Prestige as a Driving Force in Cultural Transmission

Saar Egozi

together with Yoav Ram

Efi Arazi School of Computer Science, IDC Herzliya

March 26, 2022 saartk@gmail.com

Contents

2	Abstract	2
	Introduction	2
4	Models and Methods	5
	Continuous Model	5
6	Binary model	7
	Methods	7
8	Results	8
	Approximations	8
10	General Binomial Distribution Approximation	8
	Dirichlet-Multinomial Distribution Approximation	10
12	Numeric comparisons	11
	Fixation probability and time - binary model	12
14	Changing environment	16
	Discussion	21
16	summary	21
	Prestige in the literature	22
18	Evidence from Fijian villages for adaptive learning biases (Henrich and Broesch, 2011)	24
	Using social influence to reverse harmful traditions (Efferson et al., 2020) $\dots \dots \dots$	24
20	The evolution of prestige (Henrich and Gil-White, 2001)	25
	Biased learning may be disfavored when payoffs are uncertain (Takahashi and Ihara, 2019)	25
22	Prestige in medicine (Norredam and Album, 2007)	26
	Collective brains (Muthukrishna and Henrich, 2016)	26
24	Prestige-biased cultural learning (Chudek et al., 2012)	26

Abstract

Copying our role-models have always been an efficient method of acquiring knowledge (Rendell et al., 2010). In this paper, we study the effects of prestige as a cultural transmission bias on the population. A common bias when choosing a role-model to copy is success bias, i.e copying whoever appears successful to us (Henrich and McElreath, 2003). This estimation is based on the performance of the role-model alone, without any other factors. We propose an additional factor we believe aids to better model the cultural inheritance of traits in a large population. Influence bias is a bias evaluated by the number of copiers a role-model already has (Henrich and Gil-White, 2001). We combine these components to what we call the prestige bias and analyze its effects on the dynamics of the population. We present a model of prestige bias as we defined it, and observe the dynamics of the population using computer simulations. We also analyze our model using mathematical approximations. We successfully found mathematical approximations to our model, easing the mathematical analysis and the computation power required for simulations. We show the value of these approximations using simulations, and their robustness to variations such as mutation and other relaxations required for the mathematical proofs. In the binary form of our model, we found alternatives to Kimura's equations for approximating fixation probability and time to fixation of an invading advantageous trait, in both a constant and changing environment. We show that *Influence* solely affects the effective population size. We found that influence acts as an accelerator for a state of the population, matching the rich getting richer it was based on. We believe such model better describes how humans acquire knowledge from one another, mainly in the last years where social networks are very popular. Furthermore, we believe that our model could predict various phenomena in human culture once supplemented with more 46 natural concepts like natural selection and costs.

48 Introduction

60

Traits transmission is when an individual passes on a trait, genetic or behavioral, to another individual. Transmission in nature manifests in two main ways: genetic and cultural. Genetic transmission is when an individual, or several, transmit their genes to their offspring by duplication of their own cells. Cultural transmission is the way individuals transmit cultural traits (i.e behavior) from one another, typically via teaching and demonstrating. Cultural transmission is most common in humans (Cavalli-Sforza and Feldman, 1981, pg. 3) and in primates like chimpanzees (Horner et al., 2010; Kendal et al., 2015). The common cultural traits in humans are behavioral patterns, like personalities and habits, transmitted via observations and verbal discussions. Henrich and McElreath (2007) suggest that cultural learning may be particular to humans, but McComb et al. (2001) suggest that it appears in other mammals as well, elephants for example:

... the possession of enhanced discriminatory abilities by the oldest individual [matriarch] in a group can influence the social knowledge of the group as a whole.

They showed that once a matriarch is removed from the group, the group's survival instincts are inferior. They support their hypothesis by exacting an experiment: playing audio recordings of African elephants, showing that groups with a matriarch recognize and react better to hostile or friendly calls than the groups without one. Moreover, cultural transmission appears in other species, even simpler than mammals, such as *Drosophila*. Battesti et al. (2012) show that oviposition site choice in fruit flies is culturally transmitted. They showed that flies without experience in choosing sites, after spending some time with "experienced" flies, chose the same type of site without directly observing this behavior. Battesti et al. (2012) mention that how the information is transferred is still an open question, but suggest that the flies may use olfactory cues, like other animals such as 70 rodents and bees.

72 Cultural transmission is similar to genetic transmission in many ways, while different in others. Similar to genetic transmission, the effects of culturally transmitted traits can be physiological rather than behavioral, and transmitted from parents to offspring. For example, parents can teach their children to be strong or tall, within some biological limits, by instructing them to maintain a healthy diet and engage in physical activity. Contrary to genetic transmission, the sources of the traits can be many, and not only parents. They can even be unrelated, like teachers, celebrities, coaches, the media, or any stranger that comes in contact with them. Cultural transmission can be vertical, where parents transmit to their children, but also oblique, where other adults transmit traits to children (not their own). Horizontal transmission is also possible, where peers transmit traits to one another. Lastly, vertical transmission in the opposite direction is possible too, where parents copy traits from their children (e.g playing video games) as Cavalli-Sforza and Feldman (1981) and Creanza et al. (2017) suggest. In addition, even when a cultural trait is disfavored by natural selection, it still may spread across a population given transmission biases strong enough to negate the selection bias (Boyd and Richerson, 1988, Ch. 8 pg. 279).

86

94

Transmission bias occurs when a trait has a disproportionate probability from its frequency in the population to be transmitted. For example, Eickbush et al. (2019) show that there are genes 88 of yeast called wtf genes, that bias their transmission to the gametes. They secrete a long life ex-90 pectancy poison, together with a short life expectancy antidote, so a gamete without the gene will perish (the poison will outlive the antidote). Transmission biases, though exist in genetic transmission, are probably more common in cultural transmission. Much like mutation in genetic evolution, one could learn behavioral patterns or traits on his own, usually referred to as innovation, also called individual learning, and just like mutation, without it humans might have been remained at the stone age, or even go extinct. Rendell et al. (2010) suggest that success biased social transmission contribute more to the general success of the population than individual learning. They conducted a tournament for developing learning strategies of a population, where each participant need to devise a strategy. Each strategy must define when individuals should observe and copy from others, and when to engage in individual learning. The best strategies contained a high percentage of social

learning relative to individual learning, even when the error when copying was as high as almost 0.5. It is important to add that all of the strategies include some percentage of individual learning,

and without it the results would be a lot worse. In addition to Rendell et al. (2010), Fogarty et al. (2017) define different types of transmission biases based on success. They define several types of

role-model choosing methods, all assuming that the copier correctly identifies the successful ones. Both studies assume that individuals can successfully evaluate successful individuals. Boyd and

106 Richerson (1988, Ch. 5) suggest that the **evaluation** of success can be divided into three groups: direct bias, indirect bias and frequency-dependent bias. A direct bias is when a variation of a trait

108 is more attractive than others, and is evaluated by *directly* testing the variation of the trait. For example, an individual observing a Ping-Pong match between two others can try both of the pad-

dle grips it observed, and decide what grip is better for it. An indirect bias is when an individual uses the value of one trait to determine the attractiveness of another, so it *indirectly* evaluates the

attractiveness of the role-model. Continuing with the example, a bystander could copy the paddle grip of the Ping-Pong player who scored more points in the match. A frequency-dependent bias is

when an individual has a probability to copy a variant of the trait that is nonlinear to the trait's frequency in the parent's generation. Continuing with the example, when an individual is 80%

116 likely to copy the common paddle grip even when only 60% of the population is using it, it is said to be frequency-biased.

118 Frequency bias could be negative too. Aljadeff et al. (2020) show that societies under competitive conditions are likely to develop diversity in foraging specialization rather than uniformity.

Prestige means having a good reputation or high-esteem, therefore does not directly signify success (although it may imply it), making it an *indirect bias*. Both Boyd and Richerson (1988,

122 Ch. 8) and Fogarty et al. (2017) claim that prestige biases are probably more common in humans than success biases. Boyd and Richerson (1988, Ch. 8) add that maladaptive traits may spread

124 widely in a population, if the indirect bias is strong enough. They claim the bias could lead to a runaway process, caused by a cultural equivalent of sexual selection (Andersson, 1994). On the

other hand, Henrich and Broesch (2011) claim that prestige biases, over generations, can lead to cultural adaptations. According to them, prestige can make a maladaptive trait spread in the

population, but can also accelerate the spread of adaptive traits as well. *Prestige bias* is often mentioned in the literature, but seldom modeled. Boyd and Richerson (1988) have modeled the

130 prestige bias, but didn't include the effects the copiers of a role-model has on the probability of other individuals to choose the same role model.

