

Appendix

Information given

Diameter, $d=0.03\text{m}$ | Length, $L=8\text{ m}$ | Roughness, $\varepsilon/D = 0.00005$ |
 $T_{\text{in}} = 293\text{ K}$ | $P_{\text{in}} = 300\text{ kPa}$ | $P_{\text{atm}} = 101\text{ kPa}$ | $R=8.314$

Information found to be constant:

Gas	Air	Ammonia	Ethylene	Methane	Sulphur dioxide
γ	1.4	1.316	1.2461	1.32	1.26
M	0.029	0.017	0.028	0.016	0.0641
$c = \sqrt{\frac{\gamma RT}{M}}$	342.93	434.25	329.26	448.30	218.82
$\rho = \frac{PM}{RT}$	3.5714	2.0936	3.4483	1.9704	7.8941

Methods to calculate

Choked Conditions

1. Assume that the system is under choked conditions.
2. Guess initial value for f (e.g. = 0.02).
3. Then, solve for Ma_1 since all other variables are ascertained.

$$\frac{\gamma+1}{2} \ln \left[\frac{\left(1 + \frac{\gamma-1}{2} Ma_1^2\right)}{Ma_1^2 \left(1 + \frac{\gamma-1}{2}\right)} \right] - \frac{1}{Ma_1^2} + 1 + \gamma \frac{fL}{d} = 0$$

4. Calculate Re_1 .

$$Re_1 = \frac{(\rho D c) Ma_1}{\mu}$$

5. Calculate new f using the Haaland Equation.

$$\frac{1}{\sqrt{f}} = -1.8 \log_{10} \left[\left(\frac{\varepsilon/D}{3.7} \right)^{1.11} + \frac{6.9}{Re_1} \right]$$

6. Iterate steps 1 – 4 until the new f is closed enough with the old f set. This process is being done by using the ‘loop’ function in matlab with the codes and results attached.
7. Find P_2 with the equation:

$$\frac{P_{2,choked}}{P_1} = Ma_1 \sqrt{\frac{1 + \frac{\gamma-1}{2} Ma_1^2}{1 + \frac{\gamma-1}{2}}}$$

And check to see if $P_{2,choked} > P_{atm}$ (100kPa). If $P_{2,choked} < P_{atm}$, the choked assumption is wrong and move on to solve the unchoked conditions (Step 9).

8. If $P_{2,choked} > P_{atm}$, calculate the mass flow rate. $Q_m = \rho VA = A Ma_1 P_1 \sqrt{\frac{\gamma M}{RT_1}} = A Ma_2 P_2 \sqrt{\frac{\gamma M}{RT_2}}$

Unchoked Conditions

9. Guess initial value of Ma_1 (e.g. = 0.3).
10. Calculate Re_1 and f as per steps 4 & 5 respectively.
11. Solve for Ma_2 .

$$\frac{\gamma+1}{2} \ln \left[\frac{Ma_2^2 \left(1 + \frac{\gamma-1}{2} Ma_1^2 \right)}{Ma_1^2 \left(1 + \frac{\gamma-1}{2} Ma_2^2 \right)} \right] - \frac{1}{Ma_1^2} + \frac{1}{Ma_2^2} + \gamma \frac{fL}{d} = 0$$

12. Check to see if P_2 is correct ($= P_{atm}$, 100kPa)

$$\frac{P_2}{P_1} = \frac{Ma_1}{Ma_2} \sqrt{\frac{1 + \frac{\gamma-1}{2} Ma_1^2}{1 + \frac{\gamma-1}{2} Ma_2^2}}$$

13. If P_2 is incorrect, guess a new value for Ma_1 and repeat steps 9 – 12 until $P_2 = P_{atm}$. Once correct, stop the iterations.
14. Calculate the mass flow rate.

$$Q_m = \rho VA = AMa_1 P_1 \sqrt{\frac{\gamma M}{RT_1}} = AMa_2 P_2 \sqrt{\frac{\gamma M}{RT_2}}$$

See Matlab code below: