

Contents

1	Examples	1
1.1	Prerequisites	1
2	Straight channel with slope and bottom friction	2
2.1	Generation of the mesh	2
2.2	Initial and boundary conditions	2
2.3	Computation of the flow	3
3	Oblique hydraulic jump	4
3.1	Generation of the mesh	4
3.2	Initial and boundary conditions	5
3.3	Computation of the flow	6
4	Supercritical flow in symmetrical contraction	7
4.1	Generation of the mesh	7
4.2	Initial and boundary conditions	7
4.3	Computation of the flow on the uniform mesh	8
4.4	Computation of the flow on the non-uniform mesh	9
5	Transcritical flow in long channels	11
5.1	Generation of the mesh	11
5.2	Initial and boundary conditions	12
5.3	Computation of the flow	12
	Bibliography	14

Chapter 1

Examples

This documents aims at explaining how to use the shallow water program on the provided simple examples.

1.1 Prerequisites

On Windows the program NirCmd is required to handle the Gnuplot windows and can be downloaded from the Web.

Gnuplot is called inside the Fortran program in order to plot the convergence of the solution in case of steady flows. Gnuplot must be callable from the Terminal and must therefore be mentioned in your environment variable PATH. The data to plot and the Gnuplot commands are written in local files through subroutines located in the file *SRC/gnufor.f90*. Then Gnuplot is executed, it reads its parameters and data and displays a new window with the convergence of the error. If you encounter any difficulty with Gnuplot, you can still comment the code in *SRC/runge_kutta.f90* that calls *write_xyy_data*, *write_xyy_plots* and *run_gnuplot*.

Chapter 2

Straight channel with slope and bottom friction

This example computes the super-critical flow inside a straight channel of width $B_0 = 2m$, length $L = 1000m$ and of rectangular cross-section. A unit discharge $q = Q/B_0 = 4m^2/s$ is imposed at the inlet, the geometrical slope is $S_0 = 0.002$ and the height imposed at the inlet is $h_i = 0.7m$. This test case corresponds to the steep-slope profile S3 in Section 2.1 of the documentation file *shallow_water.pdf*.

2.1 Generation of the mesh

The geometry of the flow is provided in the file *channel_slope.geo*. This Gmsh (see [1]) contains the geometry and the data required to build an uniform mesh. The length and width of the channel can be changed by the user (parameters L and H). The number of nodes along the x - and y -directions are specified by the parameters Lp and Hp respectively.

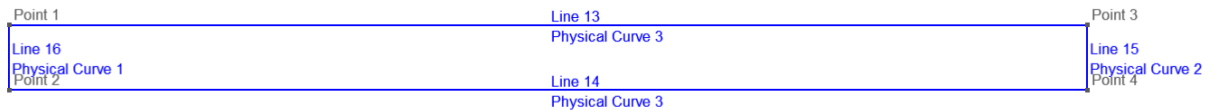


Figure 2.1: Straight channel with slope and bottom friction - Geometry of the flow.

2.2 Initial and boundary conditions

In the previous step, physical entities were created in order to join lines having the same boundary condition. The inlet has the physical tag 1, the outlet has the physical tag 2 and the horizontal walls have the physical tag 3. These tags were referenced in the source file *SRC/Build_initial_condition.f90* to create the initial height, velocity, bathymetric depth, inlet depth and velocity. Feel free to modify this file to your desired values. The physical tags are also referenced in the parameter file *parameters_channel_slope* in order to create a link between the physical tags and the actual boundary type.

```
1 channel_slope.msh : name of mesh file
2 3 : number of boundary types, the next 3 lines
3 1 : Inlet, physical tag in gmsh
4 2 : Outlet, physical tag in gmsh
5 3 : Wall, physical tag in gmsh
```

Take care that during the generation of the initial conditions, the parameter *name of mesh file* must be set to the mesh file. A unit discharge $q = Q/B_0 = 4m^2/s$ is imposed at the inlet, the geometrical slope is $S_0 = 0.002$ and the height imposed at the inlet is $h_{inlet} = 0.7m$. Thus the imposed velocity at the inlet is $u_{inlet} = q/h_i = 5.7143m/s$.

The program *EXE/build_initial_solution* is then launched to read the mesh and create a new Gmsh .msh file that contains the initial values and boundary conditions.

```
EXE\build_initial_solution.exe parameters_channel_slope channel_slope_init.msh
```

2.3 Computation of the flow

The parameter *name of mesh file* in the file *parameters_channel_slope* must be changed to the file that contains the initial values and boundary conditions.

```

1 channel_slope_init.msh           : name of mesh file
2 3                               : number of boundary types, the next 3 lines
3 1                               : Inlet, physical tag in gmsh
4 2                               : Outlet, physical tag in gmsh
5 3                               : Wall, physical tag in gmsh
6 channel_slope_sol.msh           : name of the output, gmsh format
7 channel_slope_sol.dat           : name of the output, dat format
8 channel_slope_sol.dat           : name of the restart file, dat format
9 5000                           : total number of temporal steps
10 500                           : statistics are printed every X steps
11 500                           : solution is saved every X steps
12 9.81                          : g : the gravity constant
13 0.01                          : Manning roughness coefficient
14 1                              : [1] steady or [0] unsteady flow
15 2.4                           : CFL number (used only for steady flows)
16 0.002                         : time step [s] (used only for unsteady flows)
17 0                             : restart from previous simulation [0] no or [1] yes

```

The computation is then launched by the command

```
EXE\shallow.exe parameters_channel_slope
```

A Gnuplot window appears to show the convergence of the solution and the solution is written in the Gmsh file *oblique_jump_uni_sol.msh*. The normal depth $y_n = 1m$ is reached asymptotically at the outlet as indicated in the documentation file *shallow_water.pdf*, Section 2.1.

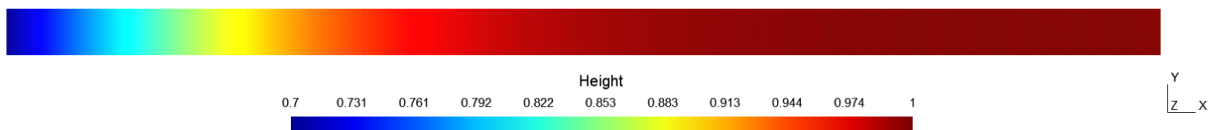


Figure 2.2: Straight channel with slope and bottom friction - Solution after convergence.

Chapter 3

Oblique hydraulic jump

A supercritical flow is deflected inwards by a vertical boundary (angle θ). The user is referred to Section 2.2 of the documentation file *shallow_water.pdf*

3.1 Generation of the mesh

The geometry of the flow is provided in the file *oblique_jump_geom.geo*. This Gmsh (see [1]) contains the geometry and the data required to build an uniform mesh. The angle of the deflection is $\theta = 10 \text{ deg}$ and can be changed in this file (parameter *angle*).

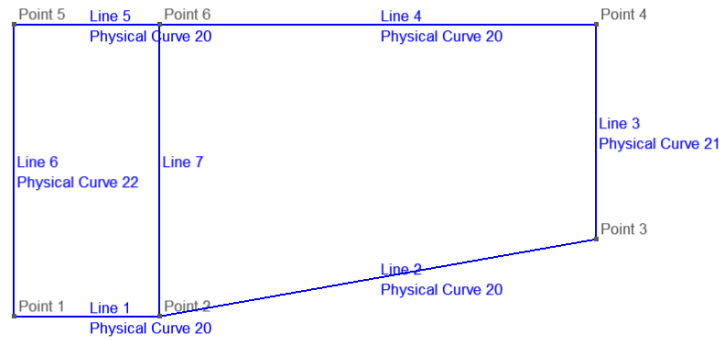


Figure 3.1: Oblique hydraulic jump - Geometry as displayed in the software Gmsh.

The generated mesh looks like

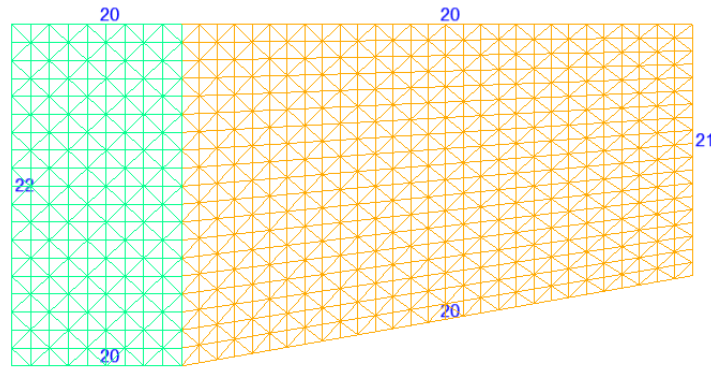


Figure 3.2: Oblique hydraulic jump - Uniform mesh as generated by the software Gmsh.