132 This effect is similar to *conformity* (Denton et al., 2020), which is usually modeled as a different bias. Conformist learning (imitating locally common behaviors) is a known bias in cultural transmission

134 (Molleman et al., 2013), and we suggest that prestige bias is made up by both indirect bias and a new type of conformity. Our new component, *influence*, is assigned to a role-model, contrary to

conformity, which refers to the frequency of a trait in the population, regardless which individuals posses it. The goal of this study is to define a more realistic model for prestige bias and

138 analyze the dynamics of the population it causes.

Today, due to social media, it is easier than ever to estimate the influence individuals have over others, therefore it is probably a major part of humans decision-making process. For example, the number of *followers* a person has in the mobile application *Instagram* may significantly affect how his beliefs are perceived by the population. We want to create a model that better fits reality and simulate scenarios that better mimic cultural transmission dynamics. With a more accurate model of prestige bias, we may understand better how cultural traits are transmitted, and why. Moreover, we could better explain the cause for the spread of maladaptive traits, or the acceleration of adaptive traits often seen in humans.

Models and Methods

148 **Reminder:** A Wright-Fisher model is a mathematical model meant to describe a genetic drift process. This model assumes that generations do not overlap and that each copy of the gene found 150 in the new generation is drawn independently at random from all copies of the gene in the old generation.

A Moran model assumes overlapping generations. At each time step, one individual is chosen to reproduce and one individual is chosen to die. In our models we harness these two models and modify them to describe new mathematical models that we use to expand the basic indirect bias model Boyd and Richerson (1988) suggest.

156 Continuous Model

Consider a population of N individuals, each individual has one trait on a continuous scale. Every generation, N naive individuals (copiers) must choose a trait to copy from one of the individuals of the previous generation (role-models). Similar to a Wright-Fisher model, we assume the generations don't overlap. We base our model on the model of Boyd and Richerson (1988), by assuming only oblique transmission of the traits (Indicator trait - A). Unlike their model, we omit a second trait called Indirectly biased trait to lower complexity. The model's state at time t can be described by:

$$\vec{A}_t = (A_{t,1}, \dots, A_{t,N}) \tag{1}$$

where \vec{A}_t is a vector describing the indicator traits at time t, and \vec{A}_0 is drawn from a standard normal distribution. Each individual from generation t+1, a copier, inherits traits like so:

$$A_i' = F_i(\vec{A_t}) \tag{2}$$

where A'_i is the indicator and indirect trait values correspondingly, that copier i acquires. We use A'_i as an alias for $A_{i,(t+1)}$ for simplicity for the transition between generations $t \to t+1$. F is a function over the t generation traits vector, and is defined differently for every implementation of the **Generic model**.

172 Success bias. Boyd and Richerson (1988, Ch.8, p.247-249) describe a method of inheritance using a blend, i.e weighted average of the trait of the entire generation. They define F as a weighted
174 average of the role-models' traits in a single generation:

$$F_i(\vec{X}) = \sum_{j=1}^{N} \left(G_{ij} \cdot X_{ij} \right) \tag{3}$$

176 where $G_{i,j}$ is:

$$G_{ij} = \frac{\beta(A_{ij})}{\sum_{l=1}^{N} \beta(A_{il})} \tag{4}$$

We define G_{ij} to be the *Success bias* of role-model j in the eyes of copier i. $A_{i,j}$ is the absolute indicator trait value copier i estimates role-model j has:

$$A_{i,j} = A_j + e_i, (5)$$

where e_i is the copier's error of estimation, $\vec{e} \sim N(0, \frac{1}{\eta^2})$. $\beta(X)$ is the bias function, meant to quantify the success bias of a role-model:

$$\beta(A_{i,j}) = b \cdot \exp\left(-\frac{(A_{i,j} - \hat{A})^2}{2J}\right),\tag{6}$$

where \hat{A} is the optimal indicator value and J, b are model parameters to control the "strength" of the bias. $G_{i,j}$ is therefore the relative success score copier i assigns to role-model j, resembling relative fitness in genetic transmission models.

Random choice transmission. Boyd and Richerson (1988) note that the method of transmis-188 sion they use in their model has alternatives. We follow their suggestion and create a model similar to theirs, with random choice as a transmission method: The probability of copier i to choose 190 role-model j as his role-model to copy its traits from is $G_{i,j}$. Once a copier chose its role-model, it will copy both its traits only from his role-model, instead of a weighted average of the entire 192 role-model generation:

$$A_i' = A_{i,j} \tag{7}$$

194 Influence bias. Copiers choose their role-models one by one. After copier i chose a role-model, we denote K_{ij} as the number of copiers that chose role-model j until that point, such that $\sum_{j=1}^{N} K_{i,j} = i$. The stochastic process of role-model choice,

$$\{\vec{K}_i\}_{i=1}^N, \quad \vec{K}_i = (K_{i1}, \dots, K_{iN}),$$
 (8)

198 is described by the recurrence equation

$$K_{i,j} = K_{i-1,j} + S_{i,j}, \quad i, j = 1, 2, \dots, N$$
 (9)

where $S_{i,j} = 1$ if the *i*-th copier chose role-model j and 0 otherwise, and the initial state is $K_{0,j} = 0$. The probability that the *i*-th copier chose role-model j

$$G_{i,j} = P(S_{i,j} = 1 | S_{1,j}, S_{2,j}, ..., S_{i-1,j})$$
(10)

is the prestige of role-model j in the eyes of copier i. This prestige $G_{i,j}$ is determined as follows. 204 First, role-model j is characterized by its indicator value A_j as before, and the estimated indicator value by copier i, $A_{i,j}$ remains as eq. (5). Finally, the prestige $G_{i,j}$ of role-model j in the eyes of copier i is determined by the estimated biased indicator value $\beta(A_{i,j})$ and the number of copiers that chose role-model j before copier i, $K_{i-1,j}$,

208
$$G_{i,j} = \frac{\alpha_j \cdot \beta(A_{i,j}) + (1 - \alpha_j) \cdot K_{i-1,j}}{W_i}, \tag{11}$$

where the weight α_j is a characteristic of role-model j that determines the relative significance of the indicator and the influence in the prestige, and W_i is a normalizing factor to ensure $\sum_{j=1}^{N} G_{i,j} = 1$,

$$W_{i} = \sum_{j=1}^{N} \left(\alpha_{j} \cdot \beta(A_{i,j}) + (1 - \alpha_{j}) \cdot K_{i-1,j} \right).$$
 (12)

212 Binary model

The indicator trait can now manifest in only two phenotypes, and for simplicity we define they can be either \hat{A} or A. In the binary model, the influence is determined by the number of copiers already chosen **any** role-model with either A or \hat{A} , as all role-models with A will contribute to the probability of the trait to be inherited just the same (can be proved with simple induction). Simply put, assuming there are two role-models with the A trait, the probability a copier will copy from either role-model will be the same, and the probability the A trait will be inherited is the sum of both role-models. In the general case, the probability of the i-th individual to inherit trait A, based on eq. (22) is:

$$P_{i,A} = \frac{(N-X)\alpha'\beta(A) + K_A}{i - 1 + (N-X)\alpha'\beta(A) + X\alpha'\beta(\hat{A})} = \frac{(N-X)\alpha'\beta(A) + K_A}{i - 1 + (N-X)\alpha'\beta(A) + \alpha'X}$$
(13)

- where X is the number of role-models with trait \hat{A} and K_A is the number of copiers that already chose A.
- The model begins with the first generation having a single individual with \hat{A} , and the rest have A. The process itself is the same stochastic process as the continuous model.

226 Methods

The main methods we used to experiment and compare our models is using computer generated 228 simulations. In order to establish our claims and base our mathematical approximations of our models, we used the χ^2 test for the full continuous model, and the Kimura's equations of fixation probability and time to fixation for the binary model.

Results

232 Approximations

Currently $\{\vec{K}_i\}_{i=1}^N$ is a stochastic process where each state depends on the previous state, i.e a Markov chain. We wanted to find an equivalent stochastic process that has the same joint distribution on $\{\vec{K}_i\}_{i=1}^N$, but it is possible to evaluate the joint distribution directly without evaluating all the marginal conditional distributions: eq. (9), eq. (10).

