Source-free Domain Adaptation. In ECCV, 2022.

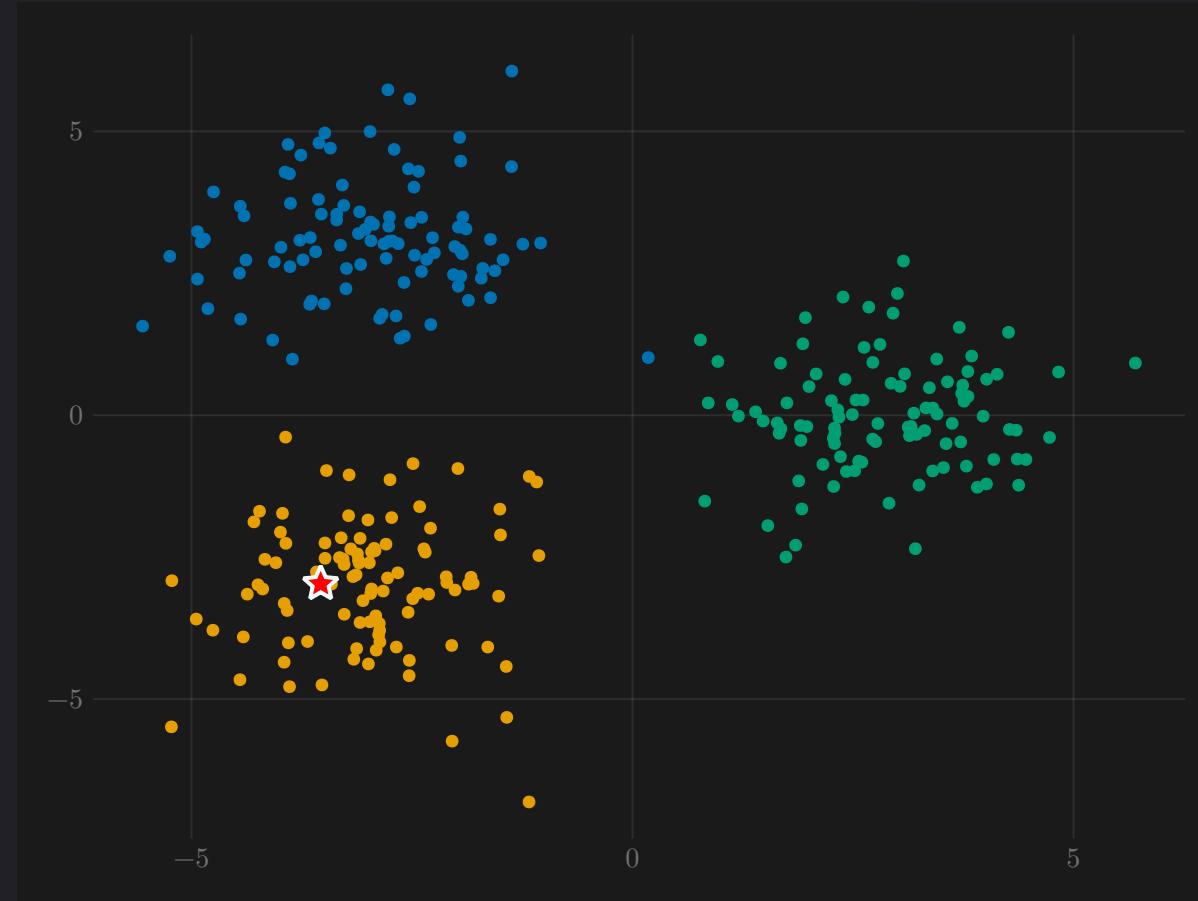
Decide When to  
Act Differently



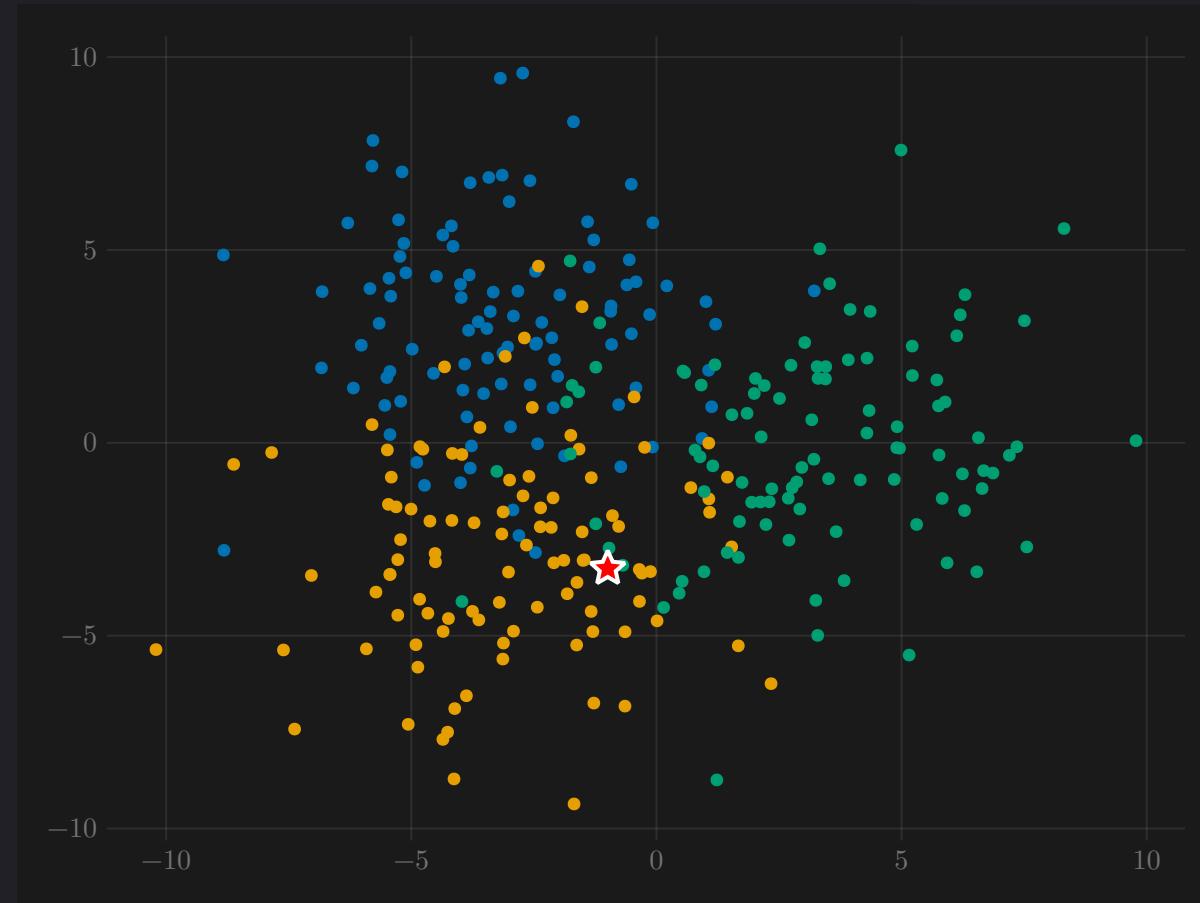
Source: L Meronen *et al.* Fixing Overconfidence in Dynamic Neural Networks. In WACV, 2024.