The user can change the number of elements by modifying the value of the parameter Vp (which corresponds to the number of nodes along the vertical direction). The number of nodes along the horizontal direction is automatically adjusted by the parameters $Hp1$ and $Hp2$.

3.2 Initial and boundary conditions

As shown in Fig. 3.1, physical entities were created in order to join lines having the same boundary condition. The inlet has the physical tag 22, the outlet has the physical tag 21 and the horizontal walls have the physical tag 20. These tags were referenced in the source file *SRC/Build_initial_condition.f90* to create the initial height, velocity, bathymetric depth, inlet depth and velocity. Feel free to modify this file to your desired values. The physical tags are also referenced in the parameter file *parameters_oblique_shock* in order to create a link between the physical tags and the actual boundary type.

1	<code>oblique_jump_uni.msh</code>	: name of mesh file
2	3	: number of boundary types, the next 3 lines
3	22	: Inlet, physical tag in gmsh
4	21	: Outlet, physical tag in gmsh
5	20	: Wall, physical tag in gmsh

Take care that during the generation of the initial conditions, the parameter *name of mesh file* must be set to the mesh file. In the present case, the super-critical boundary conditions at the inlet are $h_{inlet} = 1m$ and $U_{inlet} = (9.0, 0.0)m/s$ respectively. These values are also used to initialize the solution field. The Froude number at the inlet is $Fr = 2.8735$.

The program *EXE/build_initial_solution* is then launched to read the mesh and create a new Gmsh .msh file that contains the initial values and boundary conditions.

`EXE\build_initial_solution.exe parameters_oblique_shock oblique_jump_uni_init.msh`

The resulting Gmsh file that contains the initial values and boundary conditions looks like

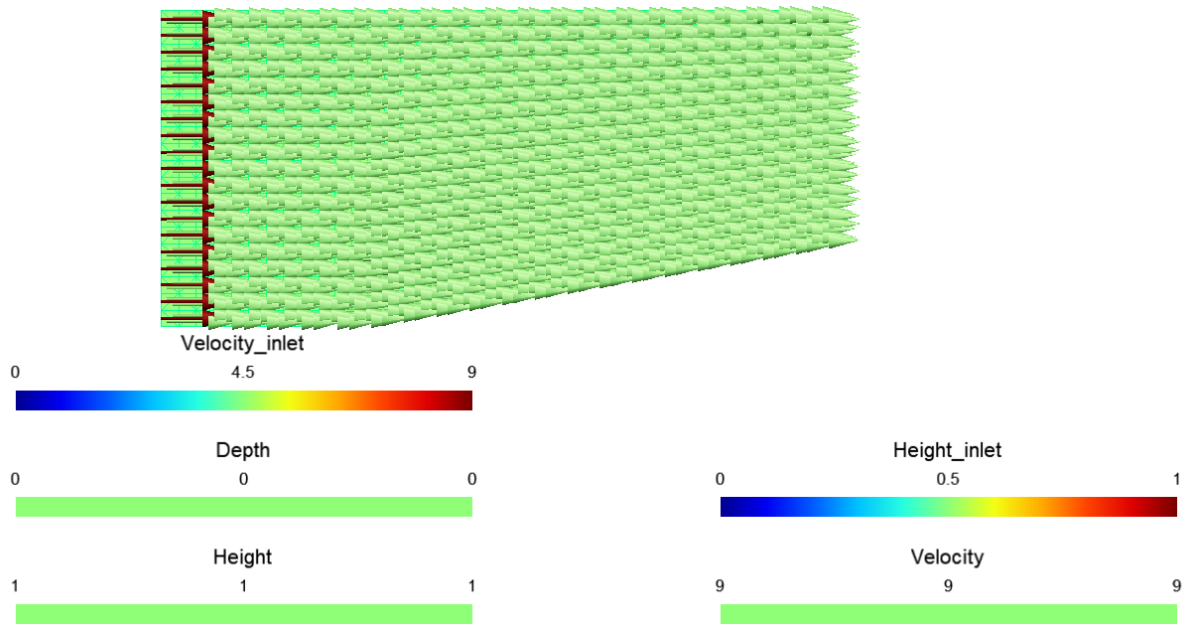


Figure 3.3: Oblique hydraulic jump - Initial values and boundary conditions.