We found two approximations to our process, which are summarized here and explained in 238 detail later on:

- K_{i,j} follows the general binomial distribution defined by Drezner and Farnum (1993). More-over, E[K_{N,j}] = N · G_{1,j} if e = e_l = e_m for all l, m. That is, the expected number of copiers of role-model j equals its prestige in the eyes of the first copier, multiplied by the total number of copiers. In addition, we find that when α is homogeneous, α_l = α_m for all l, m, then E[K_{N,j}] = β(A'_j) / β(A'), where A'_j is the estimated indicator value A'_j = A_j + e, and β(A') is the population mean estimated indicator value. That is, the expected number of copiers of a role-model equals its relative biased indicator value, similar to the role of relative fitness in population-genetic models.
- 2. The role-model choice process eq. (8) is equivalent to a Pólya urn model if $e_l = e_m$ for all l, m. Therefore, $\vec{K}_i = (K_{i,1}, \dots, K_{i,N})$ follows a Dirichlet-Multinomial distribution,

$$\vec{K}_i \sim DM(N, \vec{G}_1), \tag{14}$$

where $\vec{G}_1 = (G_{1,1}, \dots, G_{1,N})$. Note that here $G_{i,j}$ is only a function of the indicator values A_j and the weights α_j .

252 General Binomial Distribution Approximation

The general binomial distribution (GBD) is achieved by a series of Bernoulli experiments, with possible dependency between experiments.

Proposition: The number of copiers $K_{i,j}$ follows the GBD, $K_{i,j} \sim GBD(i, \alpha_i \cdot \beta(A'_j))$, when 256 $e_l = e_m$ for all $l, m \in N$ and $A'_j = A_j + e$

Proof: We'll denote $Q_j(k,i) = P(K_{i,j} = k|K_{i-1,j})$ as the probability that exactly k out of i copiers choose role-model j, using conditional probability and eq. (9):

$$Q_j(k,i) = P_j(S_{i,j} = 1|k-1,i-1) \cdot Q_j(k-1,i-1) + P_j(S_{i,j} = 0|k,i-1) \cdot Q_j(k,i-1)$$
 (15)

260 where $S_{i,j} = 1$ when the *i*-th copier chooses role-model *j*.

We see that eq. (15) is equivalent to eq. (2.1) that Drezner and Farnum (1993) define. $Q_j(k, N)$ 262 is the probability that k out of N copiers choose role-model j at the end of the process, which by our previous notation is $k = K_{N,j}$. By describing the process of eq. (8) as (Drezner and Farnum, 264—1993) did, we've completed the proof.

Corollary 1: $\mathbb{E}[K_{N,i}] = N \cdot G_{1,i}$.

In (Drezner and Farnum, 1993, equation 2.3), they show that the expected value of k is: $\mathbb{E}[k] = N \cdot Q_j(1,1)$ (using different notations). $Q_j(1,1)$ is the initial probability to choose role-model j, before any choices are made. $Q_j(1,1) = G_{1,j}$ by definition, therefore we can say that $\mathbb{E}[K_{N,j}] = N \cdot G_{1,j}$.

Corollary 2: $\mathbb{E}[K_{Nj}] = \alpha_j \cdot \beta(A'_j) / \overline{\alpha \cdot \beta(A')}$.

272 **Proof:** The initial prestige of role-model j based on eq. (11) is:

$$G_{1,j} = \frac{\alpha_j \cdot \beta(A'_j)}{\sum\limits_{m=1}^{N} \alpha_m \cdot \beta(A'_m)}$$
(16)

274 The denominator of eq. (16) can also be formulated as:

$$\sum_{m=1}^{N} \alpha_m \beta(A'_m) = N \cdot \overline{\alpha \cdot \beta(A')}$$
(17)

276 where $\overline{\alpha\beta(A')}$ is the mean value of $\alpha_m \cdot \beta(A'_m)$ for all m. Using eq. (17) we get:

$$\mathbb{E}[K_{Nj}] = \alpha_j \cdot \beta(A'_j) / \overline{\alpha \cdot \beta(A')}$$
(18)

278 , completing our proof.

The special case where $\alpha = \alpha_l = \alpha_m$ for all $l, m \in N$ is interesting, because we can evaluate the expected number of copiers using a linear equation:

$$\mathbb{E}[K_{Nj}] = N \cdot \frac{\alpha \cdot \beta(A_j')}{\sum_{m=1}^{N} \alpha \cdot \beta(A_m')} = \beta(A_j') / \overline{\beta(A_j')}$$
(19)

where the only variable is A'_j , because $\overline{\beta(A')}$ is the mean of the distribution we draw the indicator values from, modified by some constant parameters of β . We can then denote $L = 1/\overline{\beta(A')}$ and write:

$$\mathbb{E}[K_{Nj}] = L \cdot \beta(A_j') \tag{20}$$

286 Dirichlet-Multinomial Distribution Approximation

Reminder: Pólya urn model is a stochastic process that is defined as such: The process consists of N draws from an urn with an initial amount of colored balls of M colors. When a ball is drawn, it is then placed back in the urn together with an additional new ball of the same colour. Let $\vec{U_i} = \{u_{i,1}, u_{i,2}, ..., u_{i,M}\}$ where $u_{i,j}$ is the number of balls of the j-th color in the urn after i draws. Let $S_{i,j} = 1$ when drawing a j colored ball on the i-th draw, and 0 otherwise. The probability that $S_{i,j} = 1$ given $\vec{U_{i-1}}$ is:

$$P(S_{i,j} = 1|\vec{U_{i-1}}) = \frac{u_{i-1,j}}{\sum_{m=1}^{M} u_{i-1,m}} = \frac{o_j + w_{i-1,j}}{\sum_{m=1}^{M} o_m + w_{i-1,m}}$$

$$= \frac{o_j + w_{i-1,j}}{i - 1 + \sum_{m=1}^{M} o_m}$$
(21)

294 where o_j is the initial number of balls of the colour j in the urn, and $w_{i,j}$ is the number of new balls that were added to the urn after i draws of the color j.

296 **Proposition:** process $\{\vec{K}_i\}_{i=1}^N$ is equivalent to a *Pólya urn model* when $e = e_i = e_j$ and $\alpha = \alpha_j = \alpha_i$ for all $i, j \in N$.

Proof: We denote α' as the odds ratio between the weights of the indicator and the influence $(\alpha' = \frac{\alpha}{1-\alpha})$. Using eq. (11) we get:

$$G_{i,j} = \frac{\alpha \cdot \beta(A'_j) + (1 - \alpha) \cdot K_{i-1,j}}{W_i} \cdot \frac{1 - \alpha}{1 - \alpha}$$

$$= \frac{\alpha' \beta(A'_j) + K_{i-1,j}}{\sum_{m=1}^{N} \alpha' \beta(A'_m) + K_{i-1,m}}$$

$$= \frac{\alpha' \beta(A'_j) + K_{i-1,j}}{i - 1 + \sum_{m=1}^{N} \alpha' \beta(A'_m)}$$
(22)

300

We see that eq. (21) and eq. (22) are equivalent when setting M = N, $o_j = \alpha' \beta(A'_j)$, $w_{i,j} = K_{i,j}$, 302 completing the proof.

Corollary 1: In their paper, Frigyik et al. (2010, section 2) prove that the proportion of different colored balls in a *Pólya urn model* will converge to the Dirichlet distribution as the number of draws approaches infinity, based on *Martingale Convergence Theorem* (Durrett, 1999). We therefore have

an approximation for the relative "weight" or the proportion each role-model has when evaluated as a role-model. Drawing from a Multinomial distribution where the parameters are the modified weights gained from the Dirichlet distribution is viable for selecting the role-model for the next generation. We can therefore sample from a Dirichlet-Multinomial distribution to approximate how many copiers each of the role-models will have: $\vec{K}_i \sim DM(N, \vec{G}_1)$.

Numeric validation: We showed our process is DM (Dirichlet-Multinomial) distributed when there are no errors when copying or evaluating the traits, and when α is homogeneous in the population. To support our proof, we tested our approximation empirically using computer simulations.

314 To test our hypothesis, we used a *goodness of fit* method known as *Pearson's chi-squared test*. In this test, one can reject or accept the null hypothesis, which in our case is the hypothesis that the 316 simulations results were drawn from a DM distribution.

To use this test, we ran many simulations of our original model, and used the mean distribution 318 of copiers. This mean distribution is our observed distribution, and we tested it with the DM expected distribution, using said chi-squared test. We tested multiple variations of the trait weight 320 parameter (α) .

In all our tests, the p-value was 1. This means that the probability to reject the null hypothesis is essentially nonexistent (the usual threshold for a p-value needed to reject H_0 is 0.05 or lower). In addition, we found out that for high α values (above 0.5), very few simulations are needed to reach p-value 1. (less than five simulations for $\alpha = 0.9$, and less than 20 for $\alpha = 0.7$) For very low α values, which means very high influence weight, the number of simulations needed was 100, which is still a relatively small amount. To verify our codes results, we also ran the test for different distributions, for example the uniform distribution (all role-models have exactly one copier).

All these tests resulted in a p-value 0, which means we can likely reject H_0 for these distributions, as expected.

Once we validated our proof for a single iteration of the model, we went on to more complex validations for the entire model.

