## Clustering

**LING 570** 

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### Outline

The task

Clustering algorithms

Evaluation measures

• Hw10

#### The task

- Input: A collection of objects
- Output: clusters

- Potential benefits:
  - Document clustering
  - Unsupervised POS tagging
  - Smoothing for LM
  - Generalization (e.g., for MT)

— . . .

## An example

Input: All the words in a language

- Output: word clusters
  - Ex: Mon, Tues, Wed, ...
  - Ex: Mike, Bryan, Joshua, ...
  - Ex: claim, announce, declare, ...
  - Ex: politicians, lawyers, salesmen, ...

## Another example

Input: A collection of documents

- Output: document clusters
  - sports, politics, business, travel, ...
  - docs with the similar style: e.g., news, chat room, talk shows, …
  - docs written by similar kinds of authors
  - docs focusing on the same topic

#### Questions

- What should a cluster represent?
  - Two objects are similar.

How can we find good clusters?

How can one evaluate clustering results?

How can one benefit from clustering?

# Similarity

Between two instances

Between an instance and a cluster

Between two clusters

## Some similarity functions

$$p = (p_1, p_2, ..., p_n)$$
 and  $q = (q_1, q_2, ..., q_n)$ 

Euclidean distance:

$$dist(p,q) = \sqrt{\sum_{i}(p_i - q_i)^2}$$

Cosine similarity:

$$cos(\theta) = \frac{\sum_{i} p_{i} q_{i}}{\sqrt{\sum_{i} p_{i}^{2}} \sqrt{\sum_{i} q_{i}^{2}}}$$

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## Types of clustering algorithms

- Flat vs. hierarchical clustering
  - Flat: partition n objects into k clusters
  - Hierarchical: create a hierarchy

- Hard vs. soft clustering
  - Hard clustering: each instance belongs to one cluster
  - Soft clustering: an instance can belong to multiple clusters (e.g., with different costs)

#### K-means vs. k-medoids

 k-means (MacQueen, 1967): Each cluster is represented by the center of the cluster

 k-medoids (Kaufman & Rousseeuw, 1987): Each cluster is represented by the medoid of the cluster

## K-means algorithm

Select k initial centroids at random.

- Repeat until there is no more change
  - Assign each object to the cluster with the nearest centroid.
  - Compute each centroid as the mean of the objects assigned to it.

## K-means (cont)

- Relatively efficient: O(t k n)
  - t: number of iteration
  - k: number of clusters
  - n: number of objects
- Need to specify k
- Often terminates at a local optimum
- Applicable only when mean is defined (what about categorical data?)
- Trouble with noisy data and outliers

## K-medoids algorithm

Select k objects as the initial medoids

- Repeat until the medoids do not change
  - Assign each object to the cluster with the nearest medoid.
  - Find the new medoid for each cluster

#### Find the medoid of a cluster

 A medoid is an object in a cluster whose average dissimilarity to all the objects in the cluster is minimal.

- To find the medoid in a cluster
  - for each p, calculate  $f(p) = \sum_{q} sim(p, q)$
  - choose p with the highest f(p).

# Hierarchical clustering: Greedy, bottom-up approach

Initialization: Create a separate cluster for each object

- Repeat until all the objects are in the same cluster:
  - Find two most similar clusters and merge

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#### **Evaluation**

- When compared with a gold standard
  - Rand index
  - Precision/recall
  - Variation of information

- Other methods:
  - Task-based evaluation
  - Human inspection

## The setting

• Given a set of objects  $S = \{O_1, ..., O_n\}$ 

- Partition  $X = \{x_1, x_2, ..., x_r\}$
- Partition  $Y = \{y_1, y_2, ..., y_r\}$

	In the same set in X	In different sets in X
In the same set in Y	а	d
In different sets in Y	С	b

#### Rand index

http://en.wikipedia.org/wiki/Rand\_index

	In the same set in X	In different sets in X
In the same set in Y	а	d
In different sets in Y	С	b

 Rand index calculates how well the two partitions agree.

$$R = \frac{a+b}{a+b+c+d} \qquad R \in [0,1]$$

#### Precision and recall

 Treat one partition as gold standard, and the other as system output

 For each pair in a set in the system partition, check whether it appears in one set in the gold standard

Calculate precision, recall, and f-score.