# Sources of Uncertainty

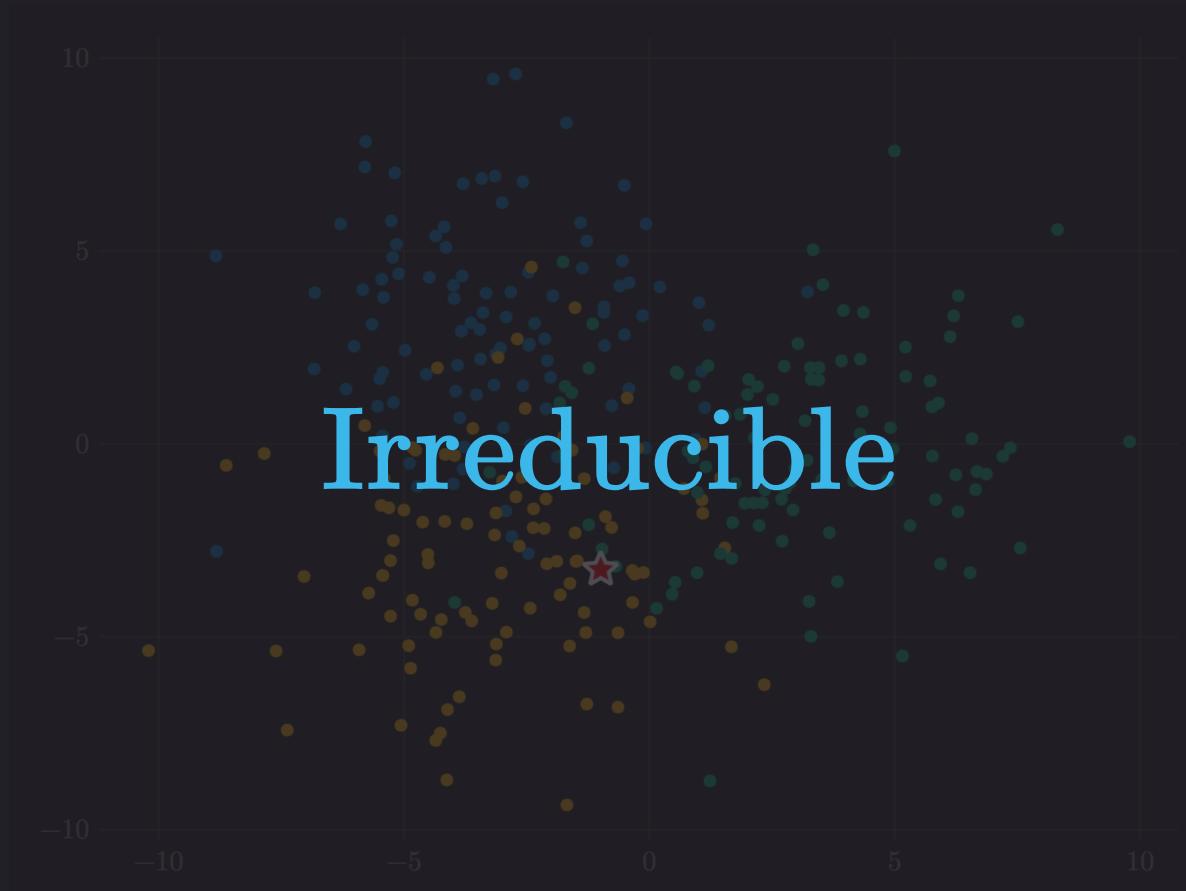
# Uncertainty Inherent to the Data



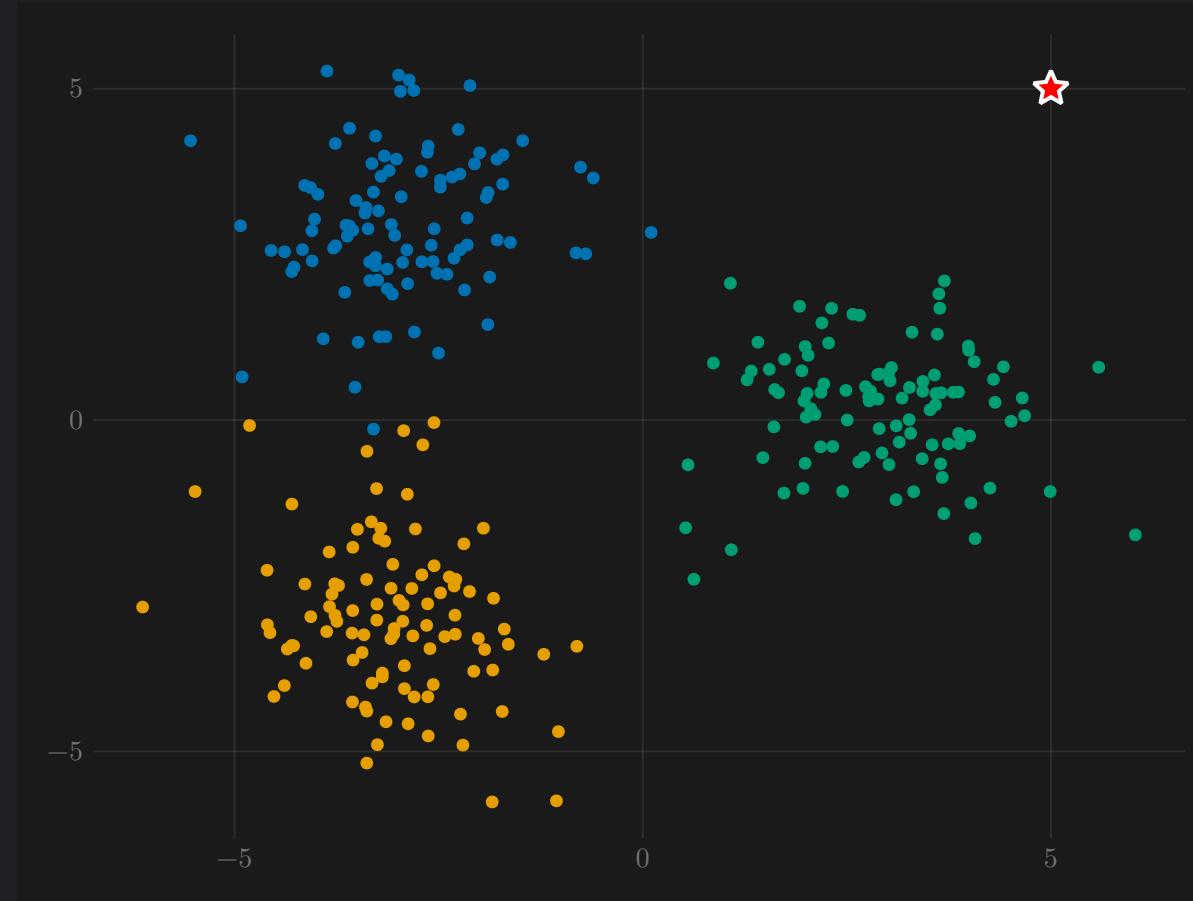
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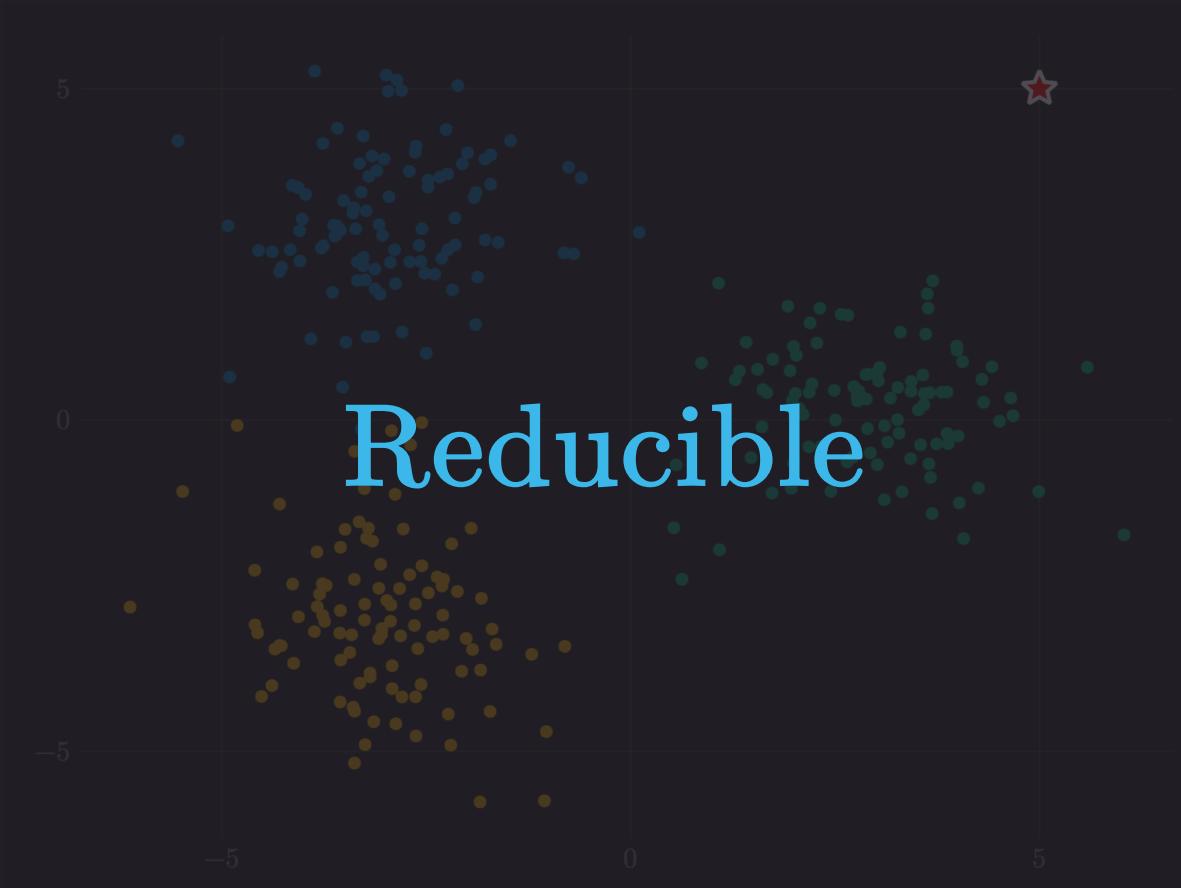
# Uncertainty Inherent to the Data