332 Numeric comparisons

We're interesting in studying the difference between the real binary model as we defined in eq. (13), 334 and the Dirichlet-Multinomial approximation. Specifically, we're interesting in the fixation probability of the favored trait (\hat{A}) and its time to fixation.

The first step was to find the number of simulations needed to sufficiently approximate the real model with the DM approximation. From fig. 1 we see that 1000 simulations or higher is enough.

The next step was to see how the observed metrics (fixation probability and time) varies when relaxing our assumptions we used to prove the DM approximation. First we relaxed our assumption of no mutation. To include mutation in the binary model, it needs to be redefined, since in the original model it was based on the fact the traits are drawn from a continuous scale. In the binary

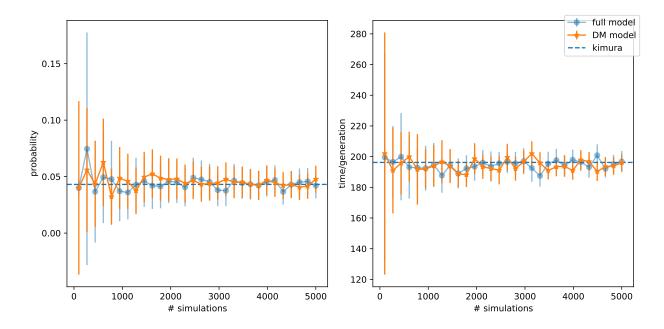


Figure 1: The number of simulations needed to get a good approximation. At 1,000 the approximation is good enough. Error bars represent 95% confidence interval. Population size $N=1000,~\alpha=0.5,~J=1,~\hat{A}=1,A=0.7,~\beta(A)=0.956.$

model mutation will be manifested as an error when evaluating the bias itself. This is easily done by using a heterogeneous J parameter, which controls the strength of the success bias in eq. (6).

In fig. 2 we see the comparison when heterogeneous mutation is applied to both models. When mutation is applied, we sample J_i for each copier i from a normal distribution with varying scale (variance). We can see that even when the standard deviation is 0.1, the metrics of both models are both similar, and close to the Kimura approximation (more details in the next section).

In fig. 3 we relaxed our assumption of a homogeneous α , and used a heterogeneous α instead. Similar to the mutation comparison, we drew α_j for each role-model j from a normal distribution with varying scale. We again see that the metrics of both models are similar in the entire spectrum of our x-axis, and the Kimura approximation is within both confidence intervals.

352 Fixation probability and time - binary model

Kimura's approximation: After establishing a case in the favor of our DM approximation, we wanted to use it to examine the behavior of the population. Specifically, we wanted to analyze the influence of the indicator weight (α) on the fixation probability and time to fixation of the favored phenotype in a binary model. For simplicity, we don't include mutation rate in the binary model approximations. Following Durrett (2008), we used our DM approximation of the model to find the effective population size. From eq. (13) we can derive that the process of inheritance in our binary model is DM distributed with a parameters vector of size two: V = (α'X, (N - X)α'β(A)).

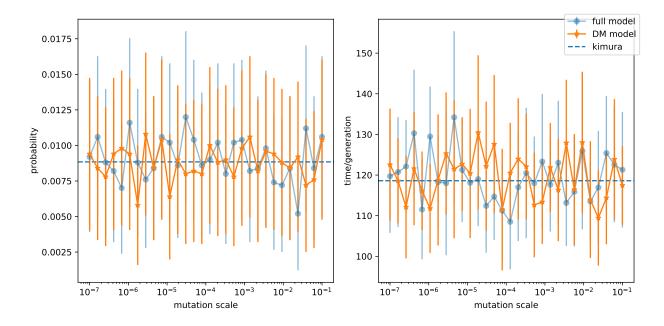


Figure 2: Comparison of the DM approximation and the full model when mutation is included. Even high mutation rate doesn't worsen the approximation, and the data points are close to the mathematical estimation (Kimura's). Error bars are 95% confidence intervals, and are condensed (+- 0.01 probability and +-40 generations) 5000 simulations per data point, $N=1000, \alpha=0.1, \hat{A}=1, A=0.7, J\sim N(1,x^2)$ where x is the mutation scale in the x-axis.

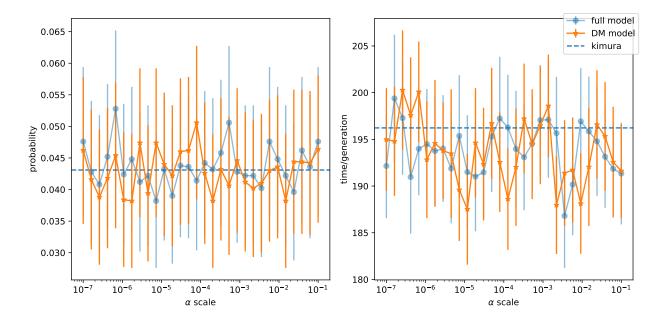


Figure 3: Comparison of the DM approximation and the full model when success weight is heterogeneous. High success weight variance distances the approximation and the full model of generations to fixation from the Kimura's approximation, but not by much (confidence intervals still cover it). Error bars are 95% confidence intervals, and are less condensed (+- 0.03 probability and +-40 generations) 5000 simulations per data point, N = 1000, $\alpha \sim N(0.5, x^2)$, $\hat{A} = 1$, A = 0.7, A = 0.7, A = 0.956.

360 Proposition: 1-β(A) is equivalent to the selection coefficient s in a classic Wright-Fisher model in the diffusion equations meant to approximate the fixation probability and time of the advanta 362 geous trait.

Proof: Let x be the frequency of type \hat{A} in the population with N individuals. Let X be the number of individuals of type \hat{A} so x = X/N. X' is the number of individuals with \hat{A} in the next generation and x' their frequency. By definition $\beta(\hat{A}) = 1$, and for simplicity we'll denote $\beta(A) = \beta$ 366 $(\beta < 1)$.

The expected number of individuals of a DM distribution is:

$$E[X'] = N \frac{\alpha_1}{\alpha_1 + \alpha_2},\tag{23}$$

where $\alpha_1 = \alpha' X$ and $\alpha_2 = \alpha' (N - X) \beta$, from eq. (13). We want to use frequencies instead of quantities to follow Durret's process so:

$$E[x'] = E[\frac{X'}{N}] = \frac{1}{N}E[X']$$
 (24)

372 Putting it together we get:

376

$$E[x'] = \frac{1}{N} N \frac{\alpha' x N}{\alpha' x N + \alpha' N (1 - x) \beta}$$

$$= \frac{x}{x + (1 - x) \beta}$$
(25)

which is identical to the equation in the top of page 253, chap 7.2 in Durrett (2008). We therefore use the same approximation and say that:

$$E[x'] = \frac{x}{x + (1 - x)\beta} = \frac{x}{x + (1 - x)(1 - s)} =$$

$$= x + x(1 - x)s + o(s)$$

$$= x + x(1 - x)(1 - \beta) + o(1 - \beta)$$
(26)

By definition, x is constant, so E[x] = x. We continue to calculate E[x' - x]:

378
$$E[x'-x] = E[x'] - E[x] = x(1-x)(1-\beta) + o(1-\beta)$$
 (27)

where when substituting $1-\beta$ with s, we get the same result as Durrett (2008) which is the desired result.

Proposition: $Ne = \alpha N + (1 - \alpha)$, where Ne is the effective population size of our binary model.

382 **Proof:** The variance of a DM distribution is:

$$V(X') = N \frac{\alpha_1}{\alpha_1 + \alpha_2} (1 - \frac{\alpha_1}{\alpha_1 + \alpha_2}) (\frac{N + \alpha_1 + \alpha_2}{1 + \alpha_1 + \alpha_2})$$
(28)

384 And again, we want to use frequencies so:

$$V(\frac{X'}{N}) = \frac{1}{N^2}V(x') \tag{29}$$

Putting it together with our model's notations:

$$V(x') = \frac{1}{N^2} N \frac{x}{x + (1 - x)\beta} \left(1 - \frac{x}{x + (1 - x)\beta}\right) \left(\frac{N + \alpha' x N + \alpha' N (1 - x)\beta}{1 + \alpha' x N + \alpha' N (1 - x)\beta}\right)$$
(30)

388 Like Durret, we'll use the zero order of the approximation when $\beta \approx 1$, so:

$$\frac{x}{x + (1 - x)\beta} \approx x \tag{31}$$

390 and we also use $\beta \approx 1$ for the entire variance expression and get:

$$V(x') \approx \frac{1}{N}x(1-x)\left(\frac{N+\alpha'xN+\alpha'N-\alpha'xN}{1+\alpha'xN+\alpha'N-\alpha'xN}\right)$$
$$= x(1-x)\left(\frac{1+\alpha'}{1+\alpha'N}\right)$$
(32)

