

# ACM 模板

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#### **FastIO**

```
namespace fastio {
     const static int buf_size = 8388608;//about 8Mb
     static char buf[buf_size];
     char *ps = buf + buf_size, *pe = buf + buf_size;
     int pos;
     bool eof = false;
     inline void read_next() {
          pe = buf + fread(buf, 1, buf_size, stdin);
          ps = buf;
          if(ps == pe) eof = true;
    }
     inline bool blank(char x) {
          return x == ' ' || x == '\n' || x == '\t' || x == '\r';
    }
     inline char nc() {
          if(ps == pe) read_next();
          return *ps++;
     }
     template<typename T>
     inline void read_num(T& res) {
          bool neg = false;
          char now = nc();
          while(blank(now)) now = nc();
          if(now == '-') {
               neg = true;
               now = nc();
          }
          T ret = 0;
          while(!blank(now)) {
               ret = ret * 10 + now - '0';
               now = nc();
          res = (neg ? -ret : ret);
     }
     template<typename T>
     inline void put_num(T x) {
          if(x < 0) {
```

```
putchar('-');
               x = -x;
          }
          if(x == 0) {
                putchar('0');
          }
          char tmp[32];
          int cnt = 0;
          while(x) {
               tmp[cnt++] = x \% 10 + '0';
               x /= 10;
          }
          while(cnt > 0) {
                putchar(tmp[cnt - 1]);
               --cnt;
          }
     }
}
```

## 计算几何基础

```
const double eps = 1e-10;
const double PI = 3.141592653589793;
double sqr(double x) { return x * x; }
int cmp(double x, double y)
{
     if(fabs(x - y) < eps) return 0;
     return (x < y) ? -1:1;
}
struct Point {
     double x, y;
     Point(double _x = 0, double _y = 0) : x(_x), y(_y) {}
     friend istream& operator>>(istream& is, Point& p) {
          is >> p.x >> p.y;
          return is;
     }
     bool operator<(Point rhs) const {</pre>
          return cmp(x, rhs.x) < 0 | | (cmp(x, rhs.x) == 0 && cmp(y, rhs.y) < 0);
     }
     bool operator==(Point rhs) const {
          return cmp(x, rhs.x) == 0 \&\& cmp(y, rhs.y) == 0;
```

```
}
     bool operator!=(Point rhs) const {
           return !(*this == rhs);
     }
};
struct Vector {
     double x, y;
     Vector(double \underline{x} = 0, double \underline{y} = 0) : x(\underline{x}), y(\underline{y}) {}
     Vector(Point s, Point t) : x(t.x - s.x), y(t.y - s.y) {}
     Vector operator+(Vector other) {
           return Vector(x + other.x, y + other.y);
     }
     Vector operator-(Vector other) {
           return Vector(x - other.x, y - other.y);
     }
     Vector operator*(double k) {
           return Vector(x * k, y * k);
     }
     double len2() const {
           return x * x + y * y;
     }
     double length() const {
           return sqrt(x * x + y * y);
     }
     Vector norm() const {
           double len = length();
           assert(len != 0);
           return Vector(x / len, y / len);
     }
     friend Vector operator*(double k, Vector other) {
           return other * k;
     }
     friend double dot(Vector lhs, Vector rhs) {
           return lhs.x * rhs.x + lhs.y * rhs.y;
     }
```

```
friend double cross(Vector lhs, Vector rhs) {
                                return lhs.x * rhs.y - rhs.x * lhs.y;
               }
               friend istream& operator>>(istream& is, Vector& v) {
                                cin >> v.x >> v.y;
                                return is;
                }
};
struct Line {
                Point o;
                Vector dir;
                Line() {}
                Line(Point x, Point y) : o(x), dir(x, y) {}
                Line(Point _o, Vector _d) : o(_o), dir(_d) {}
                friend Point getCrossPoint(Line lhs, Line rhs) {
                                assert(cmp(cross(lhs.dir, rhs.dir), 0.0) != 0);
                                Vector u(rhs.o, Ihs.o);
                                double t = cross(rhs.dir, u) / cross(lhs.dir, rhs.dir);
                                Vector dt = lhs.dir * t;
                                return Point(lhs.o.x + dt.x, lhs.o.y + dt.y);
               }
};
bool sameDir(Vector a, Vector b) {
                return cmp(dot(a, b), 0) > 0 && cmp(cross(a, b), 0) == 0;
}
bool parallel(Line a, Line b) {
                return cmp(cross(a.dir, b.dir), 0) == 0;
}
bool onSeg(Point a, Point b, Point c) {
                return c.x >= min(a.x, b.x) \&\& c.y >= min(a.y, b.y) \&\& c.x <= max(a.x, b.x) \&\& c.y <= max(a.y, b.y) && c.x <= max(a.x, b.x) && c.y <= max(a.y, b.y) 
b.y) &&
                cmp(cross(Vector(c, a), Vector(c, b)), 0) == 0;
}
double Length(Vector x) {
                return sqrt(x.x * x.x + x.y * x.y);
```

```
}
Vector rotate(Vector v, double cost, double sint) {
     double vx = cost * v.x - sint * v.y;
     double vy = sint * v.x + cost * v.y;
     return Vector(vx, vy);
}
Vector rotate(Vector v, double rad) {
     double c = cos(rad), s = sin(rad);
     return rotate(v, c, s);
}
double getAngle(Vector x, Vector y) {
     double dt = dot(x, y);
     return acos(dt / (Length(x) * Length(y)));
}
double toRad(double ang) {
     return ang / 180 * PI;
}
```