3.3 Computation of the flow

The parameter *name of mesh file* in the file *parameters_oblique_shock* must be changed to the file that contains the initial values and boundary conditions.

```

1 oblique_jump_uni_init.msh          : name of mesh file
2 3                                  : number of boundary types, the next 3 lines
3 22                                  : Inlet, physical tag in gmsh
4 21                                  : Outlet, physical tag in gmsh
5 20                                  : Wall, physical tag in gmsh
6 oblique_jump_uni_sol.msh           : name of the output, gmsh format
7 oblique_jump_uni_sol.dat           : name of the output, dat format
8 oblique_jump_uni_sol.dat           : name of the restart file, dat format
9 2000                               : total number of temporal steps
10 200                               : statistics are printed every X steps
11 500                               : solution is saved every X steps
12 9.81                              : g : the gravity constant
13 0.0                               : Manning roughness coefficient
14 1                                  : [1] steady or [0] unsteady flow
15 2.4                               : CFL number (used only for steady flows)
16 0.001                             : time step [s] (used only for unsteady flows)
17 0                                  : restart from previous simulation [0] no or [1] yes

```

The computation is then launched by the command

```
EXE\shallow.exe parameters_oblique_shock
```

A Gnuplot window appears to show the convergence of the solution and the solution is written in the Gmsh file *oblique_jump_uni_sol.msh*. The theoretical height after the jump is equal to $h_2 = 1.589m$ as indicated in Section 2.2 of the documentation file *shallow_water.pdf*.

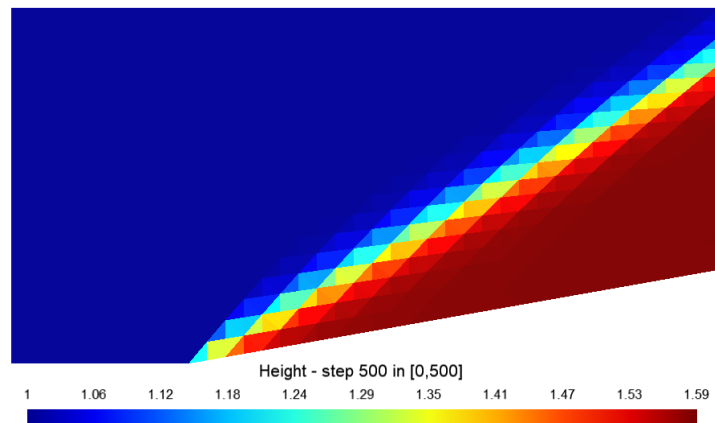


Figure 3.4: Oblique hydraulic jump - Solution after convergence.

Chapter 4

Supercritical flow in symmetrical contraction

This example computes the supercritical flow inside a symmetrical contraction of a channel of rectangular cross-section. This test case corresponds to the supercritical flow described in Section 2.3.1 of the documentation file *shallow_water.pdf*. The geometry of the channel matches the one described in Lai and Chan [2].

4.1 Generation of the mesh

The geometry of the flow is provided in the file *channel_contraction_Lai.geo*. This Gmsh (see [1]) contains the geometry and the data required to build an (non)uniform mesh. The parameter *uniform* allows to switch between an uniform and a nonuniform mesh. Let's keep the parameter *uniform=1* for the moment.

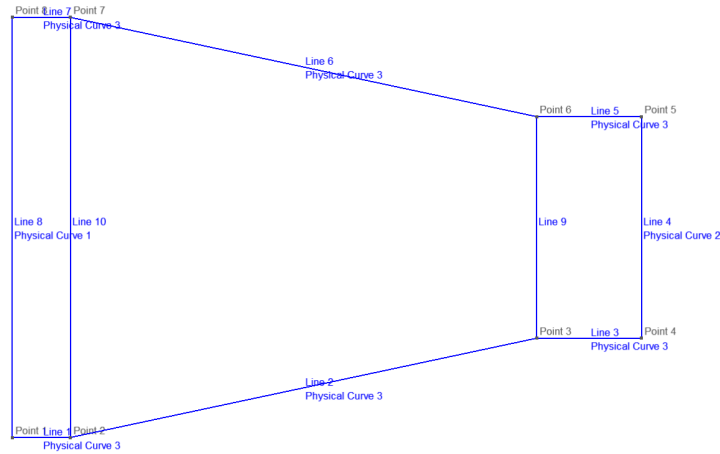


Figure 4.1: Supercritical flow in symmetrical contraction - Geometry of the flow.