392 Again following Durret we want to calculate:

$$V(x' - x) = V(x') - V(x) \approx x(1 - x)(\frac{1 + \alpha'}{1 + \alpha' N})$$
(33)

394 because x is a constant so V(x) = 0

In our model, α' is the odds ratio of a parameter we called "indicator weight", denoted in our 396 model as α , so:

$$\alpha' = \frac{\alpha}{1 - \alpha} \tag{34}$$

Combining eq. (33) and eq. (34) we get:

398

$$V(x'-x) \approx x(1-x)\left(\frac{1+\frac{\alpha}{1-\alpha}}{1+\frac{\alpha}{1-\alpha}N}\right)$$

$$= x(1-x)\left(\frac{\frac{1-\alpha+\alpha}{1-\alpha}}{\frac{1-\alpha}{1-\alpha}}\right)$$

$$= x(1-x)\left(\frac{1}{1-\alpha(1-N)}\right)$$

$$= x(1-x)\left(\frac{1}{\alpha N + (1-\alpha)}\right)$$

$$= x(1-x)\frac{1}{N_e}$$
(35)

- Using our substitute for a selection coefficient, 1β , and the effective population size N_e , we can estimate the fixation probability and time of our binary model.
- The fixation probability derived from Kimura is therefore:

$$P_{fix} = \frac{1 - e^{-2(1-\beta)N_e x}}{1 - e^{-2(1-\beta)N_e}}$$
(36)

where x is the initial frequency of the advantageous phenotype \hat{A} .

The time to fixation can be estimated by:

$$T_{fix} = \frac{1 - P_{fix}}{1 - \beta} \int_0^x \frac{e^{2(1-\beta)\xi} - 1}{\xi(1-\xi)} d\xi + \frac{P_{fix}}{1-\beta} \int_x^1 \frac{1 - e^{-2(1-\beta)(1-\xi)}}{\xi(1-\xi)} d\xi$$
 (37)

where the integrals cannot be solved in closed form, so we can only estimate them numerically.

- To validate our math we ran multiple simulations comparing our binary model with the classic Wright-Fisher model, using different α and β each time, and using the corresponding values of s
- and N_e for the WF simulations. In fig. 4 we changed α (and N_e accordingly) and used a constant β . In fig. 5 we changed β and used a constant α . In both cases we can see that the two models
- behave similarly, and both are approximated well by the Kimura's equations: eq. (36) and eq. (37).

Changing environment

- 414 After finding good estimations for our model in a constant environment, when the favorable trait is always \hat{A} , we want to find an estimation for our model in a changing environment.
- For that we will find an expression for the expected and variance of the change in frequency between t generations. Let $s_t = N(1 \beta_t)$, and $S_n = \sum_{i=1}^n s_i$, where β_t is $\beta(A)$ at time/generation t.
- 418 **Proposition:** $E\left[\frac{X_t}{N} x\right] \simeq \frac{1}{N} S_t x(1-x)$, $V\left(\frac{X_t}{N}\right) \simeq \frac{1}{N_e} t x(1-x)$, where x is the initial frequency of the favorable/invading trait and X_t is the number of individuals with the trait at time t.
- 420 The proof is based on the proof of Ram et al. (2018), proving a similar scenario.

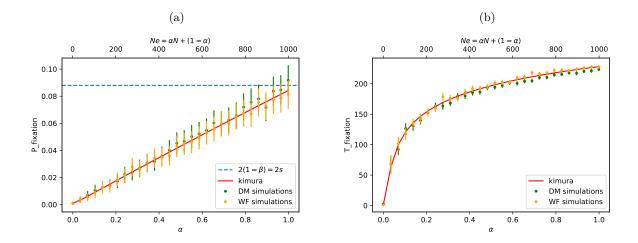


Figure 4: Comparison of the DM approximation and the WF model for different values of the effective population size. The approximation seems very good, and is also condensed around the mathematical equation expectancy. Error bars are 95% confidence intervals. Effective population calculated by $N_e = \alpha N + (1 - \alpha)$. 5,000 simulations per data point, N = 1,000, $\hat{A} = 1$, A = 0.7, $J = 1,1 - \beta = s = 0.044$.

Proof by induction: From eq. (27) we know that

422

424

$$E\left[\frac{X_{t+1}}{N} - \frac{X_t}{N} \middle| X_t\right] = \frac{X_t}{N} \left(1 - \frac{X_t}{N}\right) (1 - \beta_{t+1})$$

$$= \frac{1}{N} \frac{X_t}{N} \left(1 - \frac{X_t}{N}\right) s_{t+1}$$
(38)

Also note that using the definition of $V(y) = E[y^2] - (E[y])^2$

$$E\left[\frac{X_t}{N}\left(1 - \frac{X_t}{N}\right)\right] = E\left[\frac{X_t}{N} - \left(\frac{X_t}{N}\right)^2\right]$$

$$= E\left[\frac{X_t}{N}\right] - E\left[\left(\frac{X_t}{N}\right)^2\right]$$

$$= E\left[\frac{X_t}{N}\right] - V\left(\frac{X_t}{N}\right) - \left(E\left[\frac{X_t}{N}\right]\right)^2$$
(39)

we can now use the induction assumption of $V(\frac{X_t}{N})$ and get

$$E\left[\frac{X_t}{N}\left(1 - \frac{X_t}{N}\right)\right] \simeq E\left[\frac{X_t}{N}\right] \left(1 - E\left[\frac{X_t}{N}\right]\right) - \frac{1}{N_e}tx(1 - x) \tag{40}$$

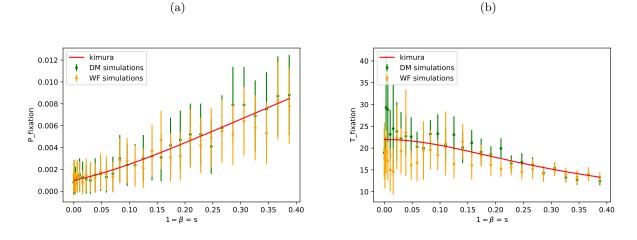


Figure 5: Comparison of the DM approximation and the WF model for different values of the selection coefficient, manifested as success bias in our model. The approximation seems good, and is also condensed around the mathematical equation expectancy. Error bars are 95% confidence intervals. Effective population calculated by $N_e = \alpha N + (1 - \alpha)$. 5,000 simulations per data point, N = 1,000, $\hat{A} = 1$, A = 0.7, J = 1, $\alpha = 0.01$.

From eq. (38) we know that

428

$$E\left[\frac{X_{t+1}}{N} - \frac{X_t}{N}\right] = \frac{1}{N} s_{t+1} E\left[\frac{X_t}{N} \left(1 - \frac{X_t}{N}\right)\right]$$

$$\simeq \frac{1}{N} s_{t+1} \left(E\left[\frac{X_t}{N}\right] \left(1 - E\left[\frac{X_t}{N}\right]\right) - \frac{1}{N_e} tx(1-x)\right)$$

$$\simeq \frac{1}{N} s_{t+1} \cdot E\left[\frac{X_t}{N}\right] \left(1 - E\left[\frac{X_t}{N}\right]\right) - \frac{1}{N_e N} s_{t+1} tx(1-x)$$
(41)

Now we'll omit $O(\frac{1}{Ne \cdot N})$ and get

430
$$E\left[\frac{X_{t+1}}{N} - \frac{X_t}{N}\right] \simeq \frac{1}{N} s_{t+1} \cdot E\left[\frac{X_t}{N}\right] \left(1 - E\left[\frac{X_t}{N}\right]\right) \tag{42}$$

We'll now look at the induction assumption to see that

$$E\left[\frac{X_t}{N} - x\right] = E\left[\frac{X_t}{N}\right] - E[x] = E\left[\frac{X_t}{N}\right] - x,\tag{43}$$

so using the assumption we get

$$E\left[\frac{X_t}{N}\right] \simeq \frac{1}{N} S_t x (1-x) + x$$

$$1 - E\left[\frac{X_t}{N}\right] \simeq 1 - \frac{1}{N} S_t x (1-x) + x \tag{44}$$

we'll use both expressions in eq. (42) and get

436
$$E\left[\frac{X_{t+1}}{N} - \frac{X_t}{N}\right] \simeq \frac{1}{N} s_{t+1} \left(\frac{1}{N} S_t x(1-x) + x\right) \left(1 - \frac{1}{N} S_t x(1-x) + x\right)$$

$$\simeq \frac{1}{N} s_{t+1} \cdot x(1-x)$$
(45)

after again omitting $O(\frac{1}{N^2})$ parts of the equation. To conclude our proof, we see that

$$E\left[\frac{X_{t+1}}{N} - x\right] = E\left[\frac{X_{t+1}}{N} - \frac{X_t}{N}\right] + E\left[\frac{X_t}{N} - x\right]$$
(46)

so again using the induction assumption, together with eq. (45) we get

$$E\left[\frac{X_{t+1}}{N} - x\right] \simeq \frac{1}{N} s_{t+1} \cdot x(1-x) + \frac{1}{N} S_t \cdot x(1-x)$$

$$\simeq \frac{1}{N} x(1-x)(S_t + s_{t+1})$$

$$\simeq \frac{1}{N} S_{t+1} x(1-x)$$
(47)

which proves the first part of our preposition.