## 圆基础

```
struct Circle {
     const double PI = 3.141592653589793;
     Point c;
     double r;
     Circle(Point \_c, double \_r) : c(\_c), r(\_r) \{\}
     Circle(Point x, Point y, Point z) {
           Point cxy(0.5 * (x.x + y.x), 0.5 * (x.y + y.y));
           Point cyz(0.5 * (y.x + z.x), 0.5 * (y.y + z.y));
           Vector xy(x, y), yz(y, z);
           Vector nxy(-xy.y, xy.x), nyz(-yz.y, yz.x);
           c = getCrossPoint(Line(cxy, nxy), Line(cyz, nyz));
           r = Vector(c, x).length();
     }
     double area() const {
           return PI * sqr(r);
     }
```

```
friend void getCrossPoint(Circle a, Circle b, Point* ps, int& cnt) {
          if(a.c == b.c) return;
          int cdis2 = Vector(a.c, b.c).len2();
          int tp1 = cmp(cdis2, sqr(a.r + b.r));
          int tp2 = cmp(cdis2, sqr(a.r - b.r));
          cnt = 0;
          if(tp1 == 1 | | tp2 == -1) return;
          Vector ab(a.c, b.c);
          double cost = 0.5 * (sqr(a.r) + ab.len2() - sqr(b.r)) / (ab.length() * sqr(a.r));
          double sint = sqrt(1 - sqr(cost));
          Vector v1 = rotate(ab, cost, sint).norm();
          ps[cnt++] = Point(v1.x * a.r, v1.y * a.r);
          if(tp1 == 0 || tp2 == 0) return;
          Vector v2 = rotate(ab, cost, -sint).norm();
          ps[cnt++] = Point(v2.x * a.r, v2.y * a.r);
     }
};
```

### 凸包

```
int ConvexHull(Point* in, Point* out, int n) {
     sort(in, in + n);
     n = unique(in, in + n) - in;
     int m = 0;
     for(int i = 0; i < n; ++i) {
          while(m > 1 &\& cmp(cross(Vector(out[m - 2], out[m - 1]), Vector(out[m - 2], in[i])), 0) <=
0) --m;
          out[m++] = in[i];
     }
     int k = m;
     for(int i = n - 2; i >= 0; --i) {
          while(m > k \&\& cmp(cross(Vector(out[m - 2], out[m - 1]), Vector(out[m - 2], in[i])), 0) <=
0) --m;
          out[m++] = in[i];
     }
     if(n > 1) --m;
     return m;
}
double getArea(Point* p, int n) {
     double area = 0.0;
     for(int i = 2; i < n; ++i) {
          area += cross(Vector(p[0], p[i - 1]), Vector(p[0], p[i]));
```

```
}
     return 0.5 * area;
}
int inPolygon(Point o, Point p[], int n) {
     int w = 0;
     for(int i = 0; i < n; ++i) {
           if(onSeg(p[i], p[(i + 1) \% n], o)) return -1;//on
           int k = cmp(cross(Vector(p[i], p[(i + 1) % n]), Vector(p[i], o)), 0);
           int d1 = cmp(p[i].y - o.y, 0);
           int d2 = cmp(p[(i + 1) \% n].y - o.y, 0);
           if(k > 0 \&\& d1 <= 0 \&\& d2 > 0) ++w;
           if(k < 0 && d2 <= 0 && d1 > 0) --w;
     }
     if(w != 0) return 1;//in
     return 0;//out
}
```

## 并查集

```
namespace UFS {
     const int N = 1e5 + 10;
     int fa[N];
     inline void init() { memset(fa, 0xff, sizeof(fa)); }
     inline int id(int u) {
           int rt = u;
           while(fa[rt] > 0) rt = fa[rt];
           while(fa[u] > 0) { int tmp = fa[u]; fa[u] = rt; u = tmp; }
           return rt;
     }
     inline void join(int u, int v) {
           int uf = id(u);
           int vf = id(v);
           if(uf != vf) {
                 if(fa[uf] < fa[vf]) { fa[uf] += fa[vf]; fa[vf] = uf; }
                 else { fa[vf] += fa[uf]; fa[uf] = vf; }
           }
     }
     inline int size(int u) { return -fa[id(u)]; }
};
```

```
struct ST {
     //1 base, query O(1)
     int dp[50005][20];
     int n;
     int arr[50005];
     void make(int _n) {
           assert(n < 50005);
           n = _n;
           for(int i = 1; i \le n; ++i) {
                 dp[i][0] = arr[i];
           }
           for(int j = 1; (1 << j) <= n; ++j) {
                 for(int i = 1; (i + (1 << (j - 1))) <= n; ++i) {
                      dp[i][j] = min(dp[i][j-1], dp[i+(1 << (j-1))][j-1]);
                 }
           }
     }
     int query(int I, int r) {
           int k = 31 - \underline{\quad }builtin_clz(r - l + 1);
           return min(dp[l][k], dp[r - (1 << k) + 1][k]);
     }
} st;
```

