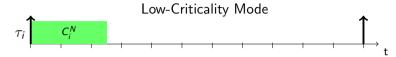
Probabilistic Real-Time Scheduling and its Possible Link to Mixed-Criticality Systems

Georg von der Brüggen¹, Sergey Bozhko², Mario Günzel¹, Kuan-Hsun Chen³, <u>Jian-Jia Chen¹</u>, and Björn B. Brandenburg²

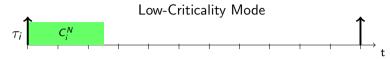
¹TU Dortmund, Germany
²Max Planck Institute for Software Systems, Germany
³University of Twente, The Netherlands

05 December 2022



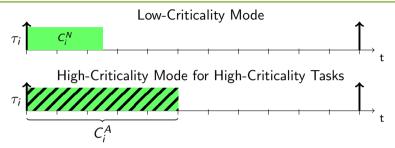


- $D_i = T_i$ $\tau_i = (C_i^N, T_i)$



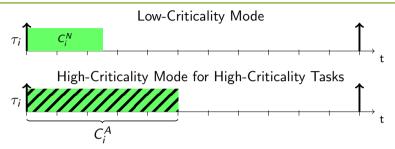
System-wide switch to high-criticality mode

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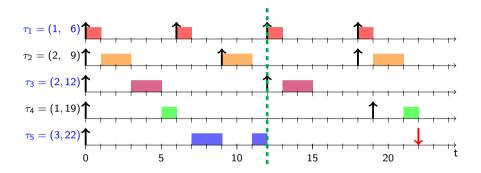
System-wide switch to high-criticality mode

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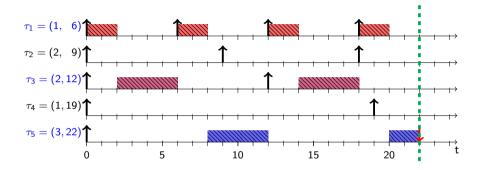
- System-wide switch to high-criticality mode
- Low-criticality tasks: No guarantees, best effort
- $D_i = T_i$
- $\tau_i = (C_i^N, T_i), C_i^A = 2 \cdot C_i^N$

Worst-Case Response-Time Analysis



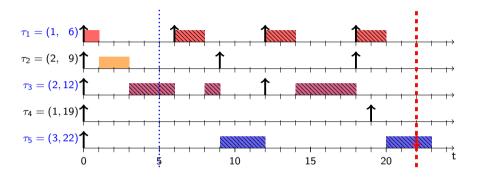
Low-criticality mode

Worst-Case Response-Time Analysis



- Low-criticality mode
- Migh-criticality mode

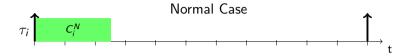
Worst-Case Response-Time Analysis



- Low-criticality mode
- Migh-criticality mode
- Mode switch (usually the bottleneck)

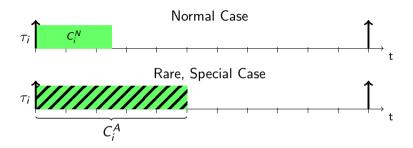


Uncertain Execution Behaviour in Probabilistic View



- $D_i = T_i$ $\tau_i = (C_i^N, T_i)$

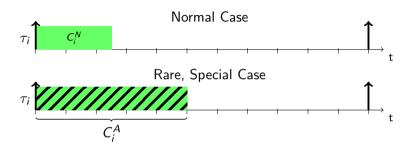
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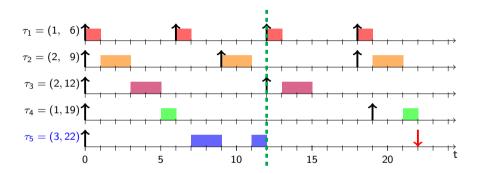
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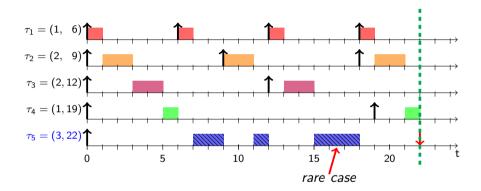
Uncertain Execution Behaviour in Probabilistic View