442 For the second part, we'll use a property of variance:

$$V\left(\frac{X_{t+1}}{N}\right) = E\left[V\left(\frac{X_{t+1}}{N}\middle|X_t\right)\right] + V\left(E\left[\frac{X_{t+1}}{N}\middle|X_t\right]\right) \tag{48}$$

using eq. (38) we see that:

440

$$E\left[\frac{X_{t+1}}{N}\middle|X_{t}\right] - E\left[\frac{X_{t}}{N}\middle|X_{t}\right] = \frac{1}{N}s_{t+1}\frac{X_{t}}{N}\left(1 - \frac{X_{t}}{N}\right)$$

$$E\left[\frac{X_{t+1}}{N}\middle|X_{t}\right] = \frac{X_{t}}{N} + \frac{1}{N}s_{t+1}\frac{X_{t}}{N}\left(1 - \frac{X_{t}}{N}\right)$$

$$(49)$$

446 Using eq. (35) we get:

$$V\left(\frac{X_{t+1}}{N}\middle|X_t\right) = \frac{1}{N_e}\frac{X_t}{N}\left(1 - \frac{X_t}{N}\right) \tag{50}$$

and using the equation $y'(1-y') \simeq y(1-y)$ on the first part of eq. (48) we get:

$$E\left[V\left(\frac{X_{t+1}}{N}\middle|X_t\right)\right] = \frac{1}{N_e}E\left[\frac{X_t}{N}\left(1 - \frac{X_t}{N}\right)\right] \simeq \frac{1}{N_e}x(1-x)$$
(51)

and moving on to simplify the second part of eq. (48) using eq. (49):

$$V\left(E\left\lceil \frac{X_{t+1}}{N} \middle| X_t \right\rceil\right) = V\left(\frac{X_t}{N} + \frac{1}{N}s_{t+1}\frac{X_t}{N}\left(1 - \frac{X_t}{N}\right)\right)$$
(52)

and now, because $\frac{X_t}{N}$ is a frequency, i.e $0 \le \frac{X_t}{N} \le 1$, we know that $V\left(\frac{X_t}{N}\left(1 - \frac{X_t}{N}\right)\right) \le \frac{1}{4}$. We therefore see that:

$$V\left(\frac{1}{N}s_{t+1}\frac{X_t}{N}\left(1-\frac{X_t}{N}\right)\right) \le \frac{1}{4N^2}s_{t+1}^2 \tag{53}$$

and so it can be ignored. Combining our equations we get:

$$V\left(E\left[\frac{X_{t+1}}{N}\middle|X_{t}\right]\right) = V\left(\frac{X_{t}}{N}\right) + O\left(\frac{1}{N^{2}}\right) \simeq V\left(\frac{X_{t}}{N}\right)$$
(54)

Using the induction assumption and eq. (51):

458
$$V\left(\frac{X_{t+1}}{N}\right) \simeq \frac{1}{N_e}x(1-x) + \frac{1}{N_e}tx(1-x) \simeq \frac{1}{N_e}x(1-x)(t+1)$$
 (55)

proving the second part of our preposition.

454

460 Following our proof, we can say that after many cycles, we can use a modified version of our fixation probability:

$$P_{fix} = \frac{1 - e^{-2\frac{S_n}{n}N_e x}}{1 - e^{-2\frac{S_n}{n}N_e}}$$
 (56)

where $\frac{S_n}{n} = \frac{k-l}{k+l}(1-beta)$, n=k+l. Put into words, we use the average selection coefficient of a cycle (k+l) as the selection coefficient in our original equation. In our proof we showed that the expected change in frequency and variance is only manifested in the selection coefficient S_n , and that we can use those modified equation as a base for Kimura's equation.

We wanted again to validate our results, using simulations. This time, the number of parameters increased: in addition to α, β , there are also k, l as model parameters.

We again tried different variations of the parameters, changing only one of them at a time. In 470 fig. 6 we can see that α on it's own doesn't cause any deviation for the the estimation. β however affects the results greatly.

We plotted along the modified estimation the original Kimura's estimation, as a limiter. We suspect that when β is too large, there won't be many cycles in the simulations. This might happen if either the population reaches a high frequency of the ideal trait after only a few cycles,

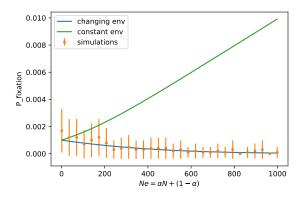
or it get extinct very quickly, because the advantage it had in the k generations wasn't sufficient, and the same s becomes a greater disadvantage when the environment changes resulting in a fast

476 and the same s becomes a greater disadvantage when the environment changes, resulting in a fast extinction.

In the larger values of beta we even see a deviation from the original estimation environment, but it's to be expected, because Kimura's equations are only viable for small s values.

We then also tried changing the composition of the cycle, by keeping a constant n = 40, but changing k, l accordingly.

In fig. 7 we see that the larger k relative to l, the closer the modified equation is to the original estimation of the constant environment. When using higher values of n, the simulation results doesn't fit the equation result as with lower values. This is due to the fact that our proof, and



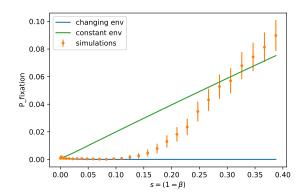


Figure 6: Model simulations compared with both the constant environment and the changing environment equations with different effective populations sizes and selection coefficients. Changing the effective population size doesn't affect the approximation, and it is condensed the mathematical expected values across all values. High values of success bias (s > 0.1) will distance the simulations from the changing environment expected values. Very high values (s > 0.35) will even deviate from the constant environment expected values. This is expected because Kimura's approximation are only viable for low selection coefficient values. 10,000 simulations per data point, $N = 1,000, \hat{A} = 1, A = 0.9, J = 1.$

therefore our equation is more accurate when more cycles occur. When n is high, there will be less cycles, and the simulations will get closer to the constant environment equation. 486

Discussion

488 summary

490

494

498

500

Cultural transmission is the phenomenon of which cultural elements, in the form of attitudes, values, beliefs, and behavioral patterns, are transmitted between individuals, typically via copying. Some cultural traits can be more likely to be copied by others, regardless of their frequency in the population. Such transmission biases are common in cultural transmission processes. Many models 492 are based on the assumption that success can be correctly identified, and easily copied. Here we assume that success isn't correctly identified, therefore individuals may use other indicators to try and estimate the success of potential role-models. We believe, as Fogarty et al. (2017) suggest, that 496 prestige biases are more common in nature than success biases, since estimating success accurately is harder. We investigated the effects of prestige on a population: we studied the behavior of an invading trait, analyzed its dynamics mathematically, and extended the basic constant environment to a changing one. We believe prestige is composed of two main components: a trait that indicates success (but doesn't guarantee it), and the influence the individual already has on others, i.e number of individuals already chose him as a role-model. We suggest a model for prestige bias, 502 inspired by the model Boyd and Richerson (1988) have suggested, and added the influence bias to it. We approximated our models using various distributions, and compared them to

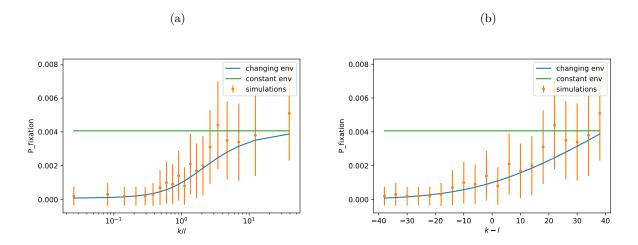


Figure 7: Model simulations compared with both the constant environment and the changing environment equations for different compositions of the environment cycle. When k < l the approximation is good. When k > l, the approximation and the simulations are both very close to the constant environment approximation. 10,000 simulations per data point, N = 1,000, $\hat{A} = 1$, A = 0.8, A =

the original model using simulations. We showed that a Rich getting richer type of model can be approximated well by the general binomial distribution and the dirichlet multinomial distribution. We experimented with constant and changing environment in our model, and created a variation of a binary model for easier mathematical and computational analysis. We believe that
in this era of social media it is easy to estimate one's influence over others. It is therefore crucial to model the cultural biases more realistically than success bias based model, and we believe including
influence is crucial for that purpose.