## 锛表

```
template<typename T>
struct ACM_list {
    static const int MAXN = 100005;
    static const int BEG = 0;
    static const int END = MAXN - 1;
    struct Node {
        T data;
        int next;
        int pre;
    } node[MAXN];
    int free[MAXN], fp;
    int sz;

void init() {
        node[BEG] = {T{}, END, -1};
        node[END] = {T{}, -1, BEG};
```

```
fp = MAXN - 3;
     for(int i = 0; i \le fp; ++i) {
          free[i] = i + 1;
     }
     sz = 0;
}
int ins_back(int idx, T val) {
     node[free[fp]].next = node[idx].next;
     node[free[fp]].data = val;
     node[free[fp]].pre = idx;
     node[idx].next = free[fp];
     node[node[free[fp]].next].pre = free[fp];
     return free[fp--];
}
int ins_pre(int idx, T val) {
     idx = node[idx].pre;
     return ins_back(idx, val);
}
void del(int idx) {
     assert(idx != BEG && idx != END);
     node[node[idx].pre].next = node[idx].next;
     node[node[idx].next].pre = node[idx].pre;
     free[++fp] = idx;
     --SZ;
}
Node& operator[](int idx) {
     return node[idx];
}
int begin() const {
     return node[BEG].next;
}
int end() const {
     return END;
}
int size() const {
     return sz;
}
```

**}**;

struct Bit {

## 树状数组

```
//1 Base
     int arr[300005];
     int n;
     int lowbit(int x) { return x & (-x); }
     void add(int i, int x) {
          int pos = i;
          while(pos <= n) {
                arr[pos] += x;
                pos += lowbit(pos);
          }
     }
     int sum(int i) {
          int pos = i, ans = 0;
          while(pos) {
               ans += arr[pos];
                pos -= lowbit(pos);
          }
          return ans;
     }
     void init(int _n) {
          n = _n;
          for(int i = 1; i <= n; ++i) {
                arr[i] += sum(i - 1) - sum(i - lowbit(i));
          }
     }
} bit;
                                                 LCA
const int VN = 50000, EN = 100000;
struct ST {
     //1 base, query O(1)
```

```
int dp[VN << 1][20];
     int n;
     int arr[VN << 1];
     void make(int _n) {
           n = _n;
           for(int i = 1; i \le n; ++i) {
                 dp[i][0] = i;
           }
           for(int j = 1; (1 << j) <= n; ++j) {
                 for(int i = 1; (i + (1 << (j - 1))) <= n; ++i) {
                      int I = dp[i][j-1], r = dp[i+(1 << (j-1))][j-1];
                      dp[i][j] = arr[l] < arr[r] ? I : r;</pre>
                }
           }
     }
     int query(int I, int r) {
           int k = 31 - \underline{\quad } builtin_clz(r - l + 1);
           int li = dp[l][k], ri = dp[r - (1 << k) + 1][k];
           return arr[li] < arr[ri] ? li : ri;
     }
} st;
struct edge {
     int to, cost, next;
     edge() {}
     edge(int _to, int _cost, int _next) : to(_to), cost(_cost), next(_next) {}
} eg[EN];
int head[VN], dis[VN], id[VN], la[VN << 1], lacnt, tot;
bool vis[VN];
void init() {
     memset(head, 0xff, sizeof(head));
     memset(vis, 0x00, sizeof(vis));
     tot = lacnt = 1;
}
void addedge(int from, int to, int cost) {
     eg[tot] = edge(to, cost, head[from]);
     head[from] = tot++;
}
void dfs(int v, int height) {
```

```
vis[v] = true;
     id[v] = lacnt;
     st.arr[lacnt] = height;
     la[lacnt++] = v;
     for(int i = head[v]; i != -1; i = eg[i].next) {
          if(!vis[eg[i].to]) {
                dis[eg[i].to] = dis[v] + eg[i].cost;
                dfs(eg[i].to, height + 1);
                st.arr[lacnt] = height;
                la[lacnt++] = v;
          }
     }
}
int lca(int u, int v) {
     int I = min(id[u], id[v]), r = max(id[u], id[v]);
     return la[st.query(l, r)];
}
                                                 SCC
namespace SCC {
     //id 1 to n
     const int VN = 10005, EN = 100005;
     struct edge {
          int to, next;
          edge() {}
          edge(int _to, int _next) : to(_to), next(_next) {}
     } se[EN], re[EN];
     int shead[VN], rhead[VN], vs[VN], cmp[VN], vidx, stot, rtot, n;
     bool vis[VN];
     void init(int _n) {
          n = _n;
          stot = rtot = 0;
          memset(shead, 0xff, sizeof(shead));
          memset(rhead, 0xff, sizeof(rhead));
          vidx = 0;
     }
     void addedge(int from, int to) {
          se[stot] = edge(to, shead[from]);
          shead[from] = stot++;
```

```
re[rtot] = edge(from, rhead[to]);
           rhead[to] = rtot++;
     }
     void dfs(int v) {
           vis[v] = true;
           for(int i = shead[v]; i != -1; i = se[i].next) {
                 if(!vis[se[i].to]) {
                      dfs(se[i].to);
                }
           }
           vs[vidx++] = v;
     }
     void rdfs(int v, int k) {
           vis[v] = true;
           cmp[v] = k;
           for(int i = rhead[v]; i != -1; i = re[i].next) {
                 if(!vis[re[i].to]) {
                      rdfs(re[i].to, k);
                }
           }
     }
     int scc() {
           memset(vis, 0, sizeof(vis));
           for(int i = 1; i <= n; ++i) {
                 if(!vis[i]) dfs(i);
           }
           memset(vis, 0, sizeof(vis));
           int k = 0;
           for(int i = vidx - 1; i >= 0; --i) {
                 if(!vis[vs[i]]) rdfs(vs[i], k++);
           }
           return k;
     }
}
using int64 = long long;
```

