## State Space LSTM Model for NLP

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#### Introduction

- Significance of LSTMs in sequence modeling
  - LSTMs' ability to capture long-range dependencies
  - Applications in natural language processing (NLP)
- Interpretability advantages of state space models
- Motivation: Integrating interpretability of state space models with the power of LSTMs
- Reference Paper: [1] State Space LSTM Models with Particle MCMC Inference, Xun Zheng et al., CoRR, 2017

### Overview

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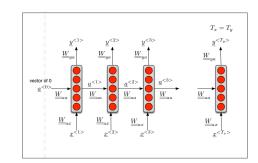
- 1 From LSTM and SSM to State Space LSTM Model (SSL)
- ② Application of the SSL model to the "Topical SSL" experiment
- 3 Inference with Particle Gibbs
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# Reccurent Neural Network: a type of neural network designed to process sequential data

Forward propagation (one hidden layer):

$$s_t = g_1(W_{ss}s_{t-1} + W_{sx}x_t + b_s)$$
  
 $\hat{y}_t = g_2(W_{ys}s_t + b_y)$ 



# Back Propagation Through Time (BPTT) and Vanishing Gradient

To train an RNN we need to back-propagate through layers and through time.

$$\frac{\partial \mathcal{L}}{\partial W_{ss}} = \sum_{t=1}^{t} \frac{\partial \mathcal{L}^{(t)}}{\partial W_{ss}}$$
$$\frac{\partial \mathcal{L}^{(t)}}{\partial W_{ss}} = \sum_{k=0}^{t} \left( \prod_{i=k+1}^{t} \frac{\partial s_{i}}{\partial s_{i-1}} \right) \frac{\partial s_{k}}{\partial W_{ss}}$$

Vanishing gradient appends when  $|rac{\partial s_i}{\partial s_{i-1}}| < 1$  :

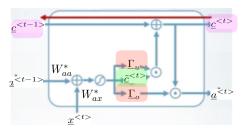
- Contributions from faraway steps vanish and don't affect the training
- Difficult to learn long-range dependencies

# LSTM: a type of RNN introduced to learn long-term dependencies

### Simplified LSTM:

We add a new path: the **memory** cell  $c_t$ 

- The candidate cell value  $\tilde{c}_t$  is added to the memory cell if the update gate  $\Gamma_u$  is open
- The hidden state is output if the output gate  $\Gamma_o$  is open



## LSTM vs. SSM

Model	Pros	Cons
LSTM	Capture long-term dependencies	Not interpretable
SSM	Interpretable	Cannot capture long-term dependencies due to the Markovian nature of the latent variable process

Table: Comparison of LSTM and SSM

## SSL: a combination of SSM and LSTM models

**Main idea**: we place an LSTM on the latent space to simulate the states  $z_t$ . We then generate the observations  $x_t$  from a SSM.

#### Generative process:

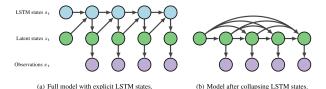


Figure 1: Generative process of SSL.

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# Background

#### Topical SSL:

- $x = (x_1, \dots, x_t, \dots, x_T)$  is a text sequence of length T
- $z = (z_1, \dots, z_t, \dots, z_T)$  is a sequence of unobserved topics characterizing the words in x

#### Example:

- x = ("I", "was", "born", "in", "Palaiseau", "in", "1999")
- z = ("Pronoun", "Verb", "Verb", "Preposition", "City", "Preposition", "Date")

**Goal**: create a generative model. Given a sequence  $(x_1, \ldots, x_t)$ , we want to predict  $(x_{t+1}, \ldots, x_T)$ .

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## Generative Model

 $x_t$  and  $z_t$  are discrete variables:

- $x_t \in \{1, ..., N\}$
- $z_t \in \{1, ..., K\}$

Where N is the size of the vocabulary and K is the number of topics. The SSL model can be written as:

- ①  $z_t|z_{1:t-1} \sim \mathsf{Categorical}(\mathsf{softmax}(\mathit{Ws}_t + b)) \; (\mathit{LSTM})$
- ②  $x_t|z_t \sim \mathsf{Categorical}(\phi_{z_t})$  (SSM)

Where:

• softmax(
$$Ws_t + b$$
) =  $[p_{\omega}(z_t = 1|z_{1:t-1}), \dots, p_{\omega}(z_t = K|z_{1:t-1})]'$ 

• 
$$\phi_{z_t} = [p_{\phi}(x_t = 1|z_t), \dots, p_{\phi}(x_t = N|z_t)]'$$

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## Dataset used, pre processing and technical aspects

#### Dataset:

- IMBD dataset [2] : 25,000 movie reviews, keep n = 200 reviews
- Consider the 5000 "top words": N = 5000
- Truncation of the sequences: T = 170
  - $T_{train} = 100$
  - $T_{\text{test}} = 70$

#### LSTM:

- 64 hidden neurons
- Model length = 10
- Add a dropout layer with p = 0.2
- Optimizer: Adam
- z<sub>t</sub> variables are one hot encoded in LSTM part

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# Particle Gibbs: a way to sample from the variational distribution in EM algorithm

#### Main idea:

We combine stochastic EM algorithm with backpropagation to train the SSL model. For each text and at each iteration of the EM algorithm, we sample  $z_{1:T_{\text{train}}}^*$  from the optimal variational distribution in order to compute the MLE of the SSM and the LSTM. To sample  $z_{1:T_{\text{train}}}^*$  we use an algorithm called **Particle Gibbs**.