# Uncertainty due to Lack of Knowledge



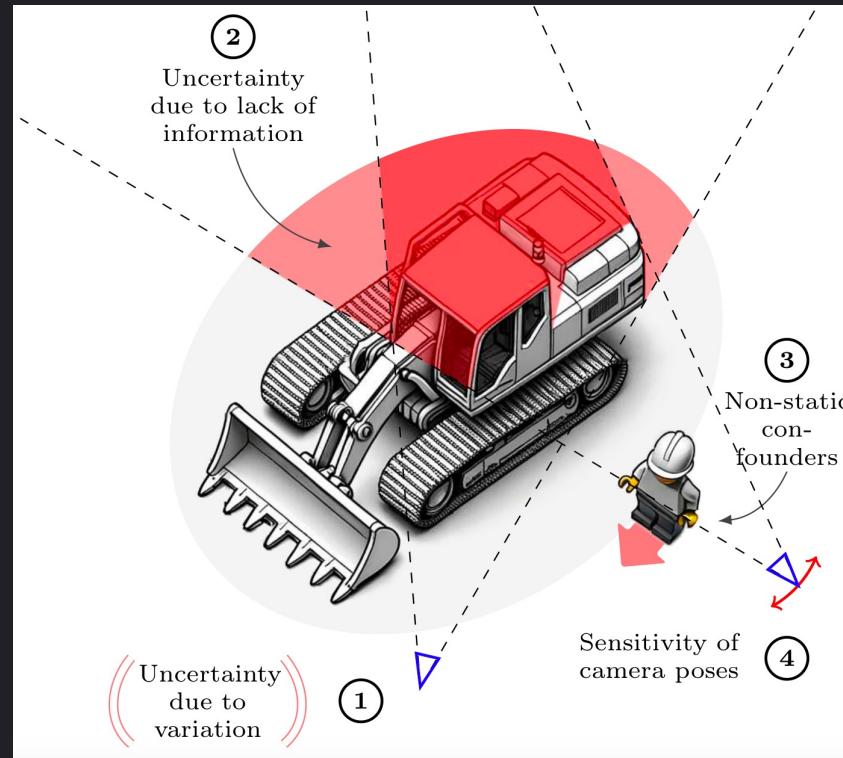
# Uncertainty due to Lack of Knowledge



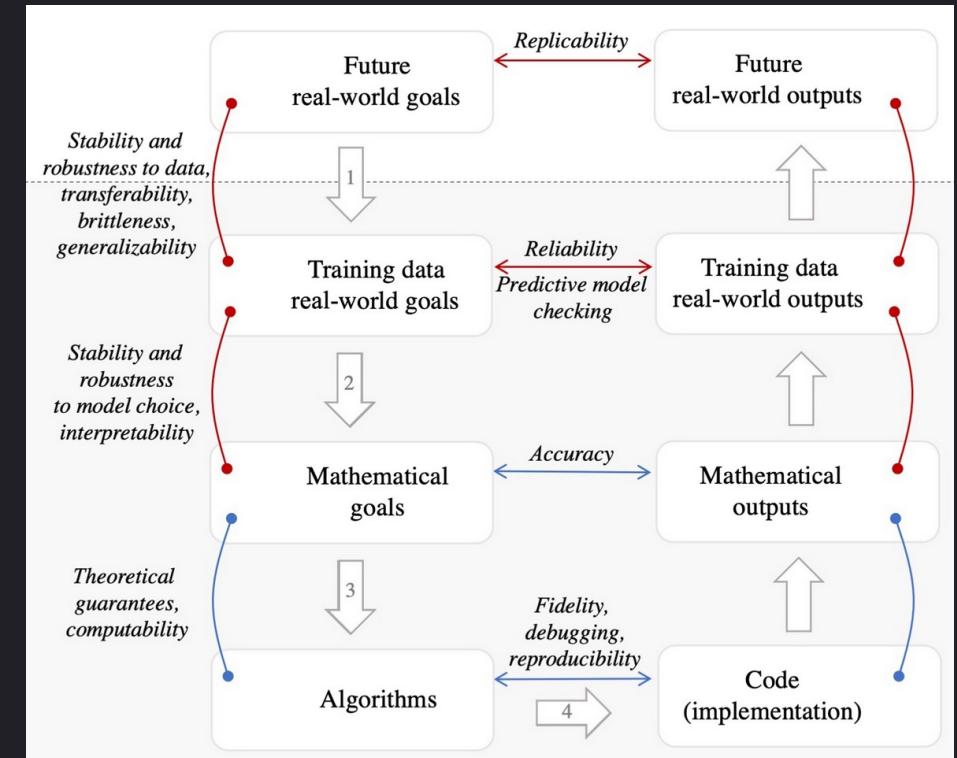
# Uncertainty due to Lack of Knowledge



# Sources vary between Applications



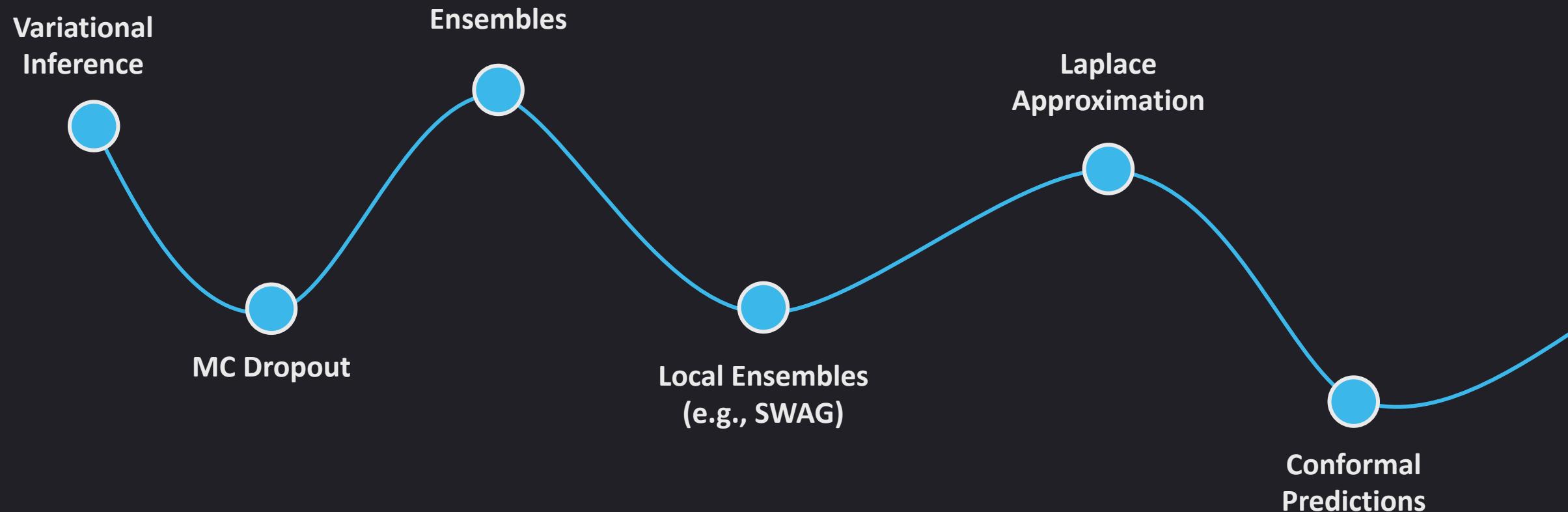
Source: M Klasson *et al.* Sources of Uncertainty in 3D Scene Reconstruction. In UNCV Workshop at ECCV, 2024.



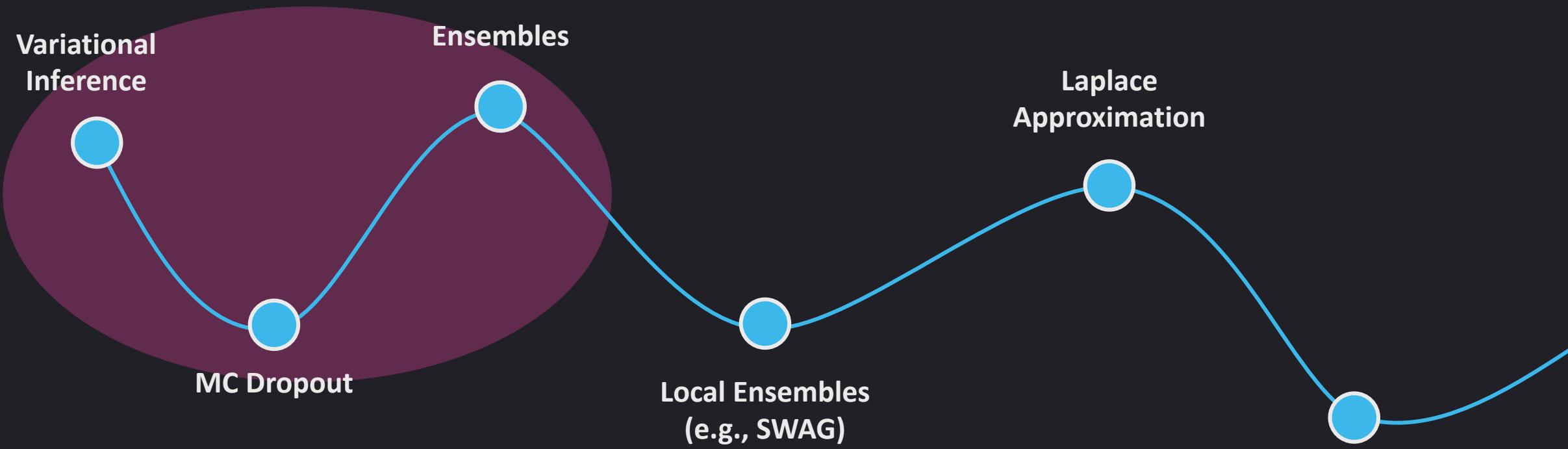
Source: T Broederick *et al.* Toward a Taxonomy of Trust for Probabilistic Machine Learning. *Science Advances* 9, eabn399, 2023.