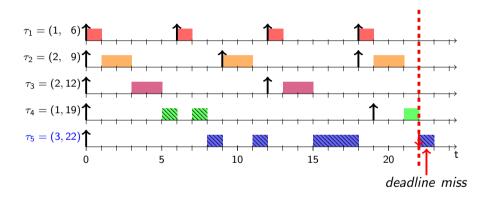
- $D_i = T_i$
- $\tau_i = (C_i^N, T_i), C_i^A = 2 \cdot C_i^N$
- $\mathbb{P}(C_i^A) + \mathbb{P}(C_i^N) = 1$
- $\mathbb{P}(C_i^A) \ll \mathbb{P}(C_i^N)$



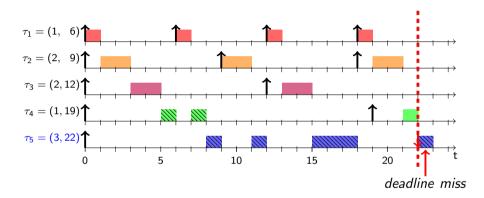
• Do all tasks meet their deadline under all circumstances?



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- Do all tasks meet their deadline under all circumstances?
- What is the probability that a job misses its deadline?

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- That only a subset of tasks exhibits abnormal behaviour seems natural

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- That only a subset of tasks exhibits abnormal behaviour seems natural
- ⇒ Frequent system-wide mode switches which may be both costly and unnecessary

Idea: Mode switch based on deadline miss probability

Soft and Firm Real-Time Systems

Important problem in industry (Akesson et al., RTSS 2020)

- 62%: system includes soft or firm real-time components
- 45%: the most critical function can miss some deadlines
- Only 15%: deadlines can never be missed

B. Akesson, M. Nasri, G. Nelissen, S. Altmeyer, and R. I. Davis

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The probability that deadlines are missed must be quantified

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Quantifying Deadline Misses

Deadline Miss Rate: Percentage of deadline misses (in the long run)

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Worst-Case Deadline Failure Probability: Maximum probability of any job to be the first to miss its deadline

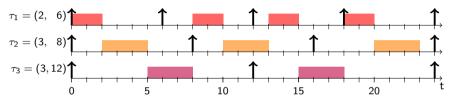
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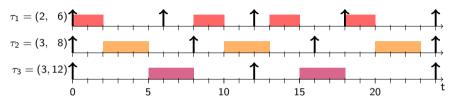
- Mean time to failure due to a deadline miss
- Bounds the deadline-miss rate (no backlog)

Complexity Issues of the Naive Solution



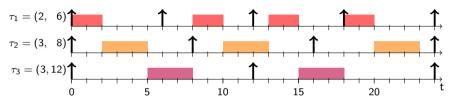
Consider all jobs in the hyperperiod individually

Complexity Issues of the Naive Solution



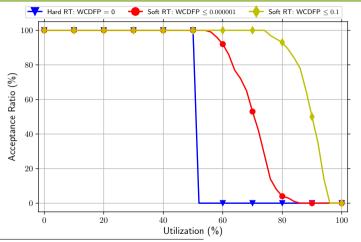
- Consider all jobs in the hyperperiod individually
- For each job, calculate the probability to miss its deadline

Complexity Issues of the Naive Solution



- Consider all jobs in the hyperperiod individually
- For each job, calculate the probability to miss its deadline
- ⇒ Computational complexity is too high to be feasible in practice

How much can we gain?



Setting for rare mode: $P_i(A) = 0.01$ $C_i^A = 2 \cdot C_i^N$

G. v. d. Brüggen, N. Piatkowski, K.-H. Chen, J.-J. Chen, K. Morik, and B. Brandenburg "Efficiently Approximating the Worst-Case Deadline Failure Probability under EDF", RTSS 2021

1 Which scenarios must be considered?

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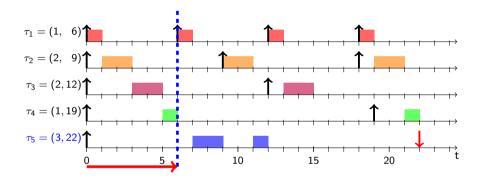
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- Observe the Miss Probability for a job efficiently?