The parameters Vp , Hp and $Hp2$ contain the numbers of nodes along the vertical, horizontal middle and horizontal left+right lines respectively. The generated mesh looks like

4.2 Initial and boundary conditions

As shown in Fig. 4.1, physical entities were created in order to join lines having the same boundary condition. The inlet has the physical tag 1, the outlet has the physical tag 2 and

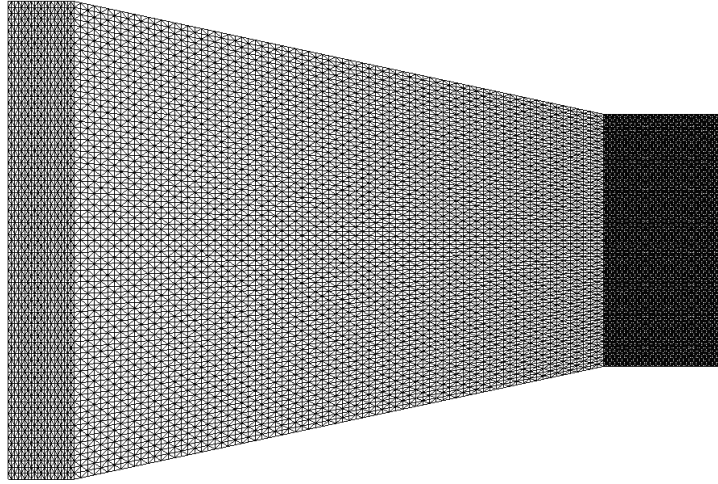


Figure 4.2: Supercritical flow in symmetrical contraction - Uniform mesh.

the horizontal walls have the physical tag 3. These tags were referenced in the source file *SRC/Build_initial_condition.f90* to create the initial height, velocity, bathymetric depth, inlet depth and velocity. Feel free to modify this file to your desired values. The physical tags are also referenced in the parameter file *parameters_channel_contraction* in order to create a link between the physical tags and the actual boundary type.

```

1 channel_contraction_Lai_uni.msh           : name of mesh file
2 3                                           : number of boundary types, the next 3 lines
3 1                                           : Inlet, physical tag in gmsh
4 2                                           : Outlet, physical tag in gmsh
5 3                                           : Wall, physical tag in gmsh

```

Take care that during the generation of the initial conditions, the parameter *name of mesh file* must be set to the mesh file. In the present case, the super-critical boundary conditions at the inlet are $h_{inlet} = 1m$ and $Fr_{inlet} = 2.7$ respectively. These values are also used to initialize the solution field. The velocity at the inlet is thus equal to $u_{inlet} = Fr_{inlet}\sqrt{9.81h_{inlet}} = 8.4567m/s$.

The program *EXE/build_initial_solution* is then launched to read the mesh and create a new Gmsh .msh file that contains the initial values and boundary conditions.

```

EXE\build_initial_solution.exe parameters_channel_contraction
                                channel_contraction_Lai_uni_init.msh

```

4.3 Computation of the flow on the uniform mesh

The parameter *name of mesh file* in the file *parameters_channel_contraction* must be changed to the file that contains the initial values and boundary conditions.

```

1 channel_contraction_Lai_uni_init.msh       : name of mesh file
2 3                                           : number of boundary types, the next 3 lines
3 1                                           : Inlet, physical tag in gmsh
4 2                                           : Outlet, physical tag in gmsh
5 3                                           : Wall, physical tag in gmsh
6 channel_contraction_Lai_uni_sol.msh       : name of the output, gmsh format
7 channel_contraction_Lai_uni_sol.dat       : name of the output, dat format
8 channel_contraction_Lai_uni_sol.dat       : name of the restart file, dat format
9 4000                                       : total number of temporal steps
10 100                                       : statistics are printed every X steps
11 500                                       : solution is saved every X steps

```

```

12 9.81          : g : the gravity constant
13 0.00          : Manning roughness coefficient
14 1            : [1] steady or [0] unsteady flow
15 2.4          : CFL number (used only for steady flows)
16 0.002        : time step [s] (used only for unsteady flows)
17 0            : restart from previous simulation [0] no or [1] yes

```

The computation is then launched by the command

```
EXE\shallow.exe parameters_channel_contraction
```

A Gnuplot window appears to show the convergence of the solution and the solution is written in the Gmsh file *channel_contraction_Lai_uni_sol.msh*. As indicated in Section 2.3.1 of the documentation file *shallow_water.pdf*, the uniform mesh does not capture the correct location of the reflection of the hydraulic jump on the corner. As a consequence, diamond-shaped cross waves are generated in the downstream section of the channel.