## Dijkstra

```
struct edge {
     int to, cost, next;
```

```
edge() {}
     edge(int _to, int _cost, int _next) : to(_to), cost(_cost), next(_next) {}
} e[12500];
int tot;
int head[2505];
void init_graph() {
     tot = 0;
     memset(head, -1, sizeof(head));
}
void addedge(int from, int to, int cost) {
     e[tot] = edge(to, cost, head[from]);
     head[from] = tot++;
}
int64 dis[2505];
bool vis[2505];
int64 dijkstra(int s, int t) {
     using PLI = pair<int64, int>;
     memset(dis, 0x3f, sizeof(dis));
     memset(vis, 0x00, sizeof(vis));
     priority_queue<PLI, vector<PLI>, greater<PLI>> pq;
     pq.push(PLI(0, s));
     dis[s] = 0;
     while(!pq.empty()) {
          PLI now = pq.top();
          pq.pop();
          if(vis[now.second]) continue;
          vis[now.second] = true;
          for(int i = head[now.second]; i != -1; i = e[i].next) {
               if(!vis[e[i].to] \&\& e[i].cost + now.first < dis[e[i].to]) {
                     dis[e[i].to] = e[i].cost + now.first;
                     pq.push(PLI(dis[e[i].to], e[i].to));
               }
          }
     }
     return dis[t];
}
```

```
namespace SPFA {
     const int N = 100010, M = 600010, INF = 0x3f3f3f3f;
     struct edge {
          int to, next, cost;
          edge() {}
          edge(int _to, int _next, int _cost) : to(_to), next(_next), cost(_cost) {}
     int head[N], dis[N], cnt[N], tot, incnt[N];
     void init() {
          memset(head, -1, sizeof(head));
          tot = 0;
     }
     void addedge(int from, int to, int cost) {
          eg[tot] = edge(to, head[from], cost);
          head[from] = tot++;
     }
     bool spfa(int s, int n) {
          fill(cnt, cnt + n + 1, 0);
          fill(dis, dis + n + 1, INF);
          fill(incnt, incnt + n + 1, 0);
          queue<int> q;
          q.push(s);
          dis[s] = 0; cnt[s] = 1; incnt[s] = 1;
          while(!q.empty()) {
               int now = q.front();
               q.pop();
               if(incnt[now] == 1) {
                     for(int i = head[now]; i != -1; i = eg[i].next) {
                          edge\& e = eg[i];
                          if(dis[e.to] > dis[now] + e.cost) {
                                dis[e.to] = dis[now] + e.cost;
                               if(++cnt[e.to] > n) return false;
                               q.push(e.to);
                               ++incnt[e.to];
                          }
                     }
               --incnt[now];
          }
          return true;
     }
```