- Which scenarios must be considered?
 - depends on inter-arrival constraints
 - depends on scheduling policy
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 - reduce number of scenarios without under-approximation
 - reduce number of scenarios without being too pessimistic
- 2 How to calculate the miss probability for a job efficiently?
 - determine probability for too much workload in an interval

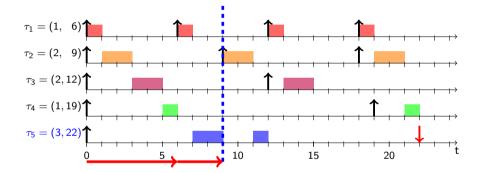
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- 2 How to calculate the miss probability for a job efficiently?
 - determine probability for too much workload in an interval
- 3 How can dependencies be handled?

State of the Art - Calculation

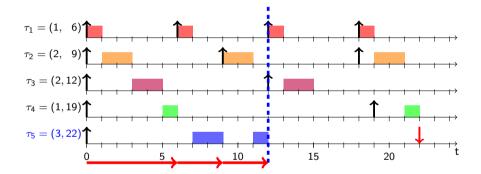
Job-based approaches



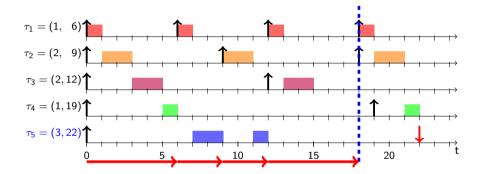


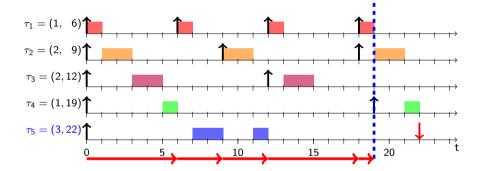




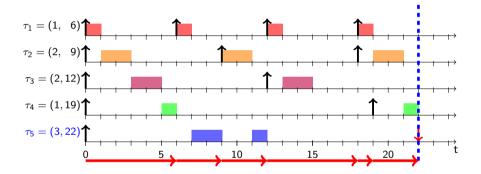










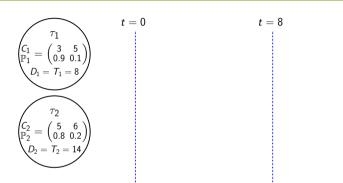




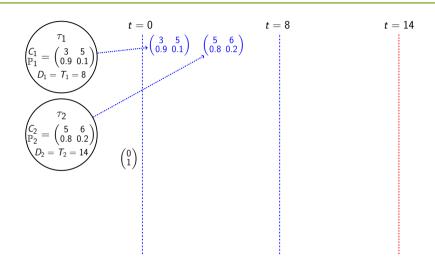
$$egin{aligned} \mathcal{C}_1 &= \begin{pmatrix} 3 & 5 \ 0.9 & 0.1 \end{pmatrix} \; \otimes \; \begin{pmatrix} 5 & 6 \ 0.8 & 0.2 \end{pmatrix} = egin{aligned} \mathcal{C}_2 \ \mathbb{P}_2 \end{aligned} \ egin{aligned} egin{aligned} egin{aligned} egin{aligned} egin{aligned} egin{aligned} egin{aligned} egin{aligned} \mathcal{C}_2 \ 0.8 & 0.2 \end{pmatrix} = egin{aligned} \mathcal{C}_2 \ \mathbb{P}_2 \end{aligned} \end{aligned}$$

$$\begin{array}{c}
\tau_1 \\
C_1 = \begin{pmatrix} 3 & 5 \\
0.9 & 0.1 \end{pmatrix} \\
D_1 = T_1 = 8
\end{array}$$

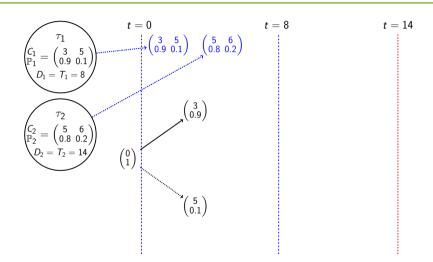
$$\begin{array}{c}
\tau_2 \\
C_2 = \begin{pmatrix} 5 & 6 \\
0.8 & 0.2 \end{pmatrix} \\
D_2 = T_2 = 14
\end{array}$$