With a more realistic model of a common cultural transmission bias, we may be able to better understand decision-making processes in humans, including life-changing choices such as occupation or a life partner. Our model can be expanded in multiple ways: observing the effects of different bias functions, including errors in estimating the influence, combining factors of cost when copying from an influential role model (not all could afford to copy from the most popular role-model), and analyzing the differences when including several optimal values for the indicator trait (multiple preference traits in the population).

518 Prestige in the literature

522

524

So far we discussed prestige as a main bias in humans, and to some extent in non-human species.

520 Here we further base our claims and present additional appearances of prestige in nature and in the literature.

King and Cowlishaw (2009) describe a manifestation of prestige in the form of leadership in animals. According to them, there are two main approaches to decision makings of groups in nature: leadership and consensus. Prey leaders would lead the pact when traveling, while other animal

group leaders will decide on a nesting site or foraging patches. They found out that leadership is 526 observed mostly when there is a profound social network in the group, and when there are individuals that present leadership behavior. Leaders would usually be high ranking members in the 528 group, such as elders, individuals with many kin relations, or posses other dominant traits. When no individual posses such traits, or when the social network is lacking, a consensus is more likely 530 to occur. When a leader is present, they will have greater selection costs, such as higher risk for 532 predation, being poisoned by unknown experimental patch, but also greater benefits. For example, given the route to the foraging site was successful, the leader and his closest followers would gain most of the food, unlike in a consensus, where the food would be shared more equally. It appears 534 leaders appear in simple organisms as well, like fish. In these organisms however, the leader would 536 usually be the hungriest or the weakest, while the rest would prefer to follow, minimizing their costs. In baboons however, King and Cowlishaw (2009) describe many benefits for the closest associates of the dominant male, such as protection from predators. This is an instance of sexual-selection. 538 where the leader, whose survival chances are lower, gains more sexual partners due to the benefits. ("The greater the risk, the greater the reward") What they describe could be the origins of what 540 we know today as prestige. In their paper, they show that in nature, when survival is the main concern at all times, the leaders wouldn't be chosen due to their superior abilities, but because 542 they have the least to lose. When in said position of leadership, there are greater risks, but greater 544 rewards to come with it. In humans, leadership also has its perks and costs. Leaders can make decisions that would benefit them and their closest followers the most, while still maintaining group 546 cohesion. However, wrong decision making that would harm the group could result in harm (media, social status, even violent behavior of subjects on certain cases). In our society it is less common to worry about mere survival, and so the prestigious positions, even though are not without risks 548 and costs, are not as dangerous as for animals in nature. This may be the reason humans strive for the prestigious positions, as they may reap rewards greater than the risk and costs to achieve them. 550 This is in complete contrast to animals, where the weakest/hungriest is driven to lead, compared to humans where leadership positions are mostly competitive. 552

Van Vugt and Smith (2019) suggest a different view of leadership. They note that most discussions assume there is one type of leadership, as seen above, and so they differ in their definitions.

Van Vugt and Smith (2019) suggest a way to solve said contradiction by defining two types of leaderships: prestige-based and dominance-based. They present classical views of leaderships by

Confucius and Machiavelli. Confucius views leaders as role models who exercise influence through possessing superior knowledge, skills, and (outstanding) personal qualities. This description is very similar to our indicator trait. By contrast, Machiavelli views leaders as rulers who exercise influence by imposing costs through (the threat of) punishment. They say that these two opposing views are both partially supported by the available evidence but each one on its own offers an incomplete view into the complex and dynamic processes of leadership.

Our current model doesn't reflect the model described in this article, but several adjustments could be made in order to match it. If we assume there's a correlation between trait value to a type of leadership (so in our binary model, one trait would be of prestige, and the other of dominance) we can implement their suggested model. For that we would need to add cost-benefit parameters, so the ones choosing prestige will be rewarded, but pay more, while the ones choosing dominance would pay less, but gain less benefits. It could be interesting to see the dynamics and relations between our model parameters and these cost-benefit parameters.

572 Henrich and Gil-White (2001) support said claim that there are two types of leadership, and also define the two as prestige based and dominance based leadership types. By their definition, 574 the latter is defined by acquiring social status by using aggression, intimidation and violence. It is also more common than prestige in non humans. Their definition of prestige is somewhat synonymous with ours. According to their manuscript, prestige is composed both of estimation in 576 the eyes of people (our indicator/success trait) and commanding position in people's minds, i.e number of copiers people think they have, which they define as influence (similar to our definition 578 for influence). In their paper, they show that prestige evolved from natural selection, as an efficient 580 process to extract reproductive benefit from the flow of socially transmitted information. Simply put, prestige is a natural step where social learning exists, due to saving costs of individual learn-582 ing. It could be interesting in the future to expand our model using this idea: observing the copier trait of evaluation, rather than only observing the evolution of the indicator trait copied. Henrich 584 and Gil-White (2001) suggest that the most skilled role-models will, on average, end up with most copiers. Their research, definitions and results, is consistent with ours.

So far we presented the theory behind prestige, and it's appearance in nature. The following will show the appearances of prestige biases in humans, and in recent times.

586

588

Chudek et al. (2012), for example, tested the existence of prestige in young children. Chudek et al. (2012) report the first direct tests in children that suggest the existence of prestige bias, a 590 tendency to learn from individuals to whom others have preferentially attended, learned or deferred. 592 Their definition of prestige is similar to our *influence bias*, and brings concrete proof of its existence and effects. Their study showed that the odds of 3-4 years-old children learning from an adult model to whom by tanders had previously preferentially attended for 10 seconds were over twice those 594 of their learning from a model whom bystanders ignored. In addition to this first study, they also discovered prestige effects are domain-sensitive. They saw that prestigious models were listened to 596 by most when demonstrating artifact-use, but not as much as when presenting food preferences. It lead Chudek et al. (2012) to believe that when the trait is costly to learn individually, prestige will 598 have a higher effect. It would be interesting to include costs in our model to try and observe these 600 effects and their dynamics in the simulations of a larger population than this study.

Henrich and Broesch (2011) researched Fijian villages, looking for evidence of social learning biases and their origins. They mention that:

evolutionary theorists propose that natural selection has favored the emergence of psychological biases for learning from those individuals most likely to possess adaptive information.

Their goal is to bridge from the laboratory to the field by examining if and how these biases emerge in a small-scale society. During their research they found that:

Fijian villagers (ages 10 and up) are biased to learn from others perceived as more successful/knowledgeable, both within and across domains (prestige effects).

610

618

634

636

Their research shows promising evidence for our prestige model, suggesting that copying from others who are *perceived* as successful, rather than actually are successful. In their paper, they show that the social networks representing copier-role-model relationships are centralized, suggesting:

This degree of centralization is consistent with the prediction that people substantially share notions about who is a good cultural model (network centrality), but that individuals' model selections are influenced by multiple factors.

We see here support for both our indicator trait and our influence bias in their data.

Aside from children's learning biases and small villages in a relatively primitive population, we can see prestige in more advanced domains as well, like western medicine. Norredam and Album 620 (2007) present a specific and important effect of prestige - its significance for medical specialties and diseases. They examined literature from 1950 to 2005 regarding the effects of prestige on medicinal 622 practices. They discovered that active, specialized, biomedical, and high-technological types of 624 medicine on organs in the upper part of the bodies of young and middle-aged people were accorded high levels of prestige, while medicine with opposite characteristics had low levels of prestige. They have concluded that such differences in prestige bear consequences for actual priority setting in 626 healthcare systems. They discovered that surgery counts as the most prestigious specialty, while 628 psychiatry is the less prestigious. In addition, doctors tend to rank practices that require more time to master as more prestigious, while other procedures that are considered easier are less prestigious. 630 Simply put, they found that the advance in technology and research was in accordance with the prestige rankings. This means that there may be very important practices that are neglected due 632 to the prestige bias.

As we seen so far, prestige can explain many behaviors and evolution of cultural traits. It is a tool to cheaply estimate and acquire knowledge, which helps an individual to survive and breed. However, it is not always the case, and there could be negative repercussions to this bias, such as invasion of maladaptive traits.