#### Dinic

```
namespace Dinic {
     const int V = 1000010, E = 8000010, INF = 1e9;
     int vcnt;
     struct edge {
          int to, next, cap, flow;
          edge() {}
          edge(int _to, int _next, int _cap) : to(_to), next(_next), cap(_cap), flow(0) {}
     } eg[E];
     int head[V], cur[V], dis[V], que[V], qf, qe, ecnt, s, t;
     bool vis[V];
     void init(int _vcnt) {
          vcnt = _vcnt;
          memset(head, 0xff, sizeof(head[0]) * (vcnt + 1));
          ecnt = 0;
     }
     void addedge(int from, int to, int cap) {
          eg[ecnt] = edge(to, head[from], cap);
          head[from] = ecnt++;
          eg[ecnt] = edge(from, head[to], 0);
          head[to] = ecnt++;
     }
     bool bfs() {
          memset(vis, 0, sizeof(vis[0]) * (vcnt + 1));
          qf = 0; qe = 0;
          que[qe++] = s;
          dis[s] = 0; vis[s] = true;
          while(qf < qe) {
               int x = que[qf++];
               for(int i = head[x]; i != -1; i = eg[i].next) {
                     const edge& e = eg[i];
                     if(!vis[e.to] && e.cap > e.flow) {
                          vis[e.to] = true;
                          dis[e.to] = dis[x] + 1;
                          que[qe++] = e.to;
                          if(e.to == t) return true;
                    }
```

```
}
           }
           return false;
     }
     int dfs(int x, int a) {
           if(x == t | | a == 0) return a;
           int flow = 0, f;
           for(int& i = cur[x]; i != -1; i = eg[i].next) {
                edge& e = eg[i];
                if(dis[x] + 1 == dis[e.to] && (f = dfs(e.to, min(e.cap - e.flow, a)))) {
                      e.flow += f;
                      eg[i ^ 1].flow -= f;
                      flow += f;
                      a -= f;
                      if(!a) break;
                }
           }
           return flow;
     }
     int solve(int _s, int _t) {
           s = _s; t = _t;
           int flow = 0;
           while(bfs()) {
                memcpy(cur, head, sizeof(cur[0]) * (vcnt + 1));
                flow += dfs(s, INF);
           }
           return flow;
     }
}
```

## Treap

```
template<typename T, class _Comp = less<T>>
struct Treap {
    const static int NODECNT = _;
    struct Node {
        int ch[2], p, sz;
        T v;
        void make(int _I, int _r, int _p, const T& _v) {
            ch[0] = _I; ch[1] = _r; p = _p; v = _v; sz = 1;
        }
}
```

```
} node[NODECNT];
int m_rt, mp[NODECNT], mp_idx, node_idx;
void maintain(int x) {
     node[x].sz = 1;
     node[x].sz += node[x].ch[0] == -1 ? 0 : node[node[x].ch[0]].sz;
     node[x].sz += node[x].ch[1] == -1 ? 0 : node[node[x].ch[1]].sz;
}
Comp cmp;
explicit Treap(const _Comp& c): cmp(c) { unsigned seed = 19971023; srand(seed); clear(); }
Treap() : cmp(_Comp()) { unsigned seed = 19971023; srand(seed); clear(); }
void clear() { m_rt = -1; mp_idx = -1; node_idx = 0; }
void ins(const T& val) { _ins(m_rt, val); }
void _ins(int& rt, const T& val) {
     if(rt == -1) {
          if(mp_idx == -1) { node[rt = node_idx++].make(-1, -1, rand(), val); }
          else { node[rt = mp[mp idx--]].make(-1, -1, rand(), val); }
     } else {
          int type = cmp(node[rt].v, val);
          _ins(node[rt].ch[type], val);
          maintain(rt);
          if(node[rt].p < node[node[rt].ch[type]].p) rotate(rt, type);</pre>
     }
}
void del(const T& val) { _del(m_rt, val); }
void _del(int& rt, const T& val) {
     assert(rt != -1);
     if(node[rt].v == val) {
          if(node[rt].ch[0] == -1) {
               mp[++mp_idx] = rt;
               rt = node[rt].ch[1];
          } else if(node[rt].ch[1] == -1) {
               mp[++mp_idx] = rt;
               rt = node[rt].ch[0];
          } else {
               int next = node[node[rt].ch[0]].p < node[node[rt].ch[1]].p;</pre>
               rotate(rt, next);
               _del(node[rt].ch[next ^ 1], val);
               maintain(rt);
```

```
}
     } else {
           _del(node[rt].ch[cmp(node[rt].v, val)], val);
           maintain(rt);
     }
}
int find(const T& val) {
     int rt = m_rt;
     while(rt != -1) {
          if(node[rt].v == val) return rt;
           rt = node[rt].ch[cmp(node[rt].v, val)];
     }
     return -1;
}
void rotate(int& rt, int type) {
     int tmp = node[rt].ch[type];
     node[rt].ch[type] = node[tmp].ch[type ^ 1];
     node[tmp].ch[type ^ 1] = rt;
     maintain(rt); maintain(tmp);
     rt = tmp;
}
int kth(int k) {
     assert(k >= 1 && k <= size());
     int rt = m_rt, res = -1;
     while(rt != -1) {
          int le = node[rt].ch[0] == -1 ? 0 : node[node[rt].ch[0]].sz;
           if(le == k - 1) {
               res = node[rt].v;
                break;
          } else if(le > k - 1) {
                rt = node[rt].ch[0];
          } else {
                k = le + 1;
                rt = node[rt].ch[1];
          }
     }
     return res;
}
int rank(const T& val) {
     int rt = m_rt, cnt = 0;
```

```
while(rt != -1) {
     int le = node[rt].ch[0] == -1 ? 0 : node[node[rt].ch[0]].sz;
     if(cmp(node[rt].v, val)) {
         cnt += le + 1;
         rt = node[rt].ch[1];
     } else {
         rt = node[rt].ch[0];
     }
}
return cnt + 1;
}
int size() { return node[m_rt].sz; }
};
```

