

$K = 2$



Let's pretend we have only  
two four points we are  
trying to cluster, with  $k = 2$ .

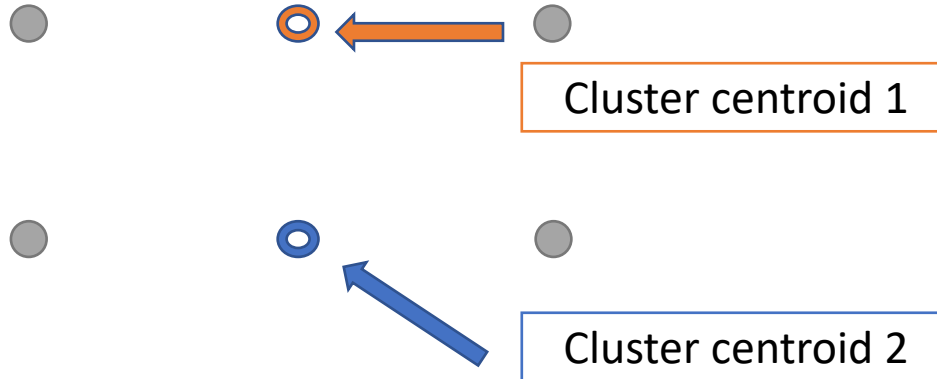
$$K = 2$$



We can see that there are two clusters, and the most logical grouping are the two points on the left, and the two points on the right.

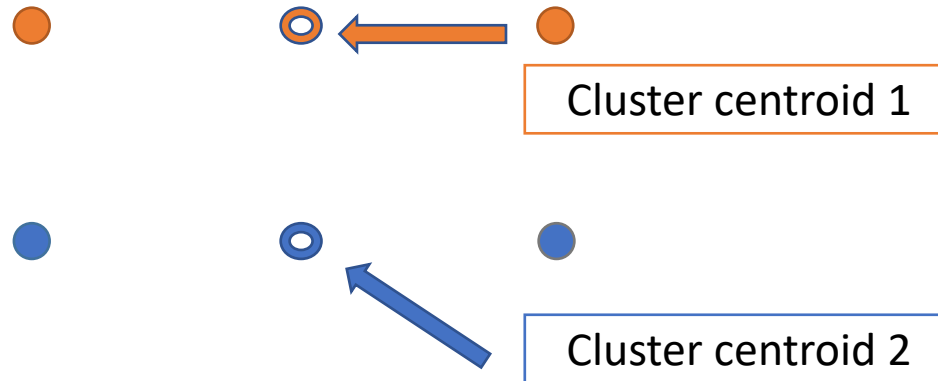
But is k-means guaranteed to find this solution?

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What happens if the  
cluster centroids are  
initialized at these points?

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These become our final state clusters! K-means is a stochastic algorithm, so our results will depend on how the cluster centroids are initialized. There is always the danger of falling into a local minimum.