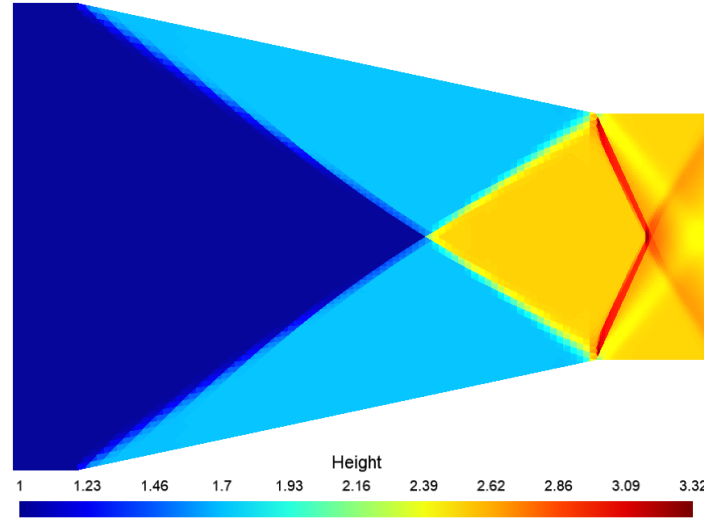


Figure 4.3: Supercritical flow in symmetrical contraction - Solution after convergence on the uniform mesh.

4.4 Computation of the flow on the non-uniform mesh

A new non-uniform mesh can be generated by changing the parameter *uniform* to 1 in the file *channel_contraction_Lai.geo*. A post-processing file .pos is loaded and contains the regions where strong gradients in the solution are present. This view is used to imposed the mesh size in the whole two-dimensional domain. Regions with slow variations will have coarse mesh sizes and regions of strong spatial variation will have small mesh sizes. The generated non-uniform mesh looks is shown in Fig. 4.4.

The converged solution on the non-uniform mesh (Fig. 4.5) captures the correct location of the incoming hydraulic jump on the corner and no diamond-shaped cross waves are generated downstream.

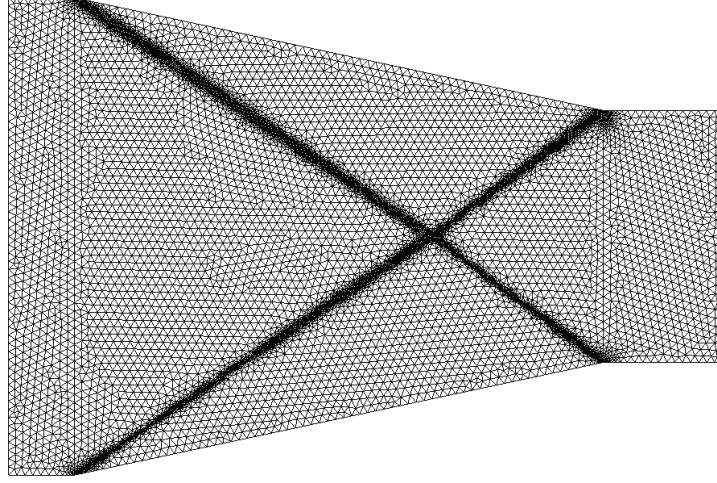


Figure 4.4: Supercritical flow in symmetrical contraction - Non-uniform mesh.