## 线段树

```
using II = long long;
struct seg_tree {
     static const int MAXN = 100005;
     struct Node {
          Il sum, tag;
     } node[MAXN << 2];
     Il arr[MAXN];
     int lson(int x) { return x << 1; }
     int rson(int x) { return (x << 1) + 1; }
     void make(int x, int xl, int xr) {
          if(xl == xr) {
               node[x].sum = arr[xl];
               node[x].tag = 0;
               return;
          }
          int mid = (xl + xr) >> 1;
          make(lson(x), xl, mid);
          make(rson(x), mid + 1, xr);
          node[x].sum = node[lson(x)].sum + node[rson(x)].sum;
          node[x].tag = 0;
     }
     void pushdown(int x, int xl, int xr) {
          node[x].sum += (xr - xl + 1) * node[x].tag;
```

```
if(xl < xr) {
                node[lson(x)].tag += node[x].tag;
                node[rson(x)].tag += node[x].tag;
          }
           node[x].tag = 0;
     }
     void pushup(int x, int xl, int xr) {
           int mid = (xl + xr) >> 1;
           int lcnt = mid - xl + 1, rcnt = xr - mid;
           node[x].sum = node[lson(x)].sum + lcnt * node[lson(x)].tag + node[rson(x)].sum + rcnt *
node[rson(x)].tag;
     }
     Il query(int x, int xl, int xr, int ql, int qr) {
           if(xl > qr | | xr < ql) return 0;
           if(xl == ql \&\& xr == qr) {
                return node[x].sum + (xr - xl + 1) * node[x].tag;
          }
           II ans = 0;
           int mid = (xl + xr) >> 1;
           pushdown(x, xl, xr);
           ans += query(lson(x), xl, mid, ql, min(mid, qr));
           ans += query(rson(x), mid + 1, xr, max(ql, mid + 1), qr);
           return ans;
     }
     void update(int x, int xl, int xr, int cl, int cr, ll dt) {
           if(xr < cl \mid \mid xl > cr) return;
           if(cl == xl \&\& cr == xr) {
                node[x].tag += dt;
                return;
           }
           pushdown(x, xl, xr);
           int mid = (xl + xr) >> 1;
           update(lson(x), xl, mid, cl, min(mid, cr), dt);
           update(rson(x), mid + 1, xr, max(cl, mid + 1), cr, dt);
           pushup(x, xl, xr);
     }
} st;
```

## KM 字符串匹配

```
typedef long long II;
typedef unsigned long long ull;
int km_match(char* pattern, char* str) {
     int plen = strlen(pattern);
     int slen = strlen(str);
     int dt = max(((plen - 1) >> 1), 1);
     int cnt = 0;
     ull phash = 0, shash = 0;
     ull con = 1;
     for(int i = 0; i < plen; ++i) {
           phash = ((phash << 7) + pattern[i]);</pre>
           shash = ((shash << 7) + str[i]);
           con <<= 7;
     }
     con >>= 7;
     for(int i = 0; i < slen - plen + 1; ++i) {
           if(phash == shash) {
                bool flag = true;
                for(int j = 0; j < plen; <math>j += dt) {
                      if(pattern[j] != str[i + j]) {
                           flag = false;
                           break;
                      }
                }
                if(flag) ++cnt;
           }
           shash = (((shash - str[i] * con) << 7) + str[i + plen]);
     }
     return cnt;
}
                                                    LIS
struct LIS {
     // O(nlgn), strictly increase monotonically
     const static int N = 100005;
     int a[N], b[N];
     void input(int n) {
           for(int i = 1; i \le n; ++i) {
                scanf("%d", a + i);
           }
```

```
int solve(int n) {
    int len = 0;
    for(int i = 1; i <= n; ++i) {
        int* p = lower_bound(b + 1, b + len + 1, a[i]);
        *p = a[i];
        len = max(len, a[i] = p - b);
    }
    return len;
}
lis;</pre>
```

## 数值积分

```
namespace Int {
     const double eps = 1e-6;
     template<class _Callable>
     double Simpson(double lb, double ub, const _Callable& f) {
          double mid = (lb + ub) * .5;
          return (ub - lb) * (f(lb) + 4 * f(mid) + f(ub)) / 6.;
     }
     template<class _Callable>
     double _asr(double lb, double ub, double pre, double eps, const _Callable& f) {
          double mid = (lb + ub) * .5;
          double L = Simpson(lb, mid, f), R = Simpson(mid, ub, f);
          if(fabs(L + R - pre) < 15 * eps) return (L + R) + (L + R - pre) / 15.;
          return _asr(lb, mid, L, eps / 2, f) + _asr(mid, ub, R, eps / 2, f);
     }
     template<class _Callable>
     double asr(double lb, double ub, const _Callable& f) {
          return _asr(lb, ub, Simpson(lb, ub, f), eps, f);
     }
}
```

