${\bf ASSIGNMENT~1-Voxelization}$

1 Images of Objects

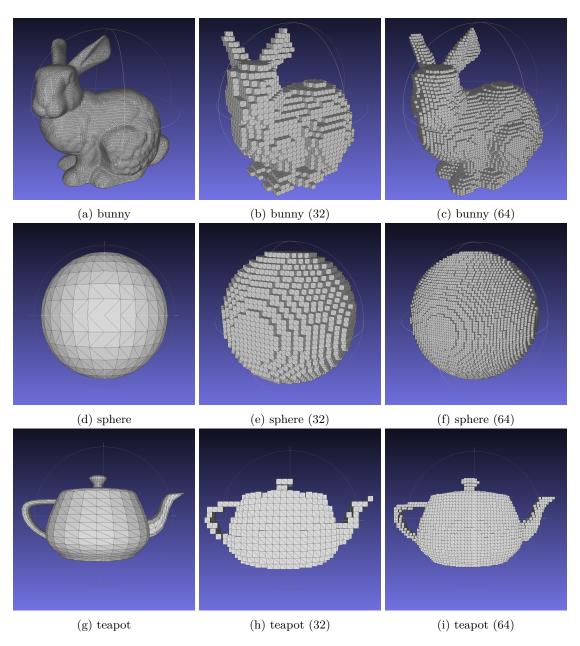


Figure 1: Voxelization

2 References

I was reading on "How to check if ray intersects a triangle" and I found one article from 1997: Fast, Minimum Storage Ray/Triangle Intersection by Moller, T. and Trumbore, B., which provides C implementation to check ray-triangle intersection with face culling and non-culling method. I modified and added some conditions to make it applicable to the C++ voxelizer.

3 Source Code Sample

```
void intersect_tri_2(CompFab::Ray &ray, CompFab::Triangle &triangle,
1
                           int &out, double &t, double &u, double &v) {
2
        // Called by int rayTriangleIntersection(CompFab::Ray &ray,
3
                                                     CompFab::Triangle &triangle);
        //
4
        //
5
        // From https://www.graphics.cornell.edu/pubs/1997/MT97.pdf
6
        // Two-sided face (with two direction option)
        CompFab::Vec3 E1, E2, T, P, Q;
        double det, inv_det;
10
        out = 0;
11
12
        E1 = triangle.m_v2 - triangle.m_v1;
13
        E2 = triangle.m_v3 - triangle.m_v1;
14
        P = ray.m_direction % E2;
17
        det = E1 * P;
18
19
        if (det > -EPSILON && det < EPSILON)</pre>
             return;
21
22
        inv_det = 1.0 / det;
        T = ray.m_origin - triangle.m_v1;
25
26
        u = (T * P) * inv_det;
27
        if (u < 0.0 | | u > 1.0)
28
             return;
29
30
        Q = T \% E1;
31
32
        v = (ray.m_direction * Q) * inv_det;
33
        if (v < 0.0 | | u + v > 1.0)
34
             return;
35
36
        t = (E2 * Q) * inv_det;
37
        // Comment out for bidirectional ray
        if (t < 0)
40
             return:
41
         // End comment
42
        out = 1;
44
45
```

4 Extra Credits

I did extra credits #2 (multi-ray casting) as do-able in this timeframe. I used cumulative bitwise OR to decide whether the voxel is inside or outside the boundary, which I think is naive and prone to errors as I have experimented so far. Here's some of the snippets from the source code involving multi-ray casting option.

```
int main(...) {
2
        CompFab::Vec3 directions[3] = {
3
                 {1., 0., 0.},
                 {0., 1., 0.},
5
                 {0., 0., 1.},
6
        };
7
        for (CompFab::Vec3 &direction: directions) {
                 // Iterating over each voxel
10
             . . .
             }}}
11
12
                 num_hits = numSurfaceIntersections(voxelPos, direction);
13
                 (g_voxelGrid->m_insideArray)[k * (nx * ny) + j * ny + i] |= (num_hits % 2);
14
             }}}
15
16
        }
17
```

In this particular example, I used orthonormal basis (in this case, standard basis): $\{\hat{e}_X, \hat{e}_Y, \hat{e}_Z\}$ I attempted to utilize GPU acceleration via NVIDIA CUDA. I also attempted to implement OpenVDB structure into the program, but there was a lot lot of work to be done.

5 Known Problems

I did not have problems for most parts, but the obvious problem was the program is very slow as number of meshes, number of rays, and grid resolution increase (Overall knr^3). As I was doing one of the extra credits (multi-direction ray test), I used a hollow cylinder model (generated in OpenSCAD) as an input model and I saw artifacts in the output voxelized object. There are also more artifacts present in multi-ray version than uni-ray version. I suspected there were flaws in the multi-ray casting checking logic (cumulative bitwise OR).

For crumbled model, which is a non-closed mesh object with no convex boundary to it, the multi-ray version makes it particularly solid, but that might not exactly be the goal.

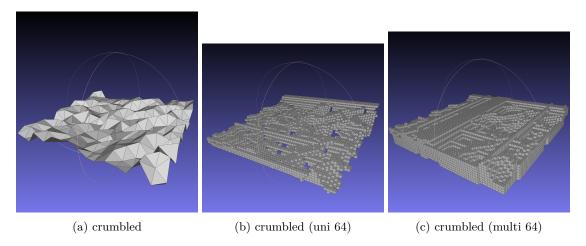


Figure 2: Uni-ray vs Multi-ray: Crumbled

For hollow model, which is a closed mesh object with hole in the middle, there are some artifacts on it. At first, I thought it was the defect from the model file itself, but as I tested more, it might be from the ray casting checking algorithm. Nevertheless, overall results look promising.

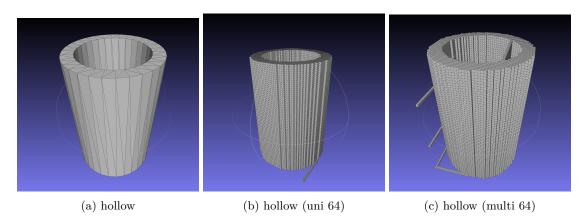


Figure 3: Uni-ray vs Multi-ray: Hollow

If I had more time, I would restudy the multi-ray casting logic and re-implement it in the more correct way.

6 Executable

I have modified parameters for the executable so that it can be tested easily with scripts without recompilation.

Usage: voxelizer <input_mesh_file> <output_mesh_file> <resolution> <multidirection?>

<resolution> Voxelizer grid resolution, e.g., 16, 32, 64

<multidirection?> 0 for uni-directional ray casting
1 for tri-directional ray casting