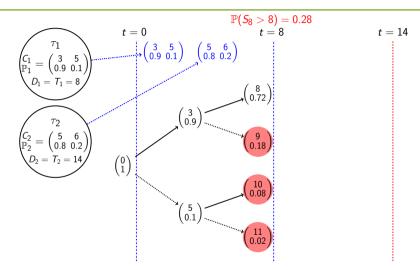
t = 14



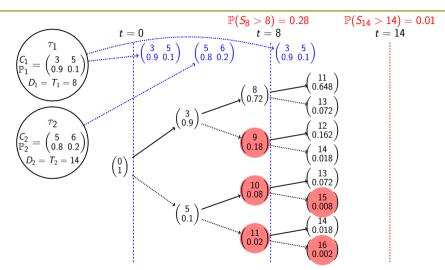




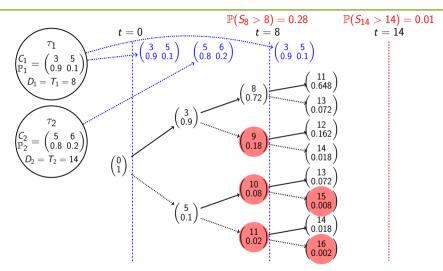




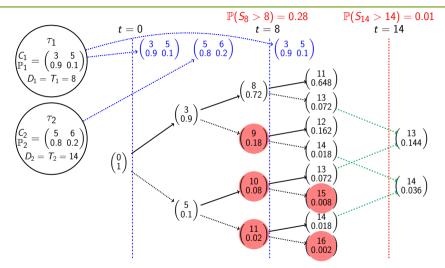








Exponential in the number of jobs



Exponential in the number of jobs

State of the Art - Calculation

- Job-based + theoretically exact
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 - Re-sampling (Maxim and Cucu-Grosjean, RTSS 13)
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$$\begin{pmatrix} 7 \\ 0.84 \end{pmatrix} \qquad \begin{pmatrix} 8 \\ 0.15 \end{pmatrix} \qquad \begin{pmatrix} 9 \\ 0.012 \end{pmatrix} \qquad \begin{pmatrix} 10 \\ 4.9 \cdot 10^{-04} \end{pmatrix} \qquad \begin{pmatrix} 11 \\ 1.3 \cdot 10^{-05} \end{pmatrix} \qquad \begin{pmatrix} 12 \\ 1.9 \cdot 10^{-07} \end{pmatrix} \qquad \begin{pmatrix} 13 \\ 1.6 \cdot 10^{-09} \end{pmatrix} \qquad \begin{pmatrix} 14 \\ 6.1 \cdot 10^{-12} \end{pmatrix}$$

Total C _i	7	8	9	10	11	12	13	14
Probability	0.84	0.15	0.012	$4.9 \cdot 10^{-04}$	$1.3 \cdot 10^{-05}$	$1.9 \cdot 10^{-07}$	$1.6 \cdot 10^{-09}$	$6.1 \cdot 10^{-12}$
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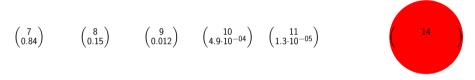
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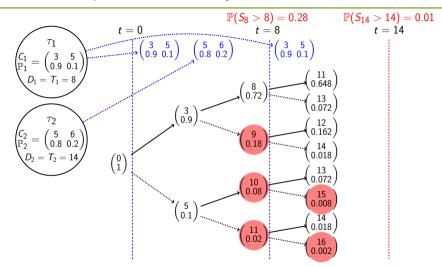
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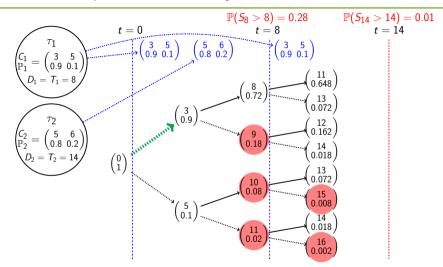
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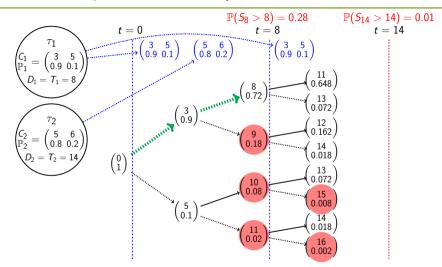