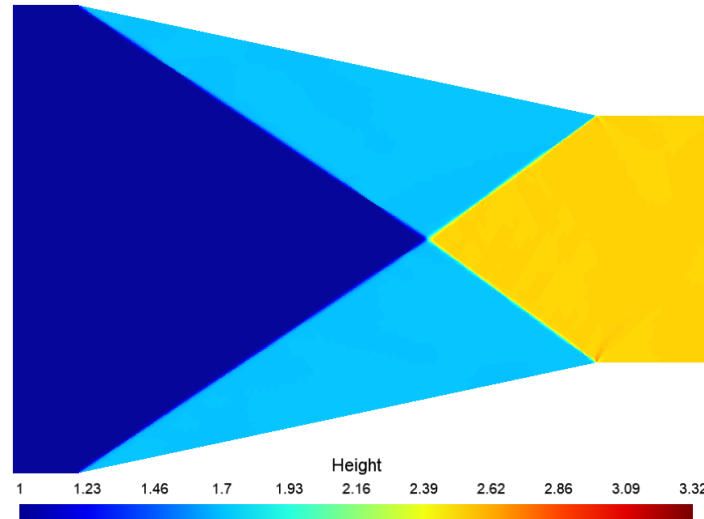


Figure 4.5: Supercritical flow in symmetrical contraction - Solution after convergence on the non-uniform mesh.

Chapter 5

Transcritical flow in long channels

This example computes the transcritical flow inside a symmetrical mild contraction of a channel of rectangular cross-section. This test case corresponds to the supercritical flow described in Section 2.4 of the documentation file *shallow_water.pdf*.

5.1 Generation of the mesh

The geometry of the flow is provided in the file *transcritical_long_channel_Ld500.geo*. This Gmsh (see [1]) contains the geometry and the data required to build a non-uniform mesh. A post view .pos is loaded and aims at positioning the location of the refinement areas where the solution shows fast spatial variations.

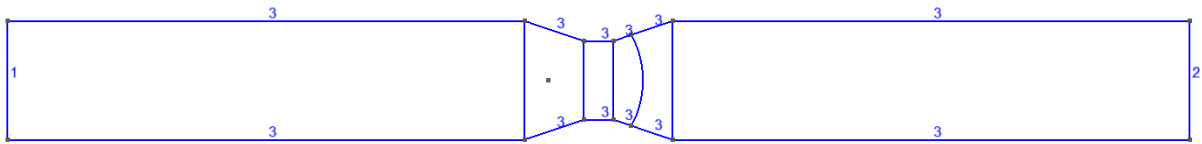


Figure 5.1: Transcritical flow in long channels - Geometry of the flow.

The user can play with the different parameters available in the .geo file in order to modify the geometry or the mesh sizes. The generated mesh looks like

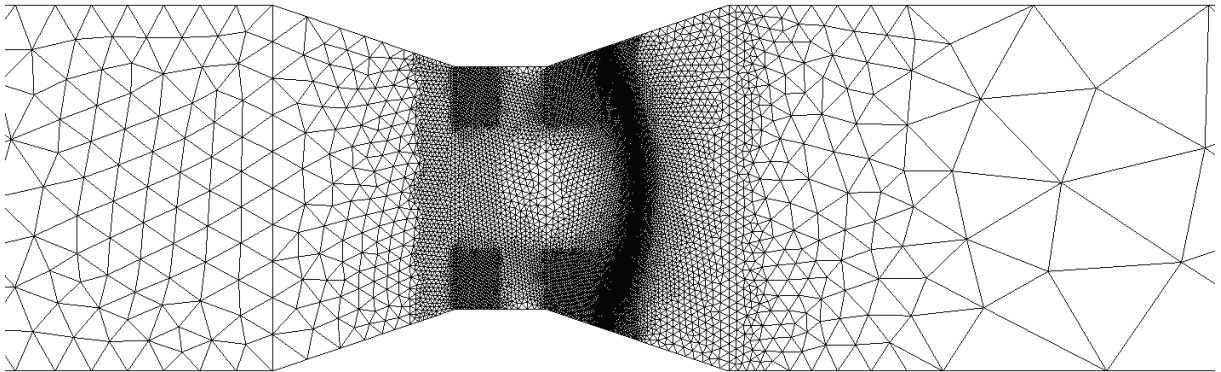


Figure 5.2: Transcritical flow in long channels - Mesh.

5.2 Initial and boundary conditions

As shown in Fig. 5.1, physical entities were created in order to join lines having the same boundary condition. The inlet has the physical tag 1, the outlet has the physical tag 2 and the horizontal walls have the physical tag 3. These tags were referenced in the source file *SRC/Build_initial_condition.f90* to create the initial height, velocity, bathymetric depth, inlet depth and velocity. Feel free to modify this file to your desired values. The physical tags are also referenced in the parameter file *parameters_transc_long_channel* in order to create a link between the physical tags and the actual boundary type.

```

1 transcritical_long_channel_Ld500.msh      : name of mesh file
2 3                                          : number of boundary types, the next 3 lines
3 1                                          : Inlet, physical tag in gmsh
4 2                                          : Outlet, physical tag in gmsh
5 3                                          : Wall, physical tag in gmsh

```

Take care that during the generation of the initial conditions, the parameter *name of mesh file* must be set to the mesh file. Subcritical boundary conditions are imposed at the inlet ($h_{inlet} = y_n = 4.543m$, $u_{inlet} = Q/b_1 h_{inlet} = 2,751m/s$) and at the outlet ($h_{outlet} = y_c = 2.516m$).