# Methods for UQ in DL

# Methods for Uncertainty Quantification

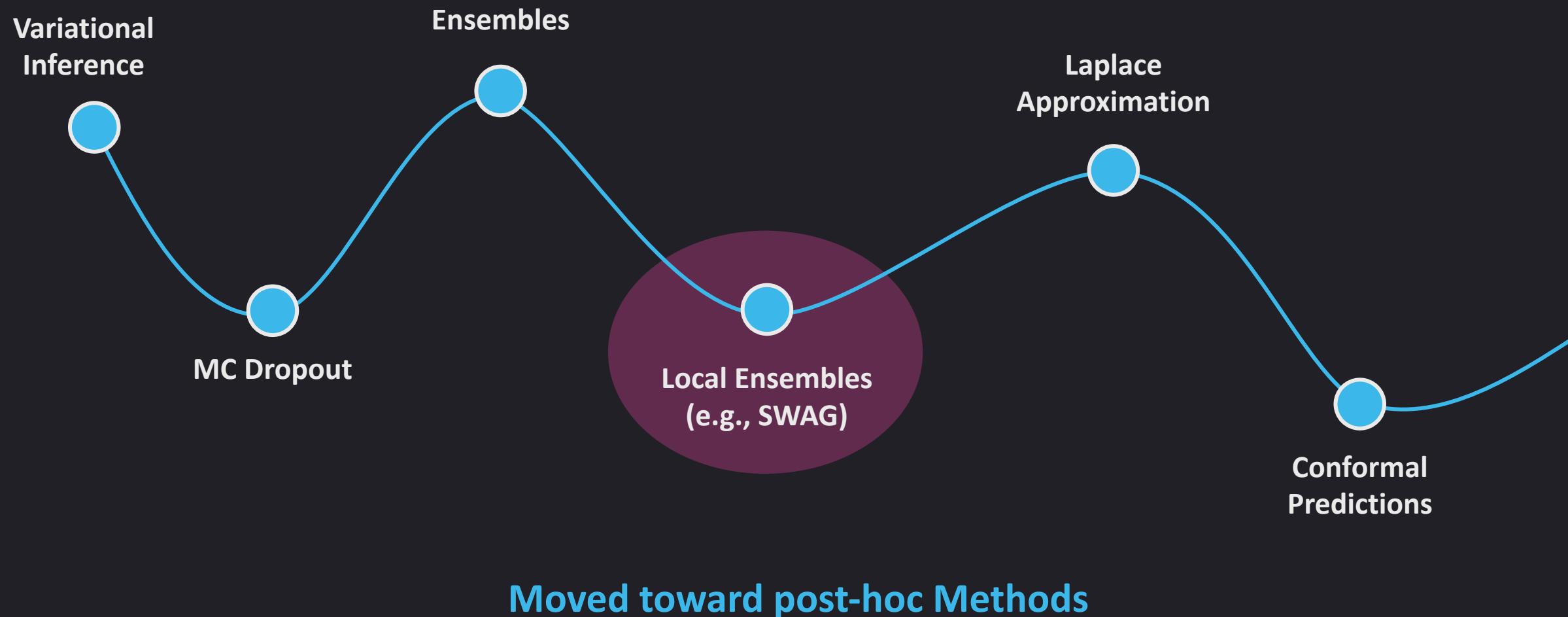


# Methods for Uncertainty Quantification

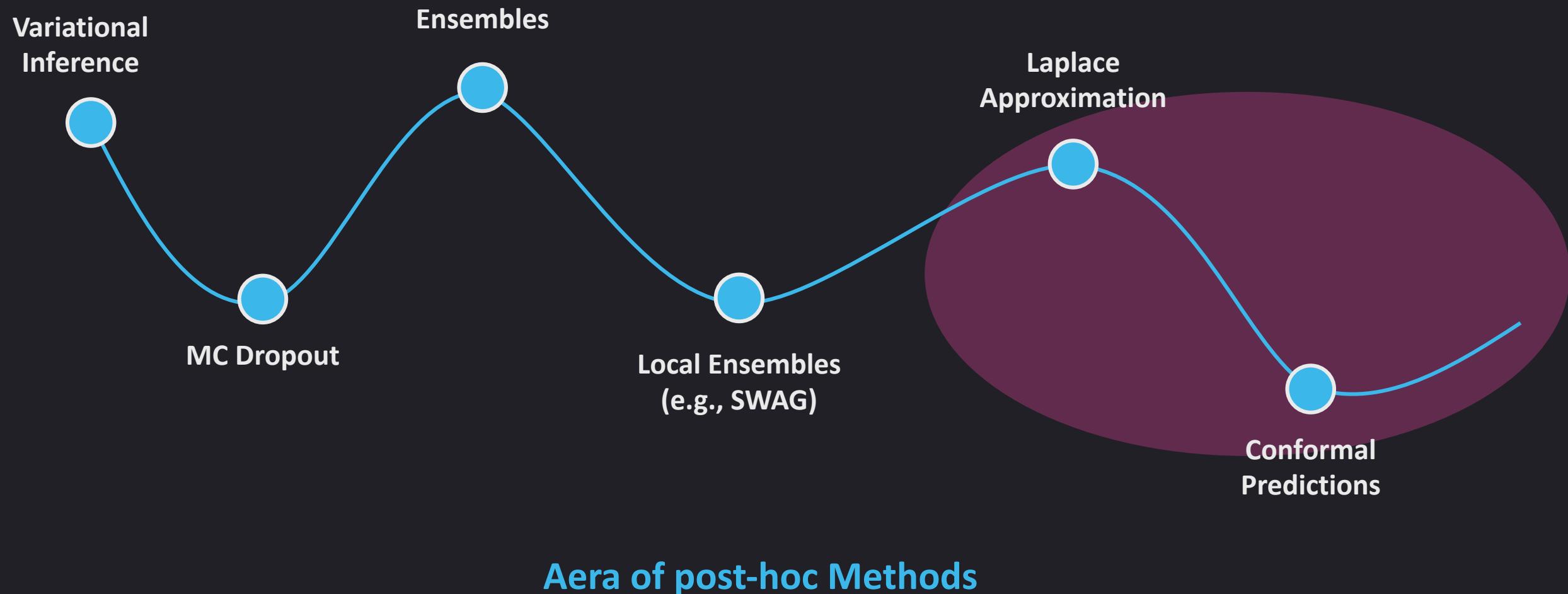


Incorporate UQ into the Training

# Methods for Uncertainty Quantification

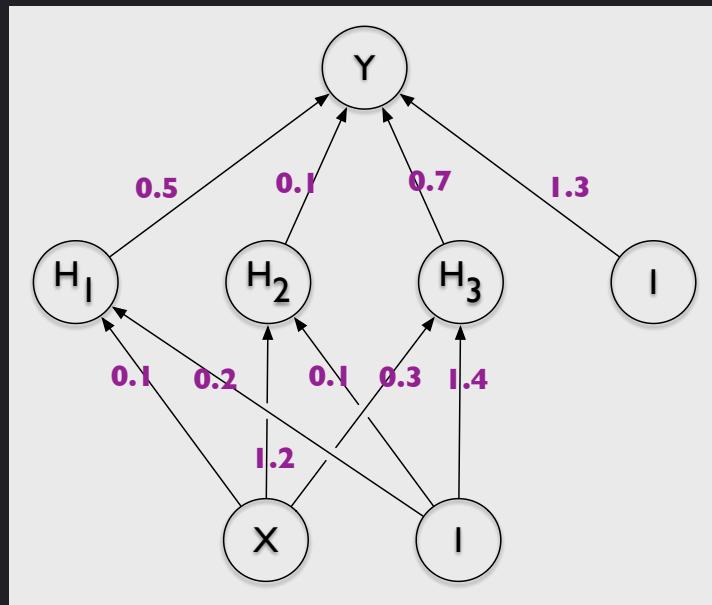


# Methods for Uncertainty Quantification

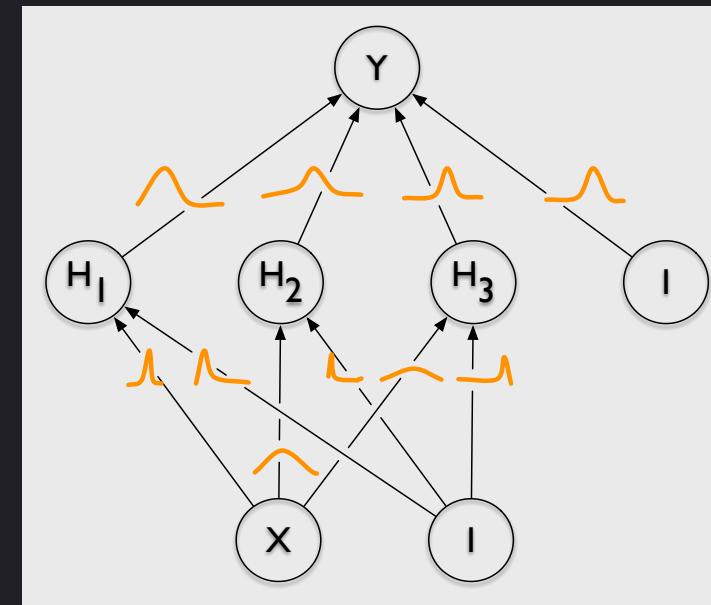


# Bayesian Deep Learning

Standard NN



Bayesian NN



- Weights are **learnable** parameters
- Output is **deterministically** given for any input

- Weights are represented by probability **distributions**
- Parameters of probability distributions are **learnable**
- Output is a **distribution** and not a single value

# Bayesian Deep Learning

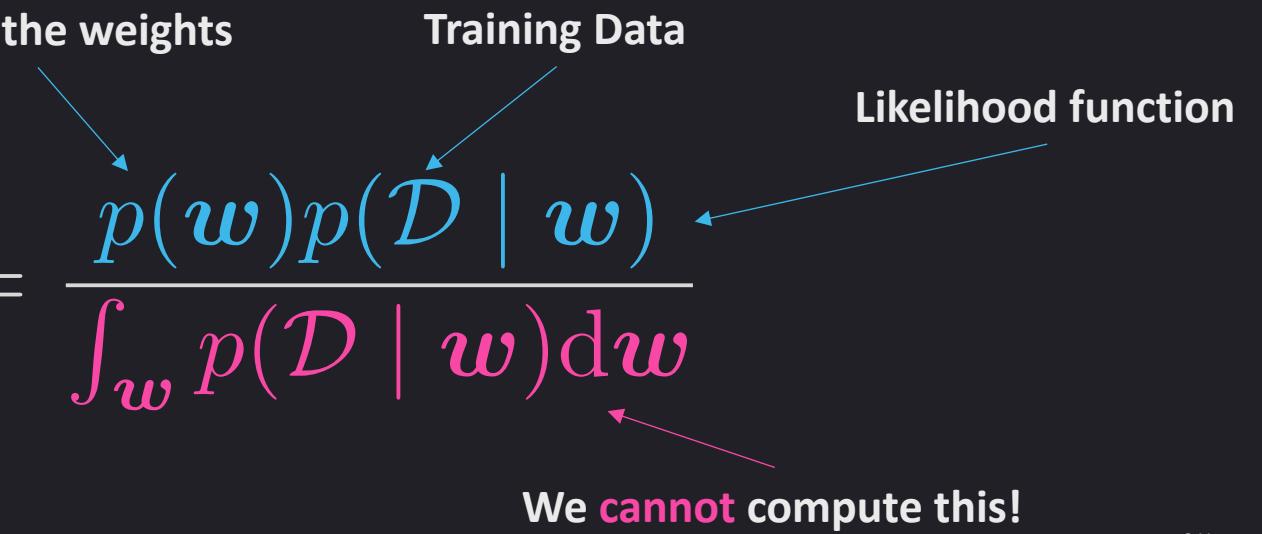
Unfortunately, inference in Bayesian Neural Networks (BNNs) is notoriously hard!