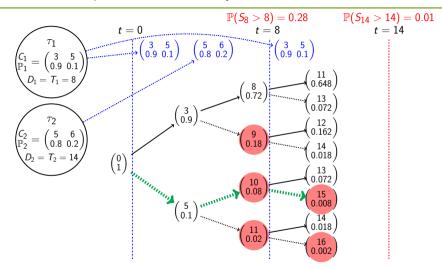




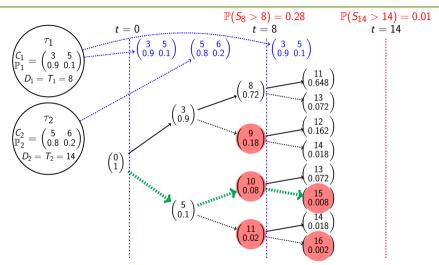












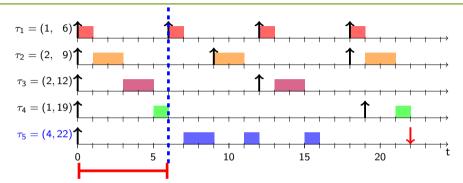
Count: #samples and #misses \Rightarrow Bernoulli trial, bounded error

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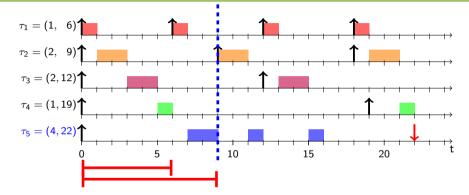
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- Interval-based

Interval-Based Approaches

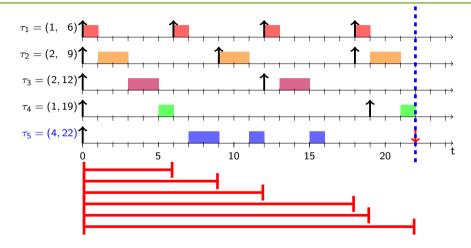




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- Interval-based + scalable iid assumption unknown loss
 - Task-level convolution (von der Brüggen et al., ECRTS 18)
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• Worst-Case Deadline Failure Probability

Deadline Miss Rate

- Worst-Case Deadline Failure Probability
 - FP: Related to critical instant (Chen et al., RTSS 22)
- Deadline Miss Rate

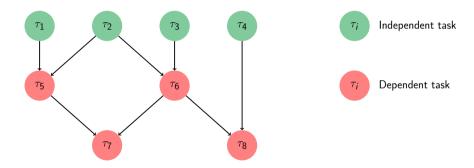
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 - FP: Related to critical instant (Chen et al., RTSS 22)
 - EDF: Align all deadlines (von der Brüggen et al., RTSS 21)
- Deadline Miss Rate

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- Worst-Case Deadline Failure Probability
 - FP: Related to critical instant (Chen et al., RTSS 22)
 - EDF: Align all deadlines (von der Brüggen et al., RTSS 21)
- Deadline Miss Rate
 - FP: —
 - EDF: —

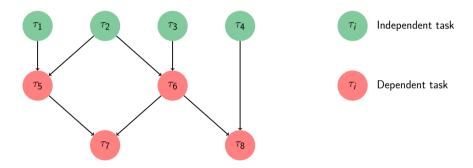
State of the Art - Dependencies

• Either iid (i.e., no dependencies) or acyclic, triggered mode dependencies



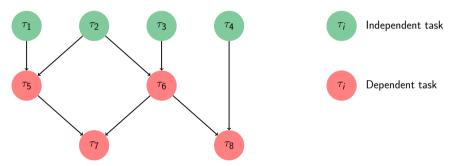
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State of the Art - Dependencies