638 Takahashi and Ihara (2019) mention that social learning not only takes the form of random copying of other individuals, but also involves learners' choice of what to learn and from whom to 640 learn. They suggest a best-of-K model where an individual samples k role-models and choose the one he deems most "successful". They mentioned that a previous mathematical analysis has shown that it may sometimes result in maladaptive cultural evolution when the payoffs associated with 642 cultural variants vary stochastically. In such a case, learners may be selectively disfavored and in the long run replaced by unbiased learners, who simply copy someone chosen at random. They develop 644 new mathematical models that are simpler and mathematically tractable. They found that bestof-k learning, unlike unbiased learning, can facilitate the invasion of an on average inferior variant 646 that sometimes gives a very high payoff. Our model, which includes influence bias, is consistent 648 with that claim. When a maladaptive trait is "piggybacking" a role-model with high influence, said trait could spread in the population, as mentioned. In addition, they show that best-of-k learning 650 can be stable against invasion by unbiased learning if social learning is sometimes combined with individual learning. Our model is based on copying based learning only, but it could be interesting to combine it with individual learning and see how it affects the dynamics of the population. 652

We discussed prestige in depth, and provided several proofs for its existence in nature, humans, and even medicine. We saw it could aid invasion of maladaptive traits, or neglect of important 654 medicinal specialities. But, it can also accelerate reversal of harmful traditions. Harmful traditions can be child marriage, open defecation, and domestic violence, to name a few. Efferson et al. (2020) suggest a mechanism called *spillover*. By their definition, a spillover is when an intervention affect 658 a large enough group in a target population, so that others not included in the intervention starts changing their behavior as well. In their research, they found that there are individuals who act as agents, who are often looked upon, and therefore they are ideal targets for interventions. This is the same concept as our role-models, where a more prestigious individual will be copied more, therefore spreading his trait wider in the population. Their research support therefore in our assumption 662 that there are social biases, conformist influence specifically. They also suggest a way to use this phenomena to change existing traditions in a population. It is very clear however, that just as it can be used to end harmful traditions, the same agents could be used for any negative way that comes to mind.

656

660

664

666

668 Up until now, we showed that cultural transmission is a process that manifests in many species, with emphasis on humans. We also displayed similarities between this process and genetic transmission, while presenting differences between them, specifically selective biases such as influence 670 and prestige. We also presented examples of good and bad usages of such biases. All of these are mainly presented as a parallel process to the natural selection process in regards to physical 672 anatomy, or at least have an indirect effect on it. Muthukrishna and Henrich (2016) offer a take 674 on prestige as a factor of human physical evolution directly. They present a concept called cultural brains - brains that evolved primarily for the acquisition of adaptive knowledge. They build on the hypothesis of Dunbar (2009) that shows that larger, more complex brains can store and 676

manage more information and in turn, this information can support the costs of a larger brain.

Muthukrishna and Henrich (2016) built a model that predicts a strong relationship between brain size and group size, because group size also provides access to more adaptive knowledge. They later present their cumulative cultural brain hypothesis, an approach which proposes that human brains have evolved with an ability and proclivity for selective, high fidelity social learning. As part of this process, there are a variety of strategies and biases that have evolved to hone in on the most adaptive knowledge. These strategies and biases include direct and indirect cues of the popularity of cultural traits (e.g. success and prestige biases). In short, they suggest that some of the reasons for the extreme increase in brain size in humans, are the ability to "cheaply" acquire adaptive knowledge, i.e transmission biases, such as prestige.

References

- 688 Aljadeff, N., Giraldeau, L.-A., and Lotem, A. (2020). Competitive advantage of rare behaviours induces adaptive diversity rather than social conformity in skill learning. *Proceedings of the Royal*
- 690 Society B, 287(1933):20201259.
 - Andersson, M. B. (1994). Sexual selection. Princeton University Press.
- 692 Battesti, M., Moreno, C., Joly, D., and Mery, F. (2012). Spread of social information and dynamics of social transmission within drosophila groups. *Current Biology*, 22(4):309 313.
- 694 Boyd, R. and Richerson, P. J. (1988). Culture and the evolutionary process. University of Chicago press.
- 696 Cavalli-Sforza, L. L. and Feldman, M. W. (1981). Cultural transmission and evolution: A quantitative approach. Number 16. Princeton University Press.
- Chudek, M., Heller, S., Birch, S., and Henrich, J. (2012). Prestige-biased cultural learning: by-stander's differential attention to potential models influences children's learning. Evolution and Human Behavior, 33(1):46-56.
- Creanza, N., Kolodny, O., and Feldman, M. W. (2017). Cultural evolutionary theory: How culture evolves and why it matters. *Proceedings of the National Academy of Sciences*, 114(30):7782–7789.
- Denton, K. K., Ram, Y., Liberman, U., and Feldman, M. W. (2020). Cultural evolution of conformity and anticonformity. *Proceedings of the National Academy of Sciences*.
- Drezner, Z. and Farnum, N. (1993). A generalized binomial distribution. *Communications in Statistics Theory and Methods*, 22(11):3051–3063.
- Dunbar, R. (2009). The social brain hypothesis and its implications for social evolution. *Annals of Human Biology*, 36(5):562–572. PMID: 19575315.
 - Durrett, R. (1999). Essentials of stochastic processes, volume 1. Springer.
- 710 Durrett, R. (2008). Probability models for DNA sequence evolution, volume 2. Springer.
- Efferson, C., Vogt, S., and Fehr, E. (2020). The promise and the peril of using social influence to reverse harmful traditions. *Nature human behaviour*, 4(1):55–68.
- Eickbush, M. T., Young, J. M., and Zanders, S. E. (2019). Killer meiotic drive and dynamic evolution of the wtf gene family. *Molecular biology and evolution*, 36(6):1201–1214.
- Fogarty, L., Wakano, J. Y., Feldman, M. W., and Aoki, K. (2017). The driving forces of cultural complexity. *Human Nature*, 28(1):39–52.

- Frigyik, B. A., Kapila, A., and Gupta, M. R. (2010). Introduction to the dirichlet distribution and related processes. *Department of Electrical Engineering, University of Washignton, UWEETR-2010-0006*, (0006):1–27.
- 720 Henrich, J. and Broesch, J. (2011). On the nature of cultural transmission networks: evidence from fijian villages for adaptive learning biases. *Philosophical Transactions of the Royal Society B:*
- 722 Biological Sciences, 366(1567):1139–1148.
- Henrich, J. and Gil-White, F. J. (2001). The evolution of prestige: Freely conferred deference as a mechanism for enhancing the benefits of cultural transmission. *Evolution and human behavior*, 22(3):165–196.
- 726 Henrich, J. and McElreath, R. (2003). The evolution of cultural evolution. *Evolutionary Anthro*pology: Issues, News, and Reviews: Issues, News, and Reviews, 12(3):123–135.
- 728 Henrich, J. and McElreath, R. (2007). Dual-inheritance theory: the evolution of human cultural capacities and cultural evolution. In *Oxford handbook of evolutionary psychology*.
- 730 Horner, V., Proctor, D., Bonnie, K. E., Whiten, A., and de Waal, F. B. (2010). Prestige affects cultural learning in chimpanzees. *PloS one*, 5(5):e10625.
- Kendal, R., Hopper, L. M., Whiten, A., Brosnan, S. F., Lambeth, S. P., Schapiro, S. J., and Hoppitt, W. (2015). Chimpanzees copy dominant and knowledgeable individuals: implications
 for cultural diversity. Evolution and Human Behavior, 36(1):65-72.
- King, A. J. and Cowlishaw, G. (2009). Leaders, followers, and group decision-making. *Commu-*736 nicative & Integrative Biology, 2(2):147–150.
- McComb, K., Moss, C., Durant, S. M., Baker, L., and Sayialel, S. (2001). Matriarchs as repositories of social knowledge in african elephants. *Science*, 292(5516):491–494.
- Molleman, L., Pen, I., and Weissing, F. J. (2013). Effects of conformism on the cultural evolution of social behaviour. *PloS one*, 8(7):e68153.
- Muthukrishna, M. and Henrich, J. (2016). Innovation in the collective brain. *Philosophical Trans*actions of the Royal Society B: Biological Sciences, 371(1690):20150192.
- Norredam, M. and Album, D. (2007). Prestige and its significance for medical specialties and diseases. Scandinavian journal of public health, 35(6):655–661.
- Ram, Y., Liberman, U., and Feldman, M. W. (2018). Evolution of vertical and oblique transmission under fluctuating selection. *Proceedings of the National Academy of Sciences*, 115(6):E1174–E1183.

- Rendell, L., Boyd, R., Cownden, D., Enquist, M., Eriksson, K., Feldman, M. W., Fogarty, L.,
 Ghirlanda, S., Lillicrap, T., and Laland, K. N. (2010). Why copy others? insights from the social
 learning strategies tournament. Science, 328(5975):208–213.
- Takahashi, T. and Ihara, Y. (2019). Cultural and evolutionary dynamics with best-of-k learning when payoffs are uncertain. *Theoretical Population Biology*, 128:27–38.
- Van Vugt, M. and Smith, J. E. (2019). A dual model of leadership and hierarchy: Evolutionary synthesis. *Trends in Cognitive Sciences*, 23(11):952–967.