In BNNs we need to perform Bayesian inference (conditioning):

$$p(\mathbf{w} \mid \mathcal{D}) = \frac{p(\mathbf{w})p(\mathcal{D} \mid \mathbf{w})}{\int_{\mathbf{w}} p(\mathcal{D} \mid \mathbf{w})d\mathbf{w}}$$

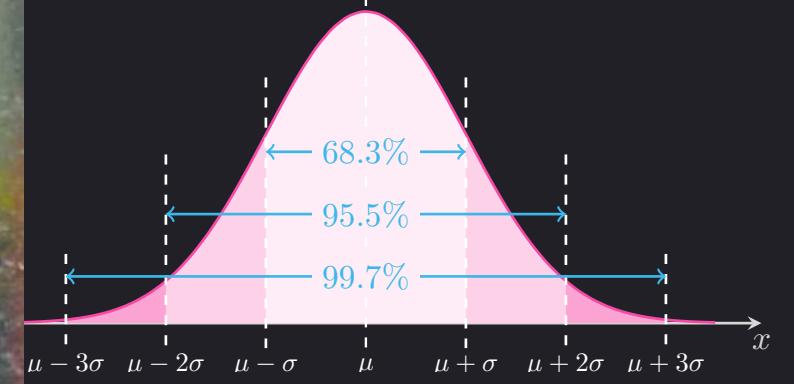
Prior on the weights  
 Training Data  
 Likelihood function  
 We cannot compute this!

Posterior (conditional)  
 Distribution over the  
 Weights





# Laplace Approximation



# Laplace Approximation



# Laplace Approximation

$$p(\mathbf{w} \mid \mathcal{D}) = \frac{p(\mathbf{w})p(\mathcal{D} \mid \mathbf{w})}{\int_{\mathbf{w}} p(\mathcal{D} \mid \mathbf{w}) d\mathbf{w}}$$

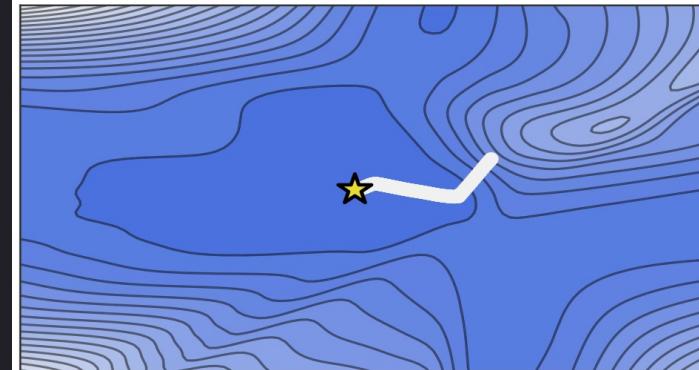
$$\log p(\mathbf{w} \mid \mathcal{D}) = \underbrace{\log p(\mathbf{w})}_{\text{L2 regularization}} + \underbrace{\log p(\mathcal{D} \mid \mathbf{w})}_{\text{Cross-Entropy}} - \underbrace{C}_{\text{Unknown}}$$