#### **FWT**

```
void FWT(int* a, int n) {
    for(int d = 1; d < n; d <<= 1) {
        for(int m = d << 1, i = 0; i < n; i += m) {</pre>
```

```
for(int j = 0; j < d; ++j) {
                     int x = a[i + j], y = a[i + j + d];
                     a[i + j] = (x + y) \% MOD;
                     a[i + j + d] = (x - y + MOD) \% MOD;
                     //xor:a[i+j]=x+y,a[i+j+d]=(x-y+MOD)%MOD;
                     //and:a[i+j]=x+y;
                     //or:a[i+j+d]=x+y;
                }
          }
     }
}
void UFWT(int* a,int n) {
     for(int d = 1; d < n; d <<= 1) {
          for(int m = d \ll 1, i=0; i < n; i += m){
                for(int j = 0; j < d; ++j) {
                     int x = a[i + j], y = a[i + j + d];
                     a[i + j] = 1LL * (x + y) * rev % MOD;
                     a[i + j + d] = (1LL * (x - y) * rev % MOD + MOD) % MOD;
                     //xor:a[i+j]=(x+y)/2,a[i+j+d]=(x-y)/2;
                     //and:a[i+j]=x-y;
                     //or:a[i+j+d]=y-x;
                }
          }
     }
}
```

## 任意模数 FFT

```
typedef long long LL;
const long double PI = acos(-1);
const int MOD =1000000007;
const int maxn=140100;
struct Complex {
    long double r,i;
    Complex(long double _r = 0.0,long double _i = 0.0) {
        r = _r;
        i = _i;
    }
    Complex operator +(const Complex &b) {
        return Complex(r+b.r,i+b.i);
    }
    Complex operator -(const Complex &b) {
```

```
return Complex(r-b.r,i-b.i);
     }
     Complex operator *(const Complex &b) {
          return Complex(r*b.r-i*b.i,r*b.i+i*b.r);
     }
};
Complex conj(Complex a)
     return Complex(a.r,-a.i);
}
void change(Complex y[],int len)
{
     int i,j,k;
     for(i = 1, j = len/2; i < len-1; i++) {
          if(i < j)swap(y[i],y[j]);
          k = len/2;
          while(j \ge k) {
               j -= k;
               k /= 2;
          if(j < k) j += k;
     }
}
void FFT(Complex y[],int len,int on) //len=2^k
{
     change(y,len);
     for(int h = 2; h <= len; h <<= 1) {
          Complex wn(cos(-on*2*PI/h),sin(-on*2*PI/h));
          for(int j = 0; j < len; j+=h) {
               Complex w(1,0);
               for(int k = j; k < j+h/2; k++) {
                     Complex u = y[k];
                    Complex t = w*y[k+h/2];
                    y[k] = u+t;
                    y[k+h/2] = u-t;
                    w = w*wn;
               }
          }
     }
     if(on == -1)
          for(int i = 0; i < len; i++)
               y[i].r /= len;
int callen(int len1,int len2)
```

```
{
     int len=1;
     while(len < (len1<<1) | | len < (len2<<1))len<<=1;
     return len;
}
LL fftans[maxn];
Complex A[maxn],B[maxn],dft[4][maxn],dt[4];
int td[4];
void fft(LL* y1,int len1,LL* y2,int len2,LL mod)
{
     int len=callen(len1,len2);
     for(int x=0; x<len1; x++)A[x]=Complex(y1[x]&32767,y1[x]>>15);
     for(int x=len1; x<len; x++)A[x]=Complex(0,0);
     for(int x=0; x<len2; x++)B[x]=Complex(y2[x]&32767,y2[x]>>15);
     for(int x=len2; x<len; x++)B[x]=Complex(0,0);
     FFT(A,len,1);
     FFT(B,len,1);
     int j;
     for(int x=0; x<len; x++) {
          j=(len-x)&(len-1);
          dt[0]=(A[x]+conj(A[j]))*Complex(0.5,0);
          dt[1]=(A[x]-conj(A[j]))*Complex(0,-0.5);
          dt[2]=(B[x]+conj(B[j]))*Complex(0.5,0);
          dt[3]=(B[x]-conj(B[j]))*Complex(0,-0.5);
          dft[0][j]=dt[0]*dt[2];
          dft[1][j]=dt[0]*dt[3];
          dft[2][j]=dt[1]*dt[2];
          dft[3][j]=dt[1]*dt[3];
     }
     for(int x=0; x<len; x++) {
          A[x]=dft[0][x]+dft[1][x]*Complex(0,1);
          B[x]=dft[2][x]+dft[3][x]*Complex(0,1);
     }
     FFT(A,len,1);
     FFT(B,len,1);
     for(int x=0; x<len; x++) {
          td[0]=(LL)(A[x].r/len+0.5)%mod;
          td[1]=(LL)(A[x].i/len+0.5)%mod;
          td[2]=(LL)(B[x].r/len+0.5)%mod;
          td[3]=(LL)(B[x].i/len+0.5)%mod;
          fftans[x]=(td[0]+((LL)(td[1]+td[2])<<15)+((LL)td[3]<<30))%mod;
     }
}
LL a[maxn],b[maxn];
```