## Particle Gibbs Inference

Overview

- Sequential Monte Carlo (SMC) method
- Particle Gibbs inference for sampling from joint posterior
- No factorization assumptions

## Particle Gibbs Inference

#### Algorithm

#### **Algorithm** Inference with Particle Gibbs

```
Require: P: number of particules, T: length of the sequence
 1: Initialize z_0^p = z_0 and \alpha_0^p = \frac{1}{P} for p = 1, \dots, P
 2: for t = 1, ..., T do
         Fix reference path: set a_{t-1}^1 = 1 and z_{1:t}^1 = z_{1:t}^* from the previous iteration
 3:
 4:
      for p = 2, \ldots, P do
 5:
              Sample ancestors a_{t-1}^p \sim \alpha_{t-1}
 6:
         end for
 7:
         for p = 2, \ldots, P do
              Sample particles z_t^p \sim \gamma_t^p and set z_{1, \star}^p = (z_{1, \star}^{a_{t-1}^p}, z_{\star}^p)
8:
9.
         end for
10:
          for p = 1, \ldots, P do
11:
              Compute normalized weights \alpha_t^p
12:
          end for
13: end for
14: Sample r \sim \alpha_T
15: return the particle path z_{1,T}^{a'_T}
```

## Particle Gibbs Inference

#### Recall:

- softmax( $\mathit{Ws}_t + b$ ) =  $[p_{\omega}(z_t = 1 | z_{1:t-1}), \dots, p_{\omega}(z_t = K | z_{1:t-1})]'$
- $\phi_{z_t} = [p_{\phi}(x_t = 1|z_t), \dots, p_{\phi}(x_t = N|z_t)]'$

Let 
$$\phi = [\phi_1, \dots, \phi_K] \in \mathbb{R}^{N \times K}$$
, such as  $\phi[i, j] = p_{\phi}(x_t = i | z_t = j)$ . Here:

- $\alpha_t = p(x_t|z_{1:t-1}) \propto \sum_{k=1}^K \operatorname{softmax}(Ws_t + b)[k] \odot \phi_k$ : unormalized distribution on  $\{1, \ldots, N\}$
- $\gamma_t = p(z_t|z_{1:t-1}, x_t) \propto \text{softmax}(Ws_t + b) \odot \phi[x_t, 1:K]$ : unormalized distribution on  $\{1, \ldots, K\}$

## Training Loop

#### **Algorithm** Training Loop for Topical SSL

```
Require: S_x: set of training sequences, P: number of particules, K: number of topics, N: size
     of the vocabulary, n: number of training samples, n_epochs: number of epochs
 1: for i = 1, ..., n do
         z_{1:T_{\text{train}}}^* \sim \text{i.i.d } \mathcal{U}\{1,\ldots,K\}
 3: end for
 4: for epoch = 1, \dots, n_epochs do
         S_{z_{1:T_{\text{train}}}^*} = []
 5:
 6:
         for i = 1, \ldots, n do
 7:
              Compute z_{1:T_{train}}^* by Particle Gibbs using previous z_{1:T_{train}}^*
             Add z_{1:T_{\text{train}}}^* to S_{z_{1:T_{\text{train}}}}
8:
              Train LSTM with z_{1:T_{\text{train}}}^{x} by back-propagation
9:
              Compute the MLE of the SSM on S_x[1:i] and S_{z_{1:T}^*} [1:i]
10:
11.
          end for
12: end for
```

# Implementation Details

- All the algorithms coded in pytorch
  - GPU usage for LSTM
  - CPU usage for other parts
- n\_epochs = 5
- P = 10
- $K \in \{10, 50, 100\}$
- Evaluation metric: perplexity



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# Perplexity curve for the LSTM model

#### Baseline

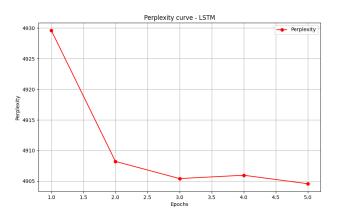
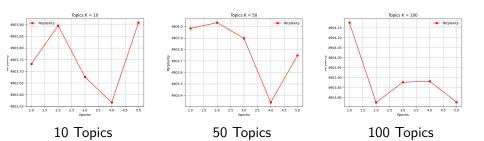


Figure: Perplexity through epochs for standard LSTM

# Perplexity curves for the SSL model



# Topics Visualization (Interpretability)

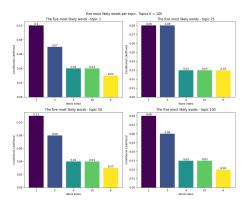


Figure: Latent Topics Visualization

Key insight: Conditionally on topic 50, the third word in the vocabulary is the second word most likely to appear, with a conditional probability of 0.08.

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# Conclusion: pros and cons of SSL

#### Pros:

- Similar performances to the LSTM model on our dataset. In the article, LSTM provides better results, but the amount of data is much greater
- Results are interpretable (main advantage)

#### Cons:

- Computational complexity: assuming that all internal operations can be performed in constant time (which is not the case), the algorithmic complexity of the Particle Gibbs algorithm is  $\mathcal{O}(PT)$  for a single observation
- Concretly, with the same set-up: about 5 minutes to run one epoch with LSTM versus about 4 hours with SSL
- Choice of K: K too high can lead to overfitting whereas K too low can lead to underfitting

## References



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## Q & A

Thank you! Questions?