Negated Loss

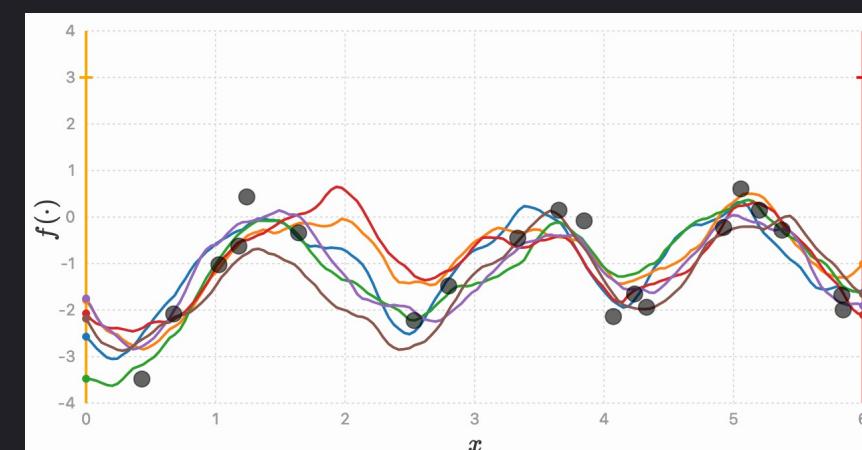
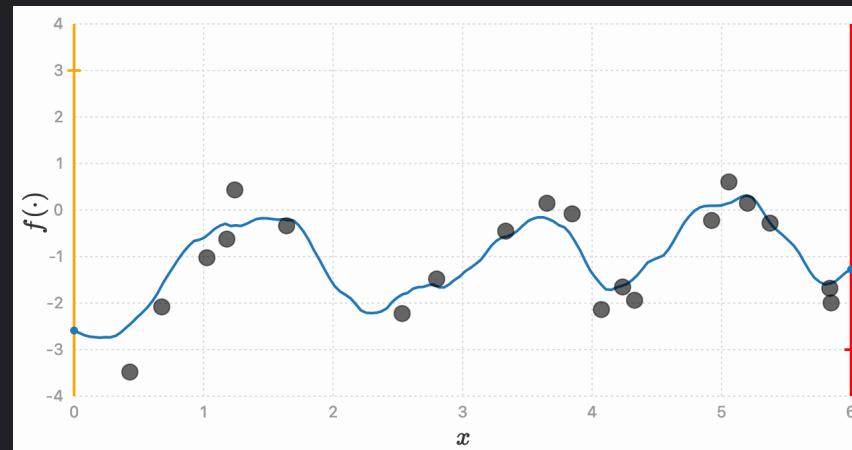
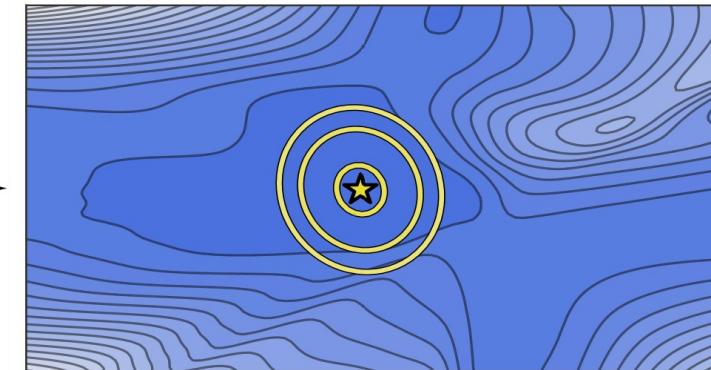
$$\begin{aligned}
 \underbrace{\log p(\mathbf{w}) + \log p(\mathcal{D} \mid \mathbf{w})}_{\ell(\mathbf{w})} &\approx \ell(\mathbf{w}^*) + J_{\ell|_{\mathbf{w}=\mathbf{w}^*}}(\mathbf{w} - \mathbf{w}^*) - \frac{1}{2} H_{\ell|_{\mathbf{w}=\mathbf{w}^*}}(\mathbf{w} - \mathbf{w}^*)^2 \\
 &= \ell(\mathbf{w}^*) - \frac{1}{2} H_{\ell|_{\mathbf{w}=\mathbf{w}^*}}(\mathbf{w} - \mathbf{w}^*)^2 \\
 &\propto \log \mathcal{N}(\mathbf{w}^*, H_{\ell|_{\mathbf{w}=\mathbf{w}^*}}^{-1})
 \end{aligned}$$

# Laplace Approximation

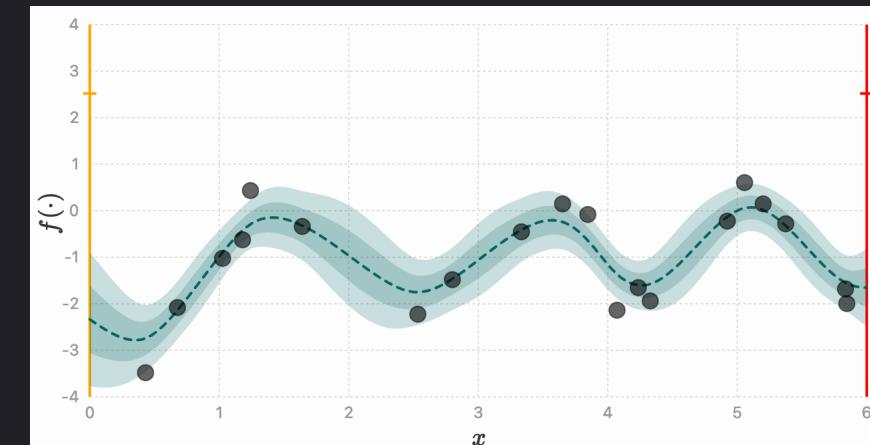
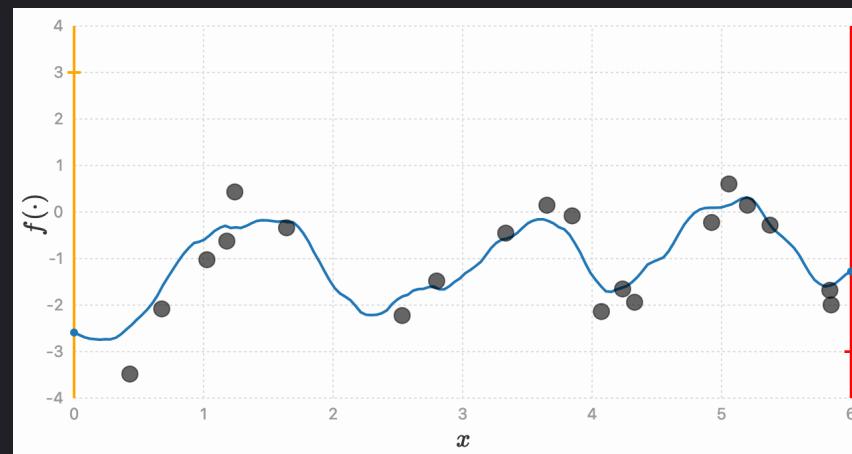
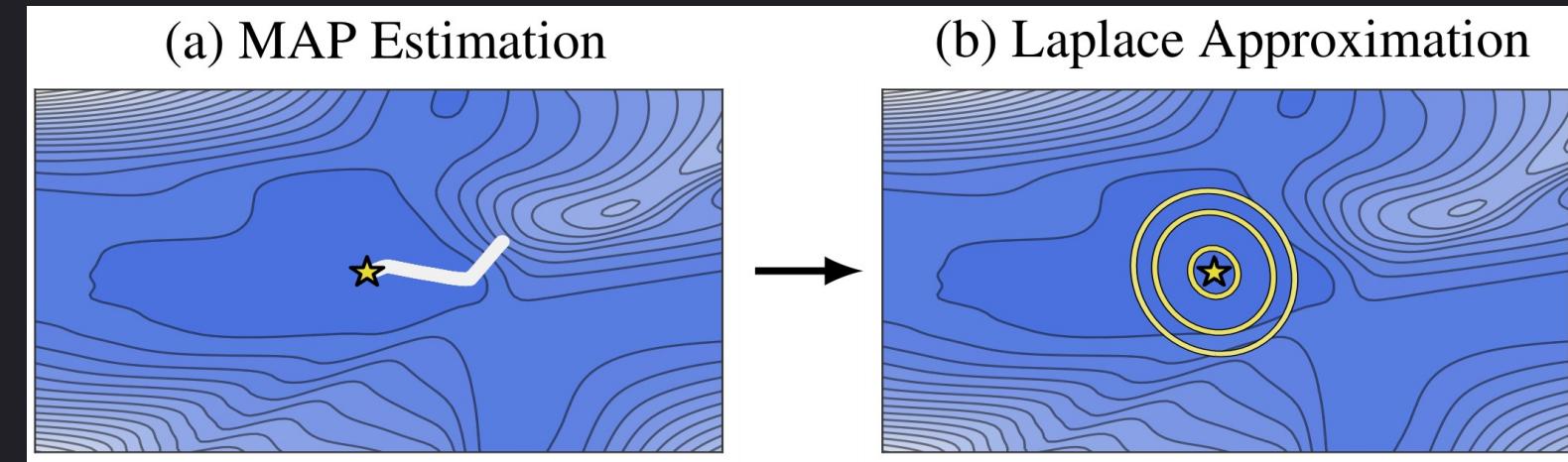
(a) MAP Estimation