The program *EXE/build_initial_solution* is then launched to read the mesh and create a new Gmsh .msh file that contains the initial values and boundary conditions.

```

EXE\build_initial_solution.exe parameters_channel_contraction
                                channel_contraction_Lai_uni_init.msh

```

5.3 Computation of the flow

The parameter *name of mesh file* in the file *parameters_transc_long_channel* must be changed to the file that contains the initial values and boundary conditions.

```

1 transcritical_long_channel_Ld500_i.msh    : name of mesh file
2 3                                          : number of boundary types, the next 3 lines
3 1                                          : Inlet, physical tag in gmsh
4 2                                          : Outlet, physical tag in gmsh
5 3                                          : Wall, physical tag in gmsh
6 transcritical_long_channel_Ld500_s.msh    : name of the output, gmsh format
7 transcritical_long_channel_Ld500_s.dat    : name of the output, dat format
8 transcritical_long_channel_Ld500_s.dat    : name of the restart file, dat format
9 10000                                     : total number of temporal steps
10 200                                      : statistics are printed every X steps
11 1000                                    : solution is saved every X steps
12 9.81                                   : g : the gravity constant
13 0.04                                  : Manning roughness coefficient
14 1                                      : [1] steady or [0] unsteady flow
15 2.4                                   : CFL number (used only for steady flows)
16 0.002                                 : time step [s] (used only for unsteady flows)
17 0                                      : restart from previous simulation [0] no or [1] yes

```

The computation is then launched by the command

```

EXE\shallow.exe parameters_transc_long_channel

```

A Gnuplot window appears to show the convergence of the solution and the solution is written in the Gmsh file *transcritical_long_channel_Ld500_s.msh*. A Matlab/Octave script is also provided (*theory_channel_varying_width_long_channel.m*) in order to compute the theoretical curves used as references.

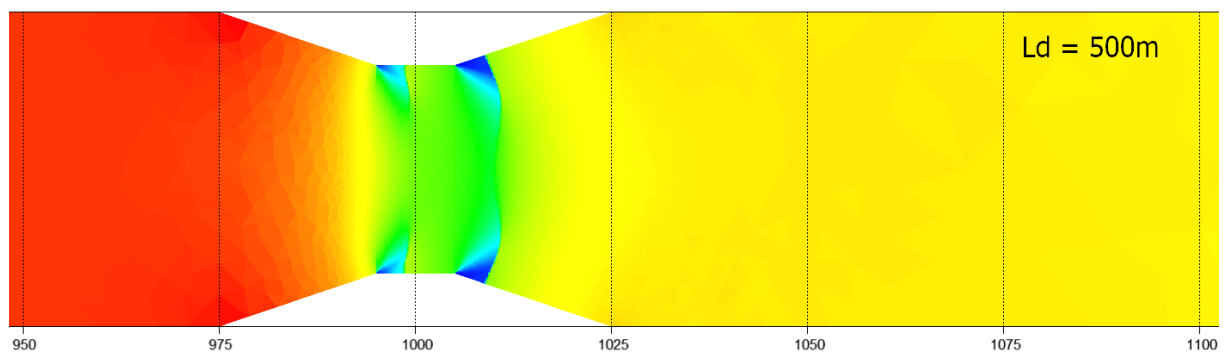


Figure 5.3: Transcritical flow in long channels - Solution after convergence for $L_d = 500m$.

Bibliography

- [1] C. Geuzaine and J.-F. Remacle. Gmsh: a three-dimensional finite element mesh generator with built-in pre- and post-processing facilities. *International Journal for Numerical Methods in Engineering*, 79(11):1309–1331, 2009.
- [2] W. Lai and A.A. Khan. A discontinuous Galerkin method for two-dimensional shock wave modeling. *Modelling and Simulation in Engineering*, Article ID 782832, 2011.