

# Functors

```
module FunctorP where
```

```
Functor :  $\forall \mathcal{U} \rightarrow \mathcal{U}^+ \rightarrow \mathcal{U}^+$   
Functor  $\mathcal{U} = \Sigma \text{Fn} : (\mathcal{U}^+ \rightarrow \mathcal{U}^+) , \Sigma \text{Fm} : (\forall \{X\ Y\} \rightarrow (f : X \rightarrow Y) \rightarrow \text{Fn } X \rightarrow \text{Fn } Y) , (\forall \{X\ Y\ Z\} \rightarrow (f : X \rightarrow Y) \rightarrow (g : Z \rightarrow X) \rightarrow \forall x \rightarrow (\text{Fm } f) (\text{Fm } g\ x) = \text{Fm } (f \circ g)\ x) \times (\forall \{X\} \rightarrow \text{Fm } \text{id} \sim \text{id } \{X = \text{Fn } X\})$ 
```

```
module Functor (func : Functor  $\mathcal{U}$ ) where
```

```
Fn :  $\mathcal{U}^+ \rightarrow \mathcal{U}^+$ 
```

```
Fn = func .pr1
```

```
Fm :  $(\forall \{X\ Y\} \rightarrow (f : X \rightarrow Y) \rightarrow \text{Fn } X \rightarrow \text{Fn } Y)$ 
```

```
Fm = func .pr2 .pr1
```

```
Fm-comp :  $(\forall \{X\ Y\ Z\} \rightarrow (f : X \rightarrow Y) \rightarrow (g : Z \rightarrow X) \rightarrow \forall x \rightarrow (\text{Fm } f) (\text{Fm } g\ x) = \text{Fm } (f \circ g)\ x)$ 
```

```
Fm-comp = func .pr2 .pr2 .pr1
```

```
Fm-id :  $\forall \{X\} \rightarrow \text{Fm } \text{id} \sim \text{id } \{X = \text{Fn } X\}$ 
```

```
Fm-id = func .pr2 .pr2 .pr2
```