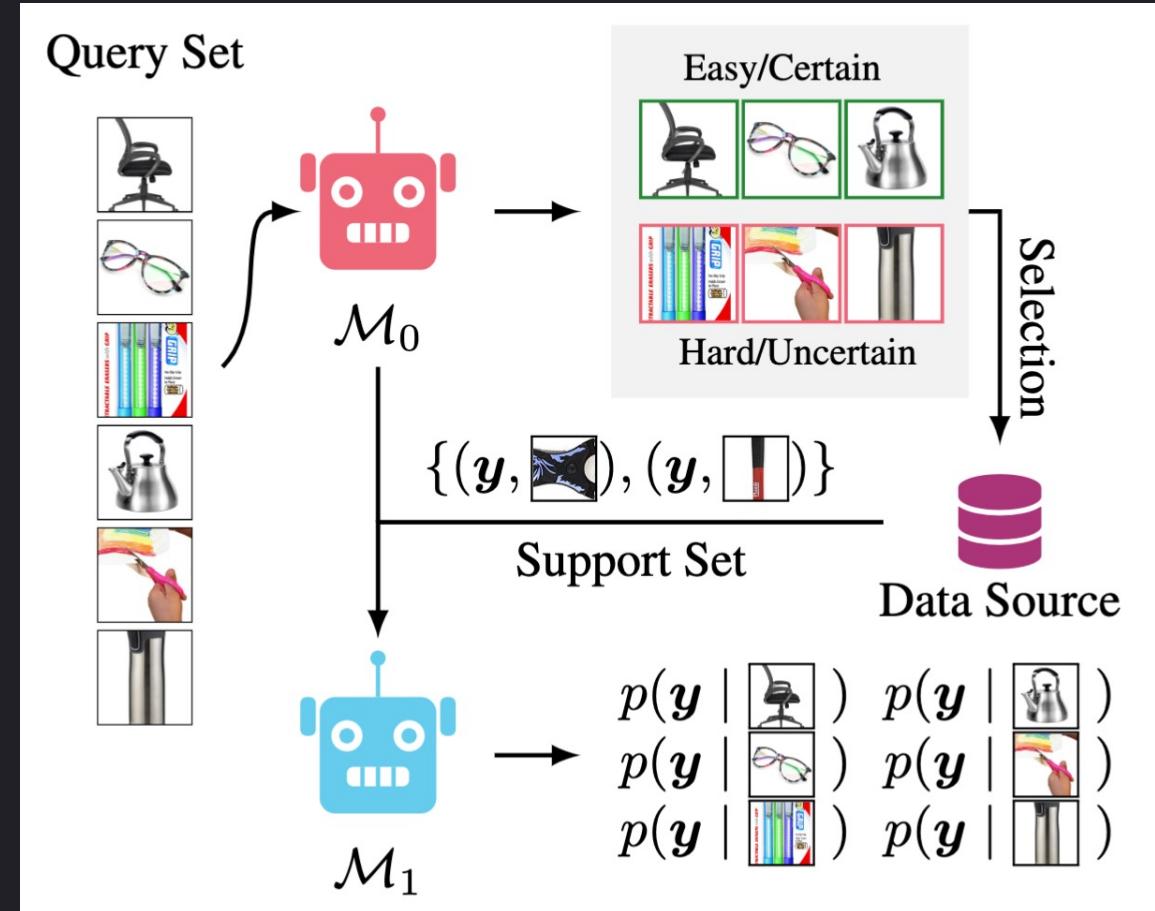
(b) Laplace Approximation



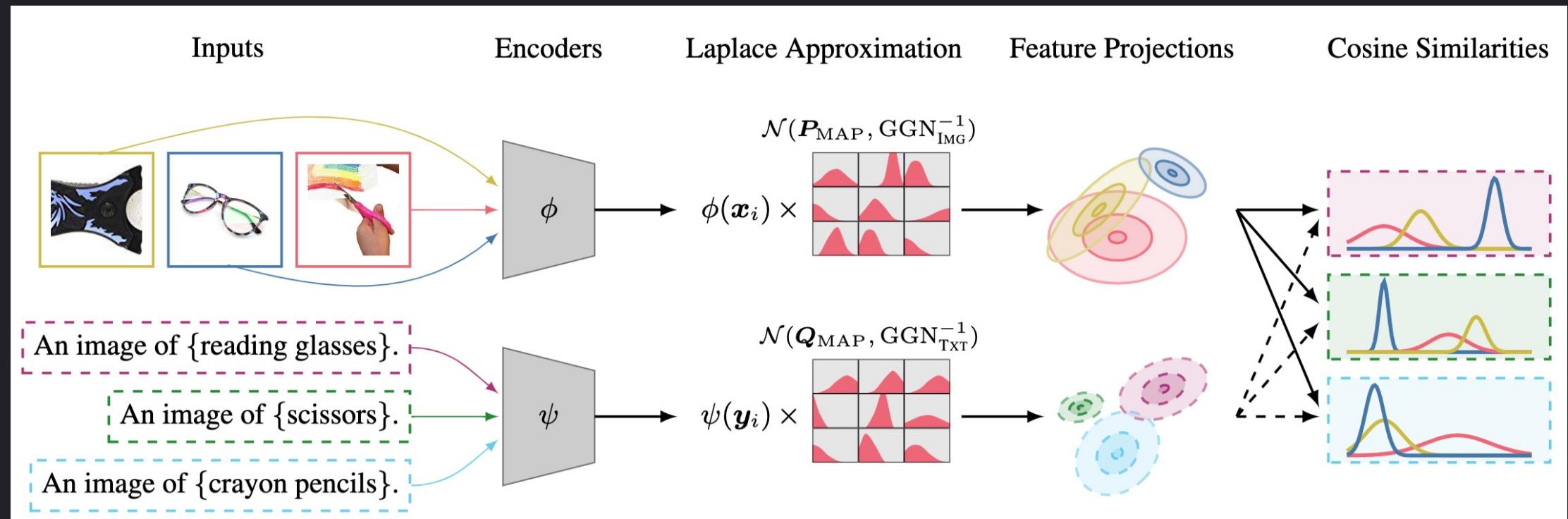
# Laplace Approximation



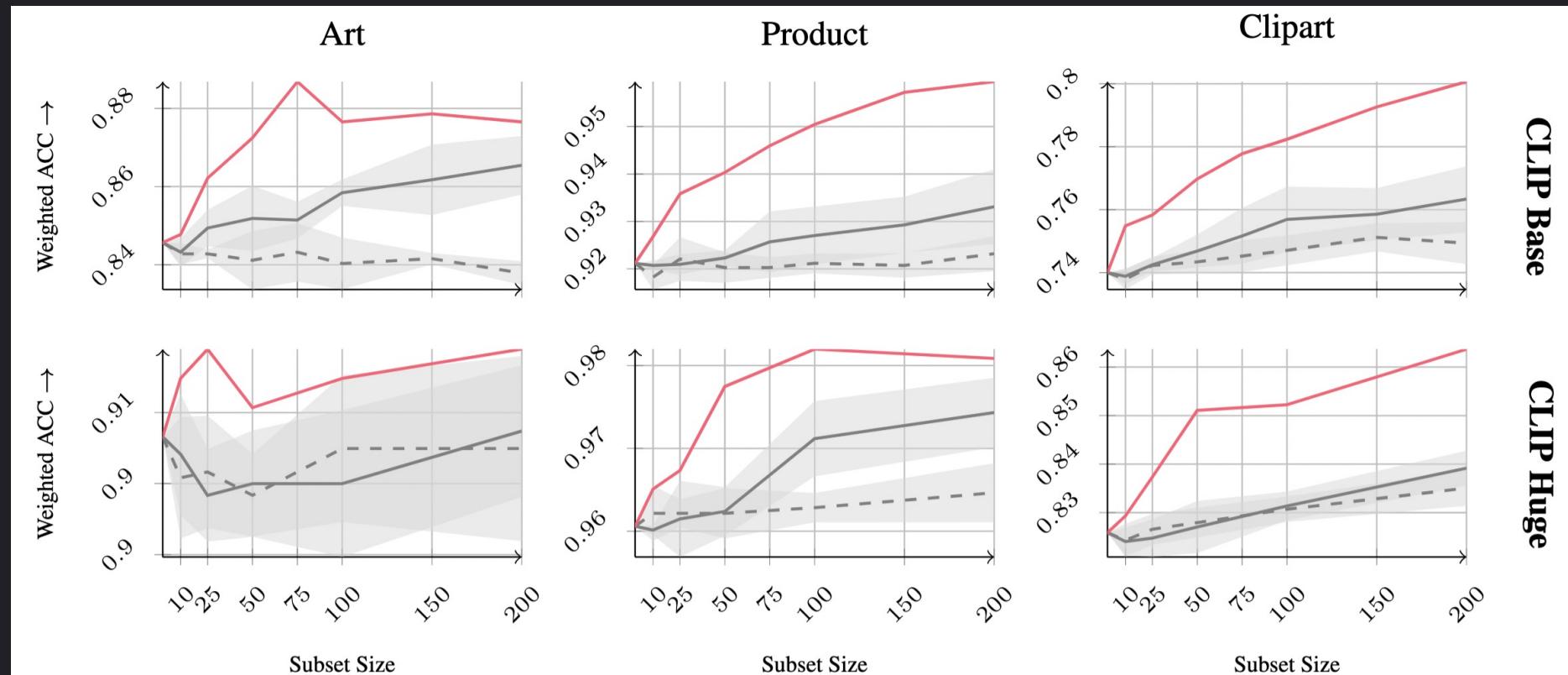
# Probabilistic Active Learning in VLMs



# Probabilistic Active Learning in VLMs



# Probabilistic Active Learning in VLMs



— selection informed by uncertainties  
 - - / — uninformed random/informed random selection

# Streamlining Predictions in BDL



$$p(\mathbf{w} \mid \mathcal{D}) = \frac{p(\mathbf{w})}{\int_{\mathbf{w}} p(\mathbf{w} \mid \mathcal{D}) d\mathbf{w}}$$