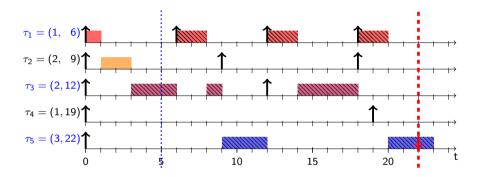
- Either iid (i.e., no dependencies) or acyclic, triggered mode dependencies
- Bounded length of triggered interval
- Over-approximation using task-level convolution



Conclusion - State of the Art for Probabilistic Scheduling

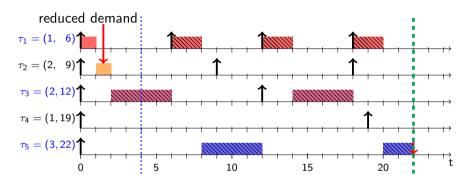
- Scenarios
 - WCDFP scenario or over-approximation known
 - DMR scenarios unknown
 - Scenarios when backlog is considered unknown
- Calculation methods with different precision/runtime tradeoffs
- Dependencies increase the complexity
 - Only limited scenarios examined
 - Many calculation methods require independent probabilities

Link - Mode Switch Probability



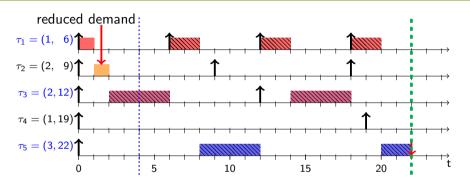
• Mode switch: bottleneck due pre-mode-change low-criticality interference

Link - Mode Switch Probability

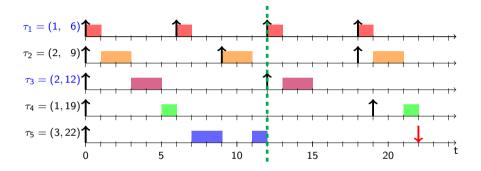


- Mode switch: bottleneck due pre-mode-change low-criticality interference
- Low-criticality resource demand and mode switch often not happen simultaneously

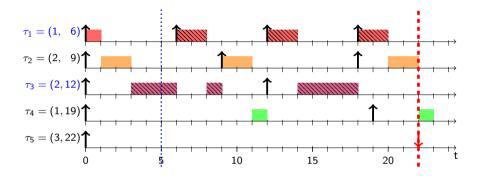
Link - Mode Switch Probability



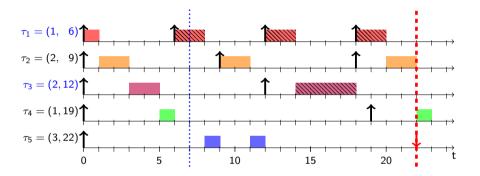
- Mode switch: bottleneck due pre-mode-change low-criticality interference
- Low-criticality resource demand and mode switch often not happen simultaneously
- ⇒ Exploit that probability of simultaneous occurrence is low during analysis



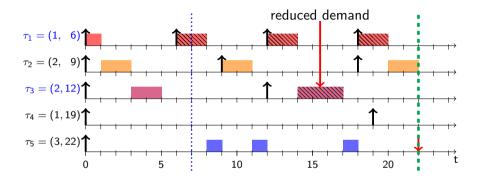
- Idea: Sample multiple schedules (e.g., probabilistic time of the mode switch)
- Determine miss probability for τ_5 : Count # samples and # misses



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- Consider probabilistic mode switch and probabilistic execution time

Conclusion

- Start discussion which links are potentially interesting
- Three main research questions in probabilistic scheduling
 - Scenario to consider: In many cases unknown
 - Calculation methods: Different precision/runtime tradeoffs
 - Dependent probabilities: Not many solutions due to complexity issues
- Additional possible links between probabilistic scheduling and mixed-criticality
 - Analysing mode switch probability
 - Probabilistic guarantees for low-criticality tasks
 - Interpret high- and low-criticality parameters (different levels of assurance) as different levels of confidence in correspondence to mode probabilities
- Additional challenges
 - Detecting a budged overrun vs. refuting an execution time distribution
 - Complex interplay of execution time dependencies in mixed-criticality systems



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Thank You!