#### **SAIS**

```
template<size_t size>
struct SuffixArray {
     bool type[size<<1];
     int bucket[size],bucket1[size];
     int sa[size],rk[size],ht[size];
     inline bool isLMS(const int i,const bool *type) { return i>0&&type[i]&&!type[i-1];}
     template<class T>
     inline void inducedSort(T s,int *sa,const int len,const int cm,const int sz,bool *type,int
*bucket,int *cntbuf,int *p) {
          memset(bucket,0,sizeof(int) * cm);
          memset(sa,-1,sizeof(int) * len);
          for (int i=0;i<len;i++) bucket[s[i]]++;
          cntbuf[0]=bucket[0];
          for (int i=1;i<cm;i++) cntbuf[i]=cntbuf[i-1]+bucket[i];</pre>
          for (int i=sz-1;i>=0;i--) sa[--cntbuf[s[p[i]]]]=p[i];
          for (int i=1;i<cm;i++) cntbuf[i]=cntbuf[i-1]+bucket[i-1];</pre>
          for (int i=0;i<len;i++)
                if (sa[i]>0&&!type[sa[i]-1]) sa[cntbuf[s[sa[i]-1]]++]=sa[i]-1;
          cntbuf[0]=bucket[0];
          for (int i=1;i<cm;i++) cntbuf[i]=cntbuf[i-1]+bucket[i];</pre>
          for (int i=len-1;i>=0;i--)
               if (sa[i]>0&&type[sa[i]-1]) sa[--cntbuf[s[sa[i]-1]]]=sa[i]-1;
     }
     template<class T>
     inline void sais(T s,int *sa,int len,bool *type,int *bucket,int *bucket1,int cm) {
          int i,j,sz=0,cnt=0,p=-1,x,*cntbuf=bucket+cm;
          type[len-1]=1;
          for (i=len-2;i>=0;i--) type[i]=s[i]< s[i+1] | |(s[i]==s[i+1] & type[i+1]);
          for (i=1;i<len;i++)
                if (type[i]&&!type[i-1]) bucket1[sz++]=i;
          inducedSort(s,sa,len,cm,sz,type,bucket,cntbuf,bucket1);
          for (i=sz=0;i<len;i++)
                if (isLMS(sa[i],type)) sa[sz++]=sa[i];
          for (i=sz;i<len;i++) sa[i]=-1;
          for (i=0;i<sz;i++) {
               x=sa[i];
               for (j=0;j<len;j++) {
                     if (p==-1||s[x+j] !=s[p+j]||type[x+j] !=type[p+j]) {
                          cnt++;p=x;break;
```

```
} else {
                          if (j>0&&(isLMS(x+j,type)||isLMS(p+j,type))) break;
                     }
               }
               x=(^x\&1?x>>1:x-1>>1),sa[sz+x]=cnt-1;
          }
          for (i=j=len-1;i>=sz;i--)
               if (sa[i]>=0) sa[j--]=sa[i];
          int *s1=sa+len-sz,*bucket2=bucket1+sz;
          if (cnt<sz) {
               sais(s1,sa,sz,type+len,bucket,bucket1+sz,cnt);
          } else {
               for (i=0;i<sz;i++) sa[s1[i]]=i;
          }
          for (i=0;i<sz;i++) bucket2[i]=bucket1[sa[i]];</pre>
          inducedSort(s,sa,len,cm,sz,type,bucket,cntbuf,bucket2);
     }
     template<class T>
     inline void getHeight(T s,int n) {
          for (int i=1;i<=n;i++) rk[sa[i]]=i;
          int j=0,k=0;
          for (int i=0;i<n;ht[rk[i++]]=k)
               for (k?k--:0,j=sa[rk[i]-1];s[i+k]==s[j+k];k++);
     }
     template<class T>
     inline void init(T s,const int len,const int cm) {
          sais(s,sa,len,type,bucket,bucket1,cm);
          for (int i=1;i<len;i++) rk[sa[i]]=i;
          getHeight(s,len);
     }
};
char s[MAXN];//0base
SuffixArray<MAXN> sf;
sf.init(s,strlen(s)+1,256);
```

## Digit count

```
II ct(int k, II n) {
    II res = 0 , x;
    if (k == 0 && n == 0) res = 1;
    for (II i = 1;x = n / i;i *= 10) {
        II high = x / 10;
```

```
if (k == 0) {
      if (high) high--;
      else {
          res++;
          break;
      }
    }
    res += high * i;
    int cur = x % 10;
    if (cur > k) res += i;
      else if (cur == k) res += n - x * i + 1;
    }
    return res;
}
```