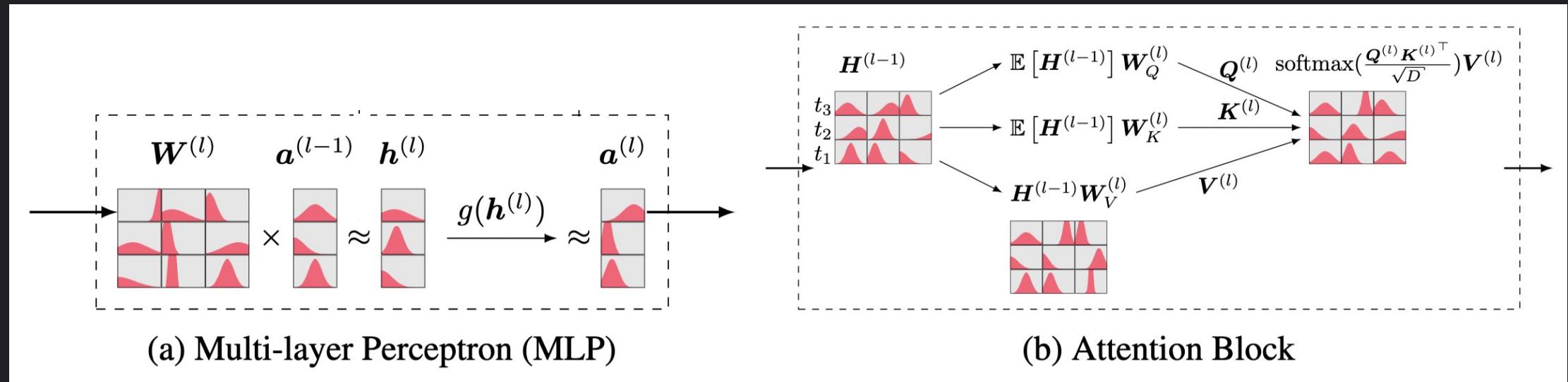
Laplace Approximation

Variational Approximation



$$p(y = c \mid \mathbf{x}^*, \mathcal{D}) = \int_{\mathbf{w}} p(\mathbf{w} \mid \mathcal{D}) p(\mathbf{x}^* \mid \mathbf{w}) d\mathbf{w}$$

# Streamlining Predictions in BDL



# Challenges

- Laplace approximations are local approximations
- Estimating the Hessian matrix is computational demanding (requires approximations)
- Predictions under the linearized Laplace can be expensive to perform
- Somewhat ad-hoc, requires tuning of the prior variance.
- Unclear, what is a good prior on the weights.

Despite those challenges, current tools can already provide useful estimates in many scenarios.

# Ready-Made Libraries

## Python (PyTorch)

- Laplace Redux: <https://github.com/aleximmer/Laplace>

## Julia

- LaplaceRedux.jl:  
<https://github.com/JuliaTrustworthyAI/LaplaceRedux.jl>

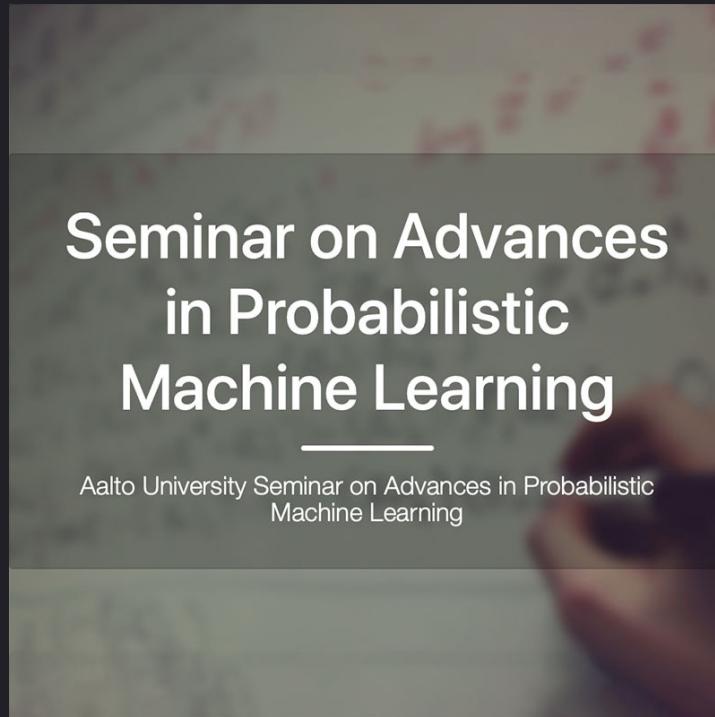
# Conclusion

# Conclusion

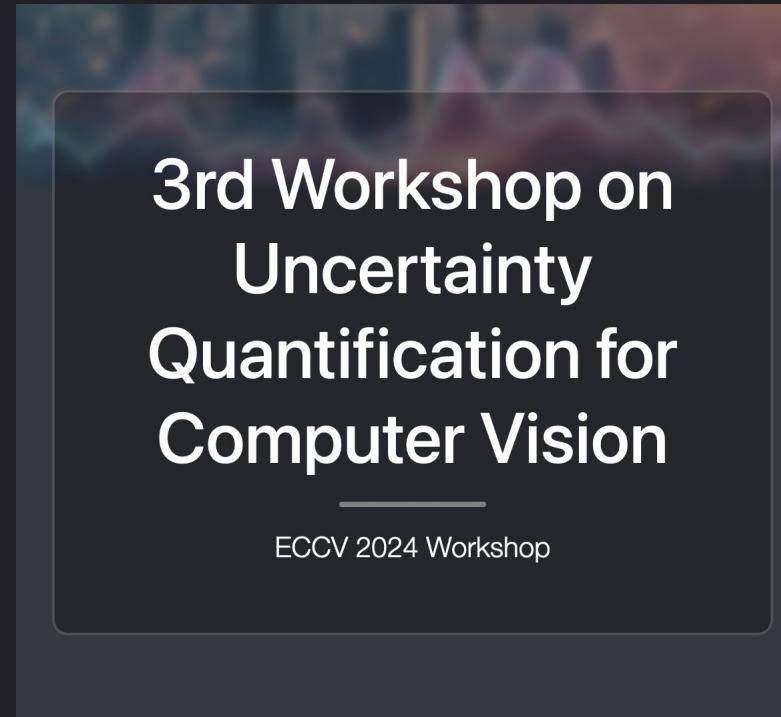
- To get toward reliable ML, we need to account for uncertainties!
- We need to move away from looking only at accuracy!
- Modern (post-hoc) tools can provide useful estimates.

Various open challenges, but the future looks bright!

# Some Advertisement



<https://aaltoml.github.io/apml/>



<https://uncertainty-cv.github.io>

A teal-themed advertisement for a special issue. The title "Special Issue" and subtitle "Advances in Probabilistic Machine Learning" are displayed in white text. The "entropy" journal logo is shown, featuring a stylized blue and white graphic next to the word "entropy".

Guest Editors  
Dr. Martin Trapp and  
Prof. Dr. Pierre Alquier

Deadline  
9 March 2025

IMPACT  
FACTOR  
2.1

Indexed in:  
PubMed

# References (order of appearance) 1/2

- P W Koh *et al.* **WILDS: A Benchmark of in-the-Wild Distribution Shifts.** In ICML, 2021.  
(<https://arxiv.org/abs/2012.07421>)
- S Sabour *et al.* **SpotlessSplats: Ignoring Distractors in 3D Gaussian Splatting.** In ICML, 2021.  
(<https://arxiv.org/abs/2406.20055>)
- A Kristiadi, M Hein, P Hennig. **Being Bayesian, Even Just a Bit, Fixes Overconfidence in ReLU Networks.** In ICML, 2020. (<https://arxiv.org/abs/2002.10118>)
- L Meronen, M Trapp, A Solin. **Periodic activation functions induce stationarity.** In NeurIPS, 2021.  
(<https://arxiv.org/abs/2110.13572>)
- S Roy *et al.* **Uncertainty-guided Source-free Domain Adaptation.** In ECCV, 2022.  
(<https://arxiv.org/abs/2208.07591>)
- L Meronen *et al.* **Fixing Overconfidence in Dynamic Neural Networks.** In WACV, 2024.  
(<https://arxiv.org/abs/2302.06359>)

# References (order of appearance) 2/2

- M Klasson *et al.* **Sources of Uncertainty in 3D Scene Reconstruction**. In UNCV Workshop at ECCV, 2024. (<https://www.arxiv.org/abs/2409.06407>)
- T Broederick *et al.* **Toward a Taxonomy of Trust for Probabilistic Machine Learning**. Science Advances 9, eabn399, 2023. (<https://arxiv.org/abs/2112.03270>)
- C Blundell *et al.* **Weight Uncertainty in Neural Networks**, In ICML 2015. (<https://arxiv.org/abs/1505.05424>)
- E Daxberger *et al.* **Laplace Redux - Effortless Bayesian Deep Learning**. In NeurIPS 2021. (<https://arxiv.org/abs/2106.14806>)
- A Baumann *et al.* **Probabilistic Active Few-Shot Learning in Vision-Language Models**. Under review.
- R Li *et al.* **Posterior Inferred, Now What? Streamlining Prediction in Bayesian Deep Learning**. Under review.