#### Variations of information

 http://en.wikipedia.org/wiki/Variation\_of\_inf ormation

$$VI(X,Y) = H(X) + H(Y) - 2*MI(X,Y)$$

$$H(X) = -\sum_{x} P(x)logP(x)$$

$$MI(X;Y) = \sum_{x} \sum_{y} P(x,y) log \frac{P(x,y)}{P(x)P(y)}$$

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#### **Hw10**

- Unsupervised POS tagging
  - One method: clustering words
- Features: the previous words and the next words
  - Ex: "book L=the 15 R=of 3 …"
- Clustering algorithm: k-medoids algorithm (with cosine as the similarity function)
- Evaluation: tagging accuracy after mapping sys clusters to clusters in gold standard

## Q1: create\_vector.sh

 create\_vector.sh train\_file output\_file word\_list feat\_list

- train\_file: w1 w2 ...
- word\_list: word freq
- feat\_list: word freq
- output\_file: word fn1 fv1 fn2 fv2 ...

#### "fn1 fv1"

- fn:
  - Format: featidx\_(L|R)=x
  - Ex: "new york" appears 919 times, and "new" is the 37<sup>th</sup> feature (i.e., appearing on the 38<sup>th</sup> line) in the feature file.
    - → "york .... 37\_L=new 919"
- fv:
  - The occurrence of the bigrams
  - Ex: "york ... 37\_L=new 919 ...137\_R=new 0 ..."

#### The order of vector file

Lines are sorted by the order in word\_list

• (fn, fv) pairs are sorted by feature index.

```
has 0_L=, 260 7_L=and 69 8_L='s 12 ... 100_R=, 5 101_R=the 55 102_R=. 4 103_R=of 3 ...
```

- Why do we need to sort features?
  - It can make the calculation of cosine faster.

#### Q2: k-medoids.sh

 k-medoids.sh vector\_file cluster\_size sys\_cluster

- vector\_file is created in Q1
- cluster\_size is an integer
- sys\_cluster:
  - "medoid word1 word2 ..."
  - medoid serves as the name of the cluster

### Q2: k-medoids.hs

similarity function: cosine

#### initial medoids:

The i-th medoid is at line  $x = (i-1) * \lfloor N/C \rfloor$ 

N is the number of vectors, C is the number of clusters.

Ex: N=100, C=34, |N/C|=2

Initial medoids are at line 0, 2, 4, ..., 66.

# Mapping sys cluster to gold cluster: greedy one-to-one

	g1	g2	g3
s1	2	10	9
s2	7	4	2
s3	0	9	6
s4	5	0	3

- (1) find the largest number in the matrix
- (2) remove both the row and the column
- (3) repeat (1)-(2) until no more row left

$$s1 \Rightarrow g2 = 10$$
 Acc= $(10+7+6)$ /sum  
 $s2 \Rightarrow g1 = 7$   
 $s3 \Rightarrow g3 = 6$ 

# Mapping sys cluster to gold cluster: greedy many-to-one

	g1	g2	g3
s1	2	10	9
s2	7	4	2
s3	0	9	6
s4	5	0	3

- (1) find the largest number
- (2) remove the row, but not the column
- (3) repeat (1)-(2) until no more row left.

$$s1 => g2 10$$

$$s3 => g2$$
 9

$$s2 => g1$$
 7

$$s4 => g1$$
 5

### Q3: calc\_acc.sh

- calc\_acc.sh gold\_cluster sys\_cluster flag > map\_file
   2>acc\_file
- gold\_cluster: "cluster\_name w1 w2 ..."
- sys\_cluster: "medoid w1 w2 ..."
- flag:
  - 0: one-to-one mapping
  - 1: many-to-one mapping
- map\_file: "sys\_cluster => gold\_cluster cnt"
- acc\_file: Acc=xx

## Q4: wrapper.sh

 wrapper.sh train\_file word\_list feawt\_list cluster\_size gold\_cluster output\_dir

- output\_dir:
  - vectors: created by Q1
  - sys\_cluster: created by Q2
  - res.\*.map and res.\*.acc: created by Q3

## Q5: Fill out a table

word	feat	cluster	gold	output	1-to-1	many-to-1	running
list	list	size	cluster	dir	Acc	Acc	time
word.100	word.100	34	gold.100	100-100-34			
word.100	word.500	34	gold.100	100-100-34			
word.500	word.100	36	gold.500	500-100-36			
word.500	word.500	36	gold.500	500-500-36			
word.1000	word.100	39	gold.1000	1K-100-39			
word.1000	word.500	39	gold.1000	1K-500-39			
word.5000	word.100	41	gold.5000	5K-100-41			
word.5000	word.500	41	gold.5000	5K-500-41			

## Calculating cosine function

$$cos(\theta) = \frac{\sum_{i} p_{i} q_{i}}{\sqrt{\sum_{i} p_{i}^{2}} \sqrt{\sum_{i} q_{i}^{2}}}$$
$$= \sum_{i} \frac{p_{i}}{\sqrt{\sum_{i} p_{i}^{2}}} \frac{q_{i}}{\sqrt{\sum_{i} q_{i}^{